Consultative Committee for Space Data Systems

REPORT CONCERNING SPACE
DATA SYSTEM STANDARDS

BANDWIDTH-EFFICIENT MODULATIONS

SUMMARY OF DEFINITION, IMPLEMENTATION, AND PERFORMANCE

CCSDS 413.0-G-1

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FOREWORD

This Report contains technical material to supplement the CCSDS Recommendations for the standardization of modulation methods for high symbol rate transmissions generated by CCSDS Member Agencies.

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1   INTRODUCTION

1.1   PURPOSE AND SCOPE

Since their inception, the various international space agencies have operated an ever-increasing number of science missions in the Earth Exploration Satellite Service (EESS) and Space Research Service (SRS) bands. The data transport requirements of these missions have also continued to escalate, with the result that the finite spectrum resources are now becoming increasingly strained.

To mitigate this situation and reduce the possibility of adjacent channel interference, spectrum advisory and regulatory agencies such as the SFCG and the ITU have recently enacted out-of-band emission mask recommendations. These masks are designed to severely restrict the power in that portion of transmitted signal falling outside some necessary bandwidth.

CCSDS has responded by developing a series of recommendations for standard bandwidth efficient modulation techniques applicable to high rate missions in selected SRS and EESS bands. These modulations were selected based on their spectral containment characteristics, with the characteristics of the SFCG Recommendation 17-2R1 mask[1] serving as a minimum requirement. Bit Error Rate (BER) performance, compatibility with existing infrastructure, and suitability for cross-support were also significant factors in selecting modulations for these recommendations.

This Green Book provides the background information for CCSDS recommendations 401(2.4.17A), 401(2.4.17B) and 401(2.4.18) addressing the use of bandwidth efficient modulations for spacecraft telemetry which were approved by the Management Council in June 2001. This document provides a technical specification for the modulation techniques approved in the above mentioned recommendations, together with a description of their main performance characteristics for the applications covered by the recommendations.   All figures are simulations unless noted otherwise.

This document includes two annexes. Annex A is a glossary of acronyms used in the document. Annex B provides simulated performance data of the efficient modulations when amplified by an SSPA operating with 0 dB output backoff referenced to maximum output power. This data includes occupied bandwidth, BER, and interference susceptibility of the bandwidth efficient modulations. The data provided in annex B is indicative of system performance expected using the reference model. Performance of other systems will be highly dependent upon their transmitter and receiver characteristics. The performance data in annex B was extracted from study reports available in [1].

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[1] Modified and renumbered in 2001 as SFCG Recommendation 21-2.

1.2   APPLICABILITY

The modulation techniques described in this document are applicable to high symbol rate (> 2 Msps) telemetry transmissions for missions in the SRS and EESS. Three classes of modulation techniques are identified:

– Those dedicated to space research, Category A missions, specified in Recommendation 401(2.4.17A) B-1. They are applicable to frequency bands 2200-2290 MHz and 8450-8500 MHz.

– Those dedicated to space research, Category B missions, specified in Recommendation 401(2.4.17B) B-1. They are applicable to frequency bands 2290-2300 MHz and 8400-8450 MHz.

– Those dedicated to Earth exploration satellite missions, specified in Recommendation 401(2.4.18) B-1. They are applicable to the frequency band 8025-8400 MHz.

It should be noted that, *sensu stricto*, the above recommendations are only applicable to the mentioned frequency bands. However, the user should take note that extension to other SRS and/or EESS frequency bands could be envisaged in the future.

In no event will CCSDS or its members be liable for any incidental, consequential, or indirect damages, including any lost profits, lost savings, or loss of data, or for any claim by another party related to errors or omissions in this report.

1.3   REFERENCES

The following documents are referenced in this Report. At the time of the publication the indicated editions were valid. All documents are subject to revision, and users of this Recommendation are encouraged to investigate the possibility of applying the most recent editions of the documents indicated below. The latest issues of CCSDS documents may be obtained from the CCSDS Secretariat at the address indicated on page ii.

[1]   *Proceedings of the CCSDS RF and Modulation Subpanel 1E on Bandwidth-Efficient Modulations*. CCSDS B20.0-Y-2. Yellow Book. Issue 2. Washington, D.C.: CCSDS, June 2001.

[2]   *Radio Frequency and Modulation Systems—Part 1: Earth Stations and Spacecraft*. Recommendations for Space Data System Standards, CCSDS 401.0-B. Blue Book. Revision 10. Washington, D.C.: CCSDS, March 2003.

[3]   *Procedures Manual for the Consultative Committee for Space Data Systems*. CCSDS A00.0-Y-8. Yellow Book. Issue 8. Washington, D.C.: CCSDS, July 2002.

[4]   K. Murota and K. Hirade. 'GMSK Modulation for Digital Mobile Radio Telephony'. *IEEE Transactions on Communications*, vol. COM-29, no. 7 (July 1981): 1044-1050.

[5]   K. Feher, et al. U.S. Patent Nos. 4,567,602 (1986), 4,644,565 (1987), and 5,784,402 (1998); WIPO PCT International Publication No. WO 00/10272 and European Patent EP1104604 (2000).

[6]   M. Simon and T.-Y. Yan. 'Performance Evaluation and Interpretation of Unfiltered Feher-Patented Quadrature Phase Shift Keying (FQPSK)'. In *Proceedings of the CCSDS RF and Modulation Subpanel 1E on Bandwidth-Efficient Modulations*. CCSDS B20.0-Y-2. Yellow Book. Issue 2, 2-61–2-89. Washington, D.C.: CCSDS, June 2001.

[7]   S. Kato and K. Feher.   'XPSK: A New Cross-Correlated Phase-Shift-Keying Modulation Technique'. *IEEE Transactions on Communications*, vol. 31, no. 5 (May 1983): 701-707, .

[8]   'NASA GSFC Efficient Spectrum Utilization Analysis'. In *Proceedings of the CCSDS RF and Modulation Subpanel 1E on Bandwidth-Efficient Modulations*. CCSDS B20.0-Y-2. Yellow Book. Issue 2, 1-257–1-399. Washington, D.C.: CCSDS, June 2001.

[9]   J. Proakis and D. Manolakis. *Introduction to Digital Signal Processing*. New York: MacMillan, 1988.

[10] T. Hill. 'An Enhanced Constant Envelope, Interoperable Shaped Offset QPSK (SOQPSK) Waveform for Improved Spectral Efficiency'. *Proceedings of the 2000 International Telemetering Conference* (2000): 127-135.

[11] M. Geoghegan. 'Bandwidth and Power Efficiency Tradeoffs of SOQPSK'. *Proceedings of the 2002 International Telemetering Conference* (2002).

[12] M. K. Simon, P. Arabshahi, and M. Srinivasan. 'Trellis-Coded Quadrature Phase Shift Keying (QPSK) with Variable Overlapped Raised Cosine Pulse Shaping'. In *Proceedings of the CCSDS RF and Modulation Subpanel 1E on Bandwidth-Efficient Modulations*. CCSDS B20.0-Y-2. Yellow Book. Issue 2, 4-1–4-16. Washington, D.C.: CCSDS, June 2001.

[13] G. Ungerboeck. 'Channel Coding with Multilevel/Phase Signals'. *IEEE Transactions on Information Theory*, vol. IT-28, no. 1 (1982): 55-67.

[14] S. Pietrobon et al. 'Trellis-Coded Multidimensional Phase Modulation'. *IEEE Transaction on Information Theory*, vol. 36, no. 1 (1990): 63-89.

[15] M. Austin and M. Chang. 'Quadrature Overlapped Raised-Cosine Modulation'. *IEEE Transactions on Communications*, vol. COM-29, no. 3 (1981): 237-249.

[16] S. S. Shah, et. al., 'Self Correcting Codes Conquer Noise Part 1: Viterbi Codecs'. *EDN* (February 15, 2001): 131-140.

[17] W. Martin, et al.. 'CCSDS-SFCG Efficient Modulation Methods Study at NASA/JPL, Phase 4: Inteference Susceptibility'. In *Proceedings of the CCSDS RF and Modulation Subpanel 1E on Bandwidth-Efficient Modulations*. CCSDS B20.0-Y-2. Yellow Book. Issue 2, 1-171–1-212. Washington, D.C.: CCSDS, June 2001.

[18] G. Povero, E. Vassallo, and M. Visintin. 'Interference Susceptibility of Selected Bandwidth-Efficient Modulation Schemes'. In *Proceedings of the CCSDS RF and Modulation Subpanel 1E on Bandwidth-Efficient Modulations*. CCSDS B20.0-Y-2. Yellow Book. Issue 2, 1-473–1-492. Washington, D.C.: CCSDS, June 2001.

2 SCOPE OF BANDWIDTH-EFFICIENT MODULATIONS

2.1 LIMITED SPECTRAL RESOURCES FOR SPACE TELEMETRY

The Category A SRS frequency band 2200-2290 MHz is currently heavily used by space research and space operations missions for their telemetry transmissions and the density of users of the band keeps increasing over the years. In addition, while until recently all these users were rather modest in telemetry symbol rate transmission, more and more new missions are appearing with telemetry symbol rates well above 1 Msps. In order to avoid a rapid saturation of the band with unsolvable interference conflicts, the CCSDS has issued Recommendation 401(2.4.17A) for a limited set of common bandwidth-efficient modulation schemes to be used for high symbol rate transmissions, thus ensuring not only an optimum use of the band but also inter-agency cross-support capability. The Recommendation is also applicable to the 8450-8500 MHz band for which a number of missions with high rate telemetry have already been earmarked.

Likewise, Recommendation 401(2.4.17B) B-1 addresses the Category B SRS bands 2290-2300 MHz and 8400-8450 MHz. These recommended modulations have been selected for their low loss and their bandwidth compactness.

Recommendation 401(2.4.18) B-1 addresses the EESS payload telemetry bands 8025-8400 MHz and 25.5-27 GHz. The band available at 8 GHz is only 375 MHz while some EESS missions are under preparation plan to transmit hundreds of Megabits per second of payload data leading to channel symbol rates possibly up to 1 Gsps. The problem is two-fold: the physical limitation of the band in terms of transmission rate capacity and the increased risk of interference. CCSDS policy as expressed in Recommendation 401(2.4.18) is to promote the use of a very compact modulation scheme for use in the 8 GHz band and to encourage the very high rate users to migrate to the 26 GHz band.

2.2 REGULATIONS: THE SFCG SPECTRAL MASK

The SFCG was established to provide a less formal and more flexible environment, compared to the official organs of the ITU, for the solution of frequency management problems encountered by member space agencies. Recognizing that the SRS and EESS frequency bands were increasingly congested and concerned with the effective use of those bands, the SFCG approved Recommendation 17-2R1 in 1999 which established spectral emission limits for space-to-Earth links in the space science services. Separate spectral emissions masks were established for missions with telemetry data rates less than 2 Msps and for those with data rates greater than 2 Msps.

In October of 2001, the 17-2R1 mask was modified and renumbered 21-2 for Category A bands 2200-2290 MHz, 8025-8400 MHz, and 8450-8500 MHz. The mask for space-to-Earth links in the Category B bands 2290-2300 MHz and 8400-8450 MHz is currently being addressed by SFCG. The SFCG Recommendations currently in-force can be found at the SFCG website http://www.sfcgonline.org/.

2.3   A SELECTION OF BANDWIDTH-EFFICIENT MODULATION METHODS

The selection of modulation schemes is the result of compromises on a number of criteria:

–   bandwidth efficiency;

–   link performances (in terms of BER);

–   implementation complexity and cost: onboard transmitter, ground receiver;

–   robustness: susceptibility to interferers;

–   programmatic aspects: cross-compatibility.

2.3.1   MODULATION METHODS FOR SRS, CATEGORY A

Due to the wide range of applications, ranging from the low Earth orbiters to the science spacecraft at the edge of the Category A region (2×10^6 km), a number of different modulation schemes were retained in Recommendation 401(2.4.17A) B-1:

–   GMSK[2] (BT_s=0.25) with precoding;

–   FQPSK-B[3];

–   Filtered OQPSK[2] with various options:

•   SRRC,[2] α=0.5;

•   Butterworth 6 poles, BT_s=0.5;

•   Shaped OQPSK[2]-A & -B;

•   Other filters meeting the requirements of the SFCG mask and interoperable with the cross-supporting networks.

2.3.2   MODULATION METHODS FOR SRS, CATEGORY B

For SRS Category B missions, two modulations were retained in recommendation 401(2.4.17B) B-1:

–   GMSK (BT_s=0.5) with precoding;

–   Trellis-coded OQPSK.

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[2] These terms are defined in sections 3 and 4.

[3] Feher-patented Quadrature Phase Shift Keying modulation.

2.3.3 MODULATION METHODS FOR EESS AT 8 GHZ

Recommendation 401 (2.4.18) recommends that EESS missions planning to use conventional modulation techniques[4] which have an occupied bandwidth[2] exceeding that permitted by the SFCG use 4-dimensional 8PSK Trellis Coded Modulation (TCM) instead. It also recommends that users migrate to the 25.5-27 GHz band in case of very large occupied bandwidth.

2.4 BIT AND SYMBOL RATE TERMINOLOGY

In the literature, the notations used for bit rate and symbol rate sometimes have different meanings. For this Green Book, R_b refers to the information bit rate and R_{ChS} refers to the channel symbol rate after the modulator. R_s is used to denote the coded symbol rate measured at the input of the modulator. If no error correcting coding nor Bi-ϕ formatting is used, then R_s is equal to the information bit rate R_b. Likewise, T_b is the bit period, T_s is the coded symbol period, and T_{ChS} is the channel symbol period. If there is no error correcting coding nor Bi-ϕ formatting, $T_s = T_b$.

Figure 2-1 shows the relationship between the different terms.
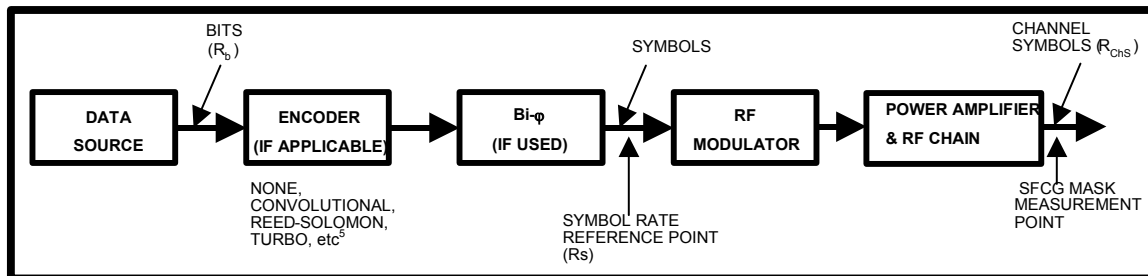
Figure 2-1: Bit and Symbol Rate Terminology

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[4] As defined in CCSDS Recommendation 401(2.4.1).

[5] See *Telemetry Channel Coding*, CCSDS 101.0-B-6, October 2002.

3 TECHNICAL DEFINITIONS

3.1 PRECODED GMSK

3.1.1 INTRODUCTION

Gaussian Minimum Shift Keying (GMSK) is a constant envelope, continuous phase modulation first introduced in 1981 by Hirade et. al. (reference [4]). It is derived from Minimum Shift Keying (MSK) with the addition of a baseband Gaussian filter that further reduces sidelobe levels and spectral bandwidth. The product of the Gaussian filter bandwidth and the coded symbol period at the input to the modulator, referred to as the BT_s factor, is used to differentiate between GMSK modulations of varying bandwidth efficiencies. If there is no coding, BT_s refers to the filter bandwidth times the bit period.[6] In general, a smaller BT_s factor results in less spectral bandwidth occupancy but greater intersymbol interference which can be compensated for using equalization or trellis demodulation. GMSK has a constant envelope which reduces spectral regrowth and signal distortion due to amplifier nonlinearity.

Like MSK, GMSK is inherently a differential Continuous Phase Modulation (CPM) (i.e., the information is carried in the change of the phase rather than the phase itself). For a coherent In-phase/Quadrature (I/Q) demodulator, a differential decoder is needed at the receiver which increases the BER by approximately a factor of two. By precoding the GMSK signal at the transmitter to remove the inherent differential encoding, the BER can be halved. Figure 3-1 shows a block diagram of the precoder were $d_k \in \{\pm 1\}$.
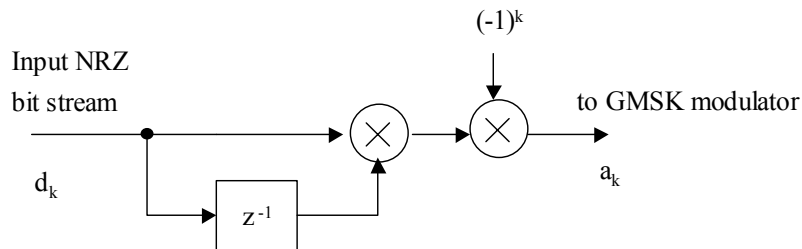
Figure 3-1: GMSK Precoder

3.1.2 SIGNAL MODEL

Mathematically, the precoded GMSK modulated RF carrier is expressed as:

$$x(\tau) = \sqrt{2P} \cos\left(2\pi f_c \tau + \varphi(\tau) + \varphi_0\right)$$

---

[6] See 2.4 for bit/symbol terminology definitions used in this Green Book.

where

> P is the power of the carrier;
> f_c is the center frequency;
> $\varphi(\tau)$ is the phase of the modulated carrier;
> φ_0 is a constant phase offset;

and

$$\varphi(t) = \sum_k (a_k \frac{\pi}{2} \int_{-\infty}^{t-kT_s} g(\tau)d\tau)$$

where $a_k = (-1)^k d_k d_{k-1}$ are the pre-coder output symbols and $d_k \in \{\pm 1\}$ is the k-th coded symbol to be transmitted.

The instantaneous frequency pulse $g(\tau)$ can be obtained through a linear filter with impulse response defined by:

$$g(\tau) = h(\tau) \ * rect\ (\tau/T_s)$$

where * denotes convolution and *rect(x)* is the function:

$$rect\ (\tau/T_s) = 1\ /\ T_s\ \ for\ \left|\tau\right| < T_s/2$$
$$rect\ (\tau/T_s) = 0\ \ \ \ otherwise$$

and *h(t)* is the Gaussian filter impulse response:

$$h(t) = \frac{1}{\sigma T_s \sqrt{2\pi}} e^{-\frac{t^2}{2\sigma^2 T_s^2}}$$

where

$$\sigma = \frac{\sqrt{\ln(2)}}{2\pi B T_s}$$

and

> $\ln (\bullet)$ is the natural logarithm (base $= e$)
> $B =$ one-sided 3-dB bandwidth of the filter with impulse response h(t)
> $T_s =$ the duration of a coded symbol at the input to the modulator

3.1.3   GMSK MODULATOR

3.1.3.1   General

There are two common methods of generating GMSK, one as a Frequency Shift Keyed (FSK) modulation and the other as an offset quadrature phase shift keyed modulation. Figure 3-2 shows GMSK generated as an FSK modulation using a Voltage Controlled Oscillator (VCO) as first described in reference [4]. Figure 3-3 shows GMSK generated using a quadrature baseband method.

Figure 3-4 shows the simulated spectrum of GMSK BT_s=0.25 and BT_s=0.5 at the output of the saturated SSPA referenced in annex B. The SFCG Recommendation 21-2 spectral high data rate mask is also plotted, and it can be clearly seen that GMSK with either BT_s factor meets the requirements of the mask.
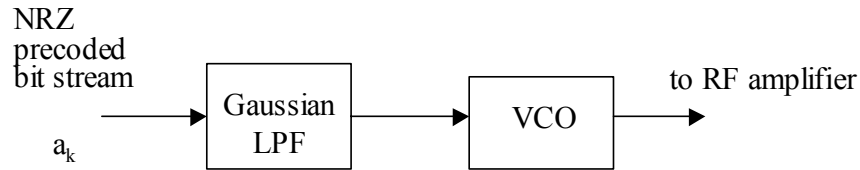
Figure 3-2: GMSK: Generated Using VCO
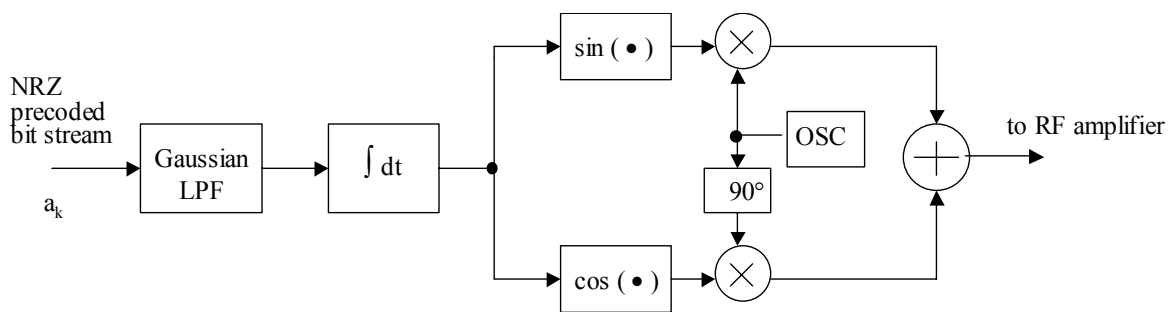
Figure 3-3: GMSK Using a Quadrature Modulator
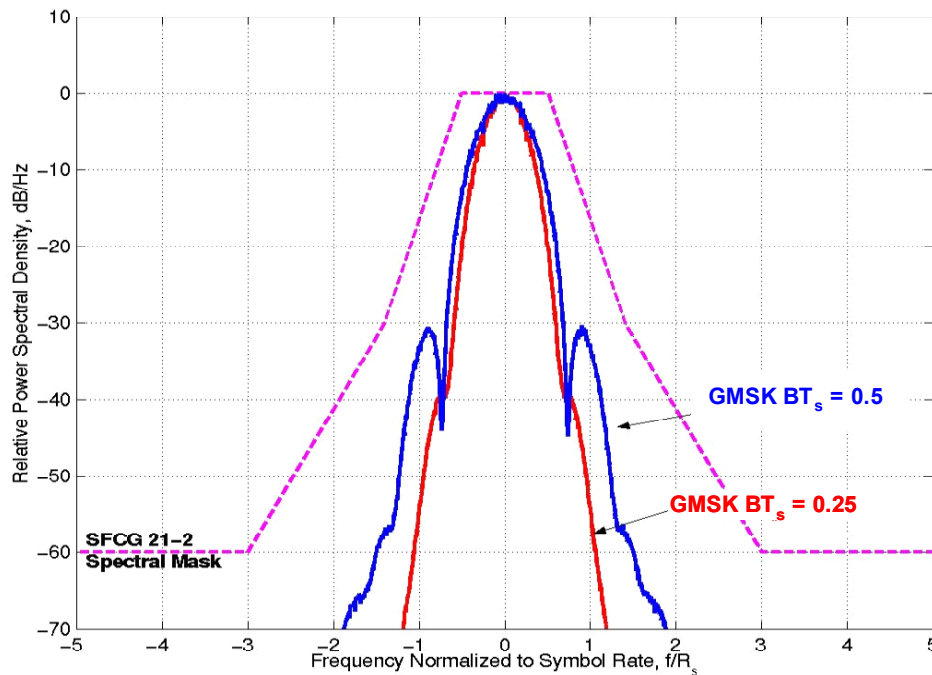
Figure 3-4: Simulated GMSK Spectrum at Output of Saturated SSPA

3.1.3.2 Symbol Asymmetry in Analog GMSK Transmitters

The analog transmitter implementations shown in figures 3-2 and 3-3 may suffer from the impairment known as data asymmetry, i.e., unequal rise and fall times of the logic gating circuits which generate the input NRZ signal (see figure 3-5). With symbol asymmetry, the positive to negative transitions occur at time instants $kT_s \pm \eta T_s$ instead of kT_s. The discussions below assume the case of $kT_s + \eta T_s$.
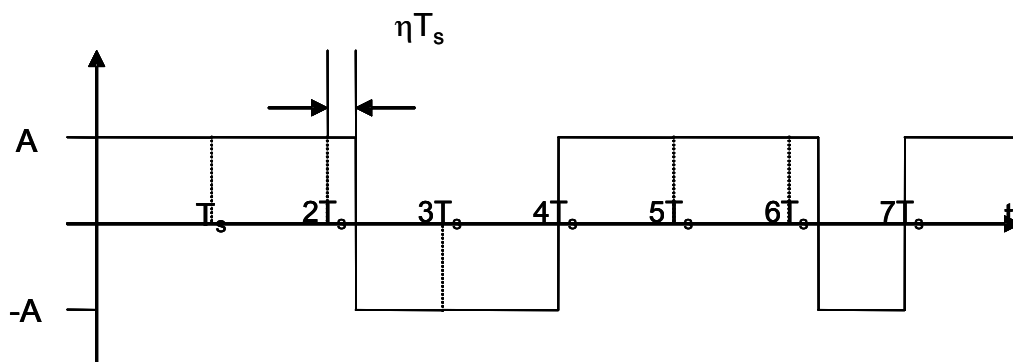
Figure 3-5: NRZ Signal Affected by Symbol Asymmetry (η=0.25)

In the presence of symbol asymmetry, the mean value of the NRZ signal is equal to *$2\eta Ap$*, where p is the probability that a negative-going transition occurs. If the positive and negative levels are equally likely (i.e., no data imbalance) and p=1/4, the NRZ signal mean value is $\eta A/2$. The signal at the output of the modulator has an instantaneous frequency deviation $f(t)=d\varphi(t)/dt$ with an average value $\mu_f=\eta/8T_s$, so its true center frequency is $f_c+\mu_f$ instead of f_c. The receiver carrier phase synchronizer is able to compensate for the frequency offset as long as its loop bandwidth B_L is larger than μ_f. However, intersymbol interference due to symbol asymmetry cannot be eliminated and the resulting loss can be measured in terms of signal to noise ratio necessary for given BER. For $\eta \leq 0.002$, the E_s/N_o degradation at the output of the GMSK receiver is lower than 0.1 dB.
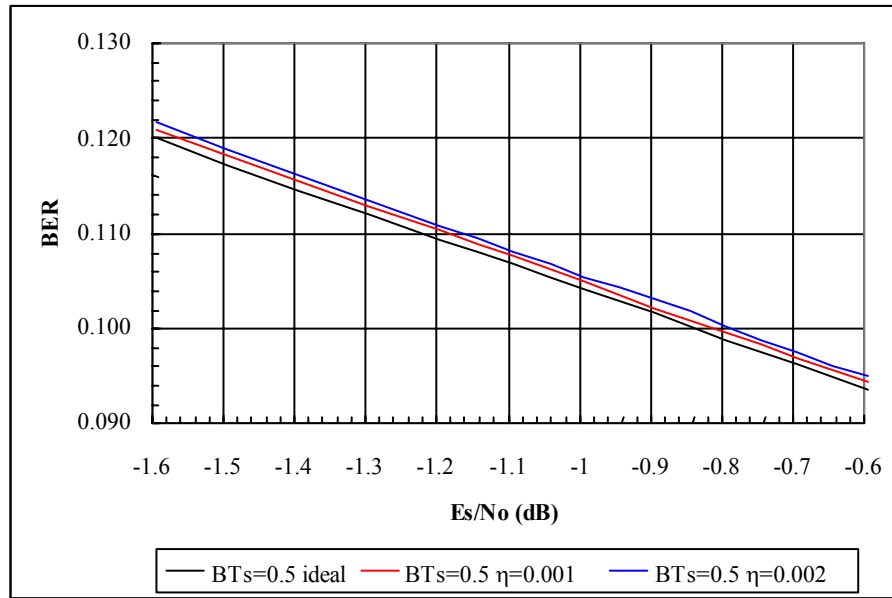
Figure 3-6: **Bit Error Rate (BER) at the Output of the GMSK Receiver in the Presence of Data Asymmetry; Case of BT_s=0.5**
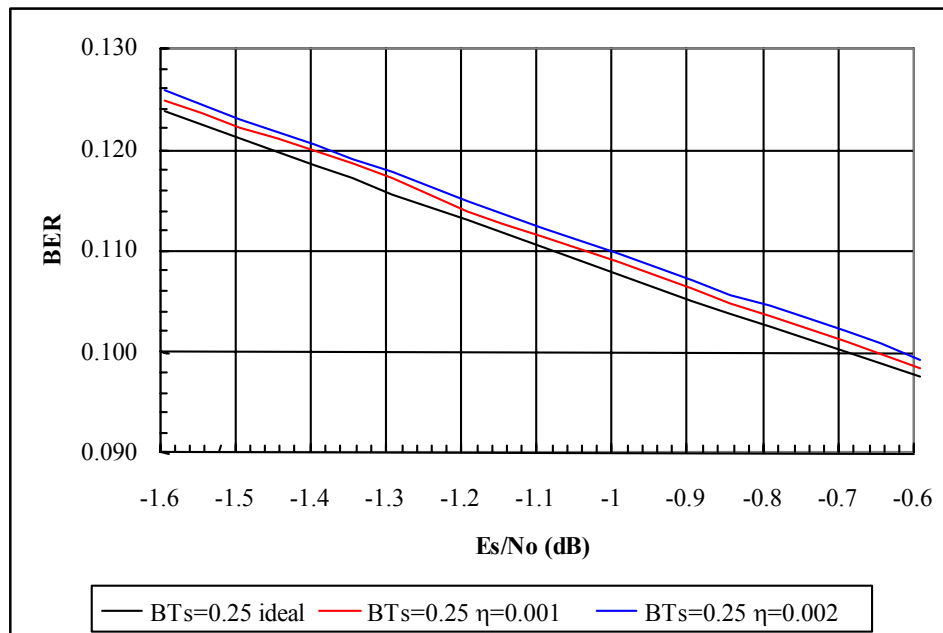
Figure 3-7: **Bit Error Rate (BER) at the Output of the GMSK Receiver in the Presence of Data Asymmetry; Case of BT_s=0.25**

3.1.3.3 Carrier Phase/Amplitude Imbalance in Quadrature GMSK Transmitters

In the quadrature GMSK modulator, two orthogonal sinusoidal signals are generated from one oscillator, using a $\pi/2$ phase shifter. The presence of carrier phase/amplitude imbalance due to implementation gives rise to spectral lines in the power spectrum of the transmitted signal and BER degradation at the receiver output. Simulations showed that the coherent receiver finds its stable phase reference at $\theta/2$ and that the loss due to increased intersymbol interference is negligible as long as θ is less than 2° and the amplitude imbalance is lower than 0.2 dB (see figure 3-7).
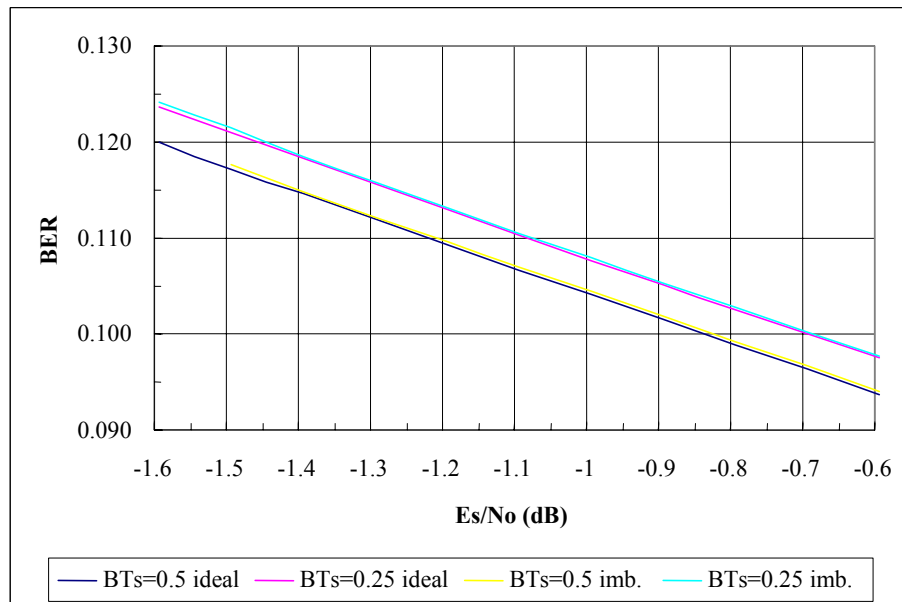
Figure 3-8: Bit Error Rate (BER) at the Output of the GMSK Receiver in the Presence of Carrier Phase/Amplitude Imbalance

3.1.3.4 Parameters to be Used in Digital GMSK Transmitters

Full digital transmitters may be developed, based on the schemes of figures 3-2 and 3-3. The NRZ signal is sampled using N_b samples per coded symbol at the input to the modulator, and an FIR filter with impulse response $h[n]$ is used instead of the analog Gaussian filter. This type of transmitter is denoted here as FM-2 if the VCO is present (figure 3-2) and IQ-2 if the IQ transmitter is present (figure 3-3). The value of N_b, the number of taps N_T of the FIR filter, and the number of quantization bits N_q to be used in the FIR filter must be found so that the introduced approximations in the transmitted signal are negligible. Another possibility, which shall be called FM-1, is shown in figure 3-9. In this case, the NRZ input signal is sampled using one sample per bit. An oversampler introduces N_b-1 zeros between the two input samples and generates a train of discrete deltas which feed an FIR filter with impulse response $g[n]$. In figure 3-9 the digital to analog conversion is placed right after the

FIR filter because an analog VCO is used, but a numerically controlled oscillator can be used instead. Moreover, a quadrature modulator may be used instead of the VCO, as in figure 3-3.
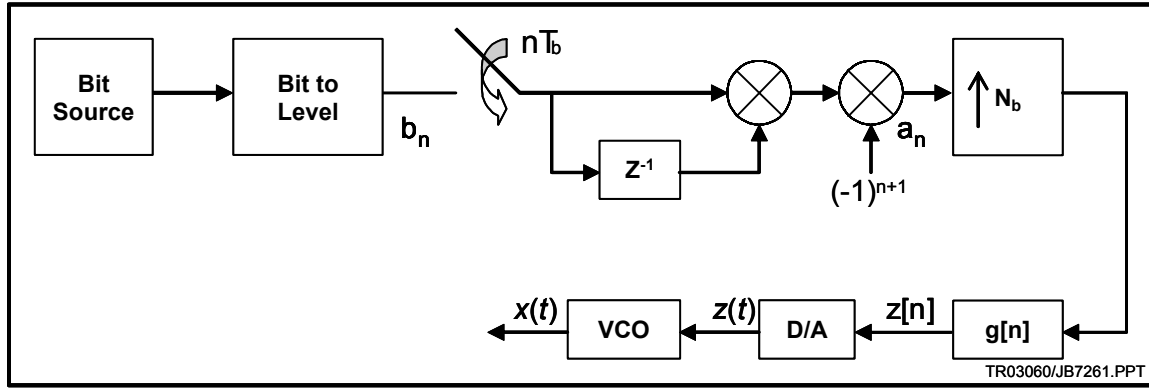
Figure 3-9: The FM-1 Implementation of the Precoded GMSK Transmitter

Another quadrature modulator (IQ-L1) can be designed, based on the Laurent decomposition of the GMSK signal complex envelope (see figure 3-11):

$$\tilde{x}(t) \approx A_c \sum_{n=-\infty}^{\infty} [b_{2n} C_0(t - 2nT_s) - b_{2n+1} b_{2n} b_{2n-1} C_1(t - 2nT_s - T_s)]$$

$$+ jA_c \sum_{n=-\infty}^{\infty} [b_{2n+1} C_0(t - 2nT_s - T_s) - b_{2n} b_{2n-1} b_{2n-2} C_1(t - 2nT_s)]$$

where $C_0(t)$ and $C_1(t)$ are shown in figure 3-10 for BT_s=0.5 and BT_s=0.25.
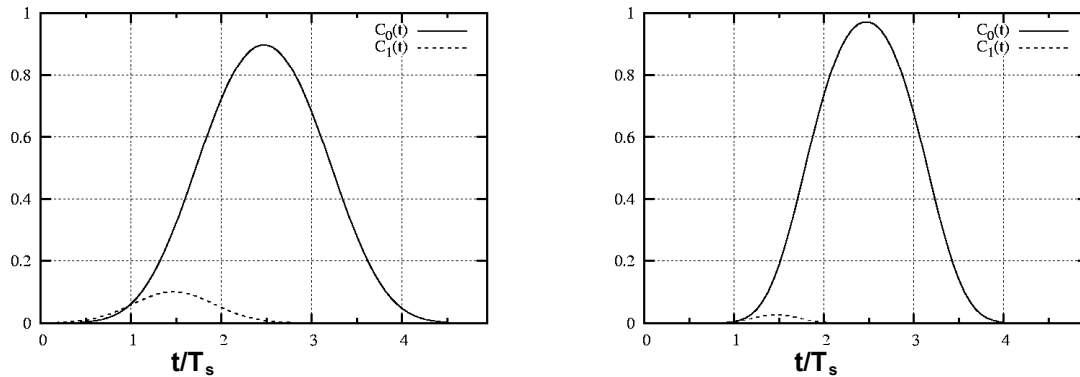
Figure 3-10: Pulses $C_0(t)$ and $C_1(t)$ with BT_s=0.25 (left) and BT_s=0.5 (right)
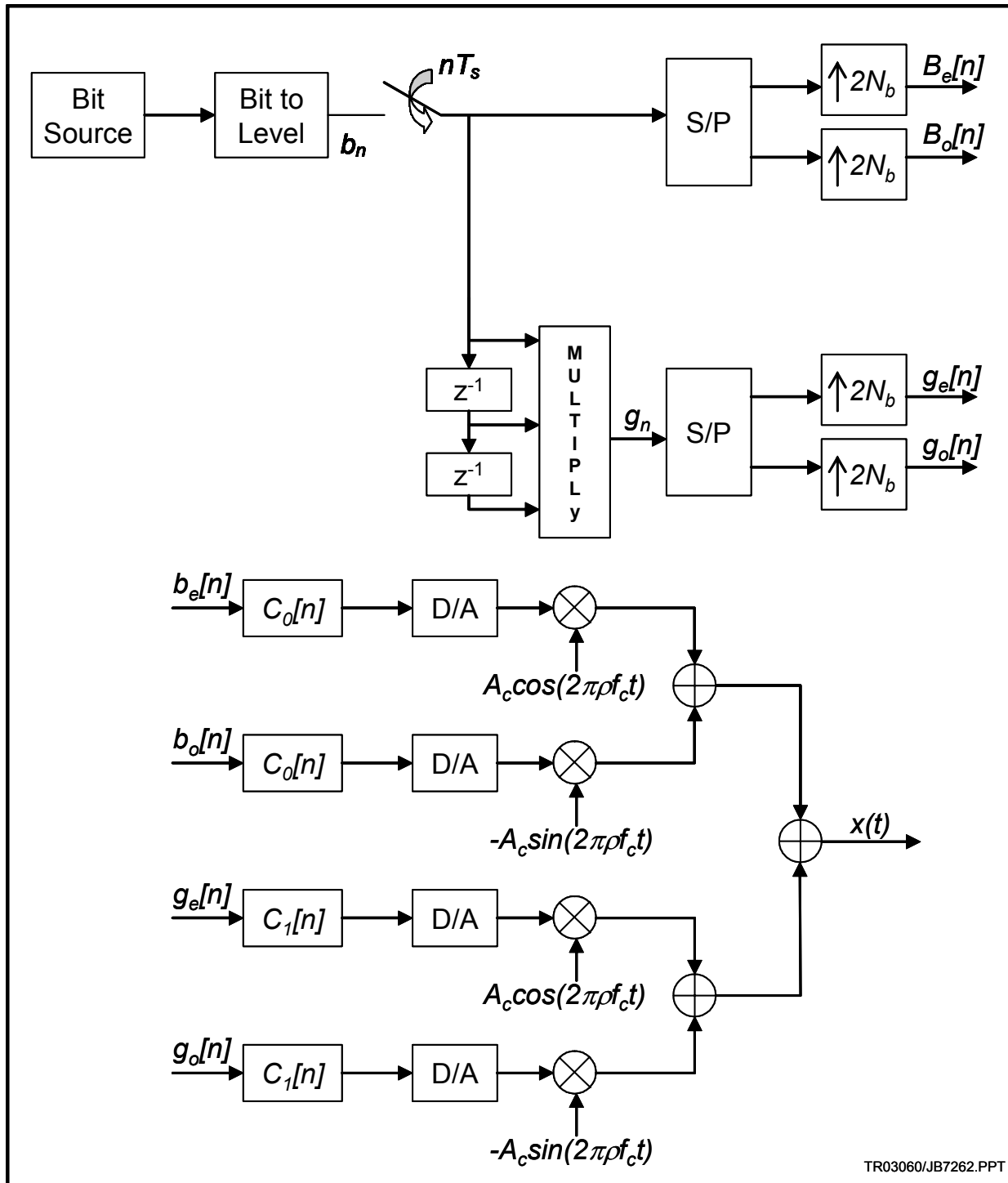
Figure 3-11: IQ-L1 Implementation of the Transmitter

The complex envelopes of the signals generated with transmitter of figure 3-11 using only one Amplitude (AMP) component (only $C_0(t)$) or both components are shown in figures 3-12 and 3-13 for BT_s=0.5 and BT_s=0.25, respectively. The use of both components is needed for GMSK with BT_s=0.25, while only one component is needed for the generation of the GMSK signal with BT_s=0.5.
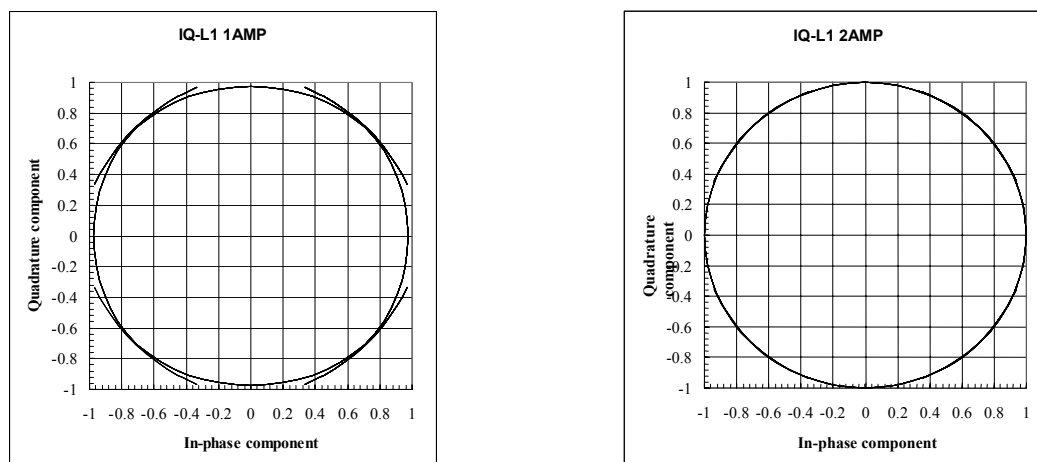
Figure 3-12: **Scattering Diagram for the IQ-L1 Implementation with 1 and 2 Amplitude Components; GMSK with BT_s=0.5**
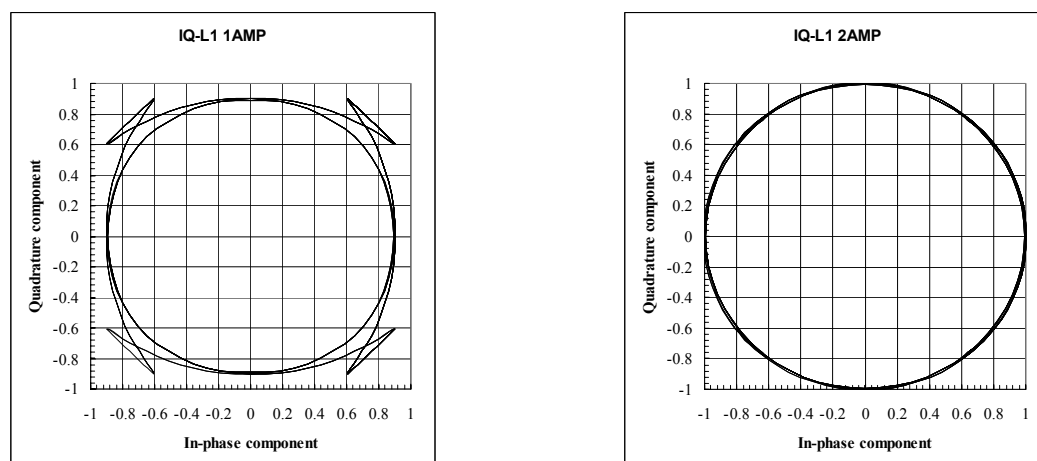
Figure 3-13: **Scattering Diagram for the IQ-L1 Implementation with 1 and 2 Amplitude Components; GMSK with BT_s=0.25**

The parameters that give negligible distortions in the transmitted signal are presented here. For BT_s=0.25, $N_b \geq 4$ and $N_q \geq 12$ are needed for all the implementations. For BT_s=0.5, $N_b \geq 4$ and $N_q \geq 12$ are needed for the IQ-L1 transmitter, while $N_b \geq 4$ and $N_q \geq 16$ are needed for the other implementations. In order to correctly implement the Gaussian filter, the number of taps N_T must be at least $5N_b$ for GMSK with BT_s=0.25, and at least $4N_b$ for GMSK with BT_s=0.5. For the filter with impulse response $g[n]$, the number of taps N_T must be at least $6N_b$ for GMSK with BT_s=0.25, and at least $5N_b$ for GMSK with BT_s=0.5. For the filter with impulse response $C_0[n]$, the number of taps N_T must be at least $4N_b$ for GMSK with BT_s=0.25 and 0.5, while $C_1[n]$ requires $2N_b$ taps. Figures 3-14 and 3-15 show the eye patterns of the signals at the output of the receiver filter (in-phase component) for pre-coded GMSK with BT_s=0.5 and BT_s=0.25. The intersymbol interference present in the case BT_s=0.25 may be reduced by including a 3-tap equalizer (Wiener filter) with weights $w_0 = w_2 = -0.0859984$, $w_1 = 1.0116342$ and delay equal to $2T_s$ between taps. The eye pattern at the output of the equalizer is shown in figure 3-16. The simulated power spectra obtained with an FM-2 implementation and with an IQ-L1 implementation with the above parameters are shown in figures 3-16 and 3-17.
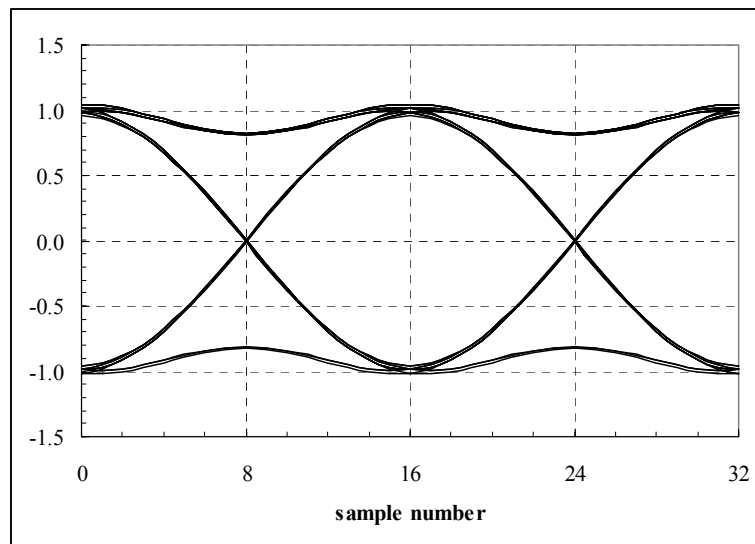
Figure 3-14:   Eye Pattern at the Output of the Receiver Filter for GMSK with BT_s=0.5
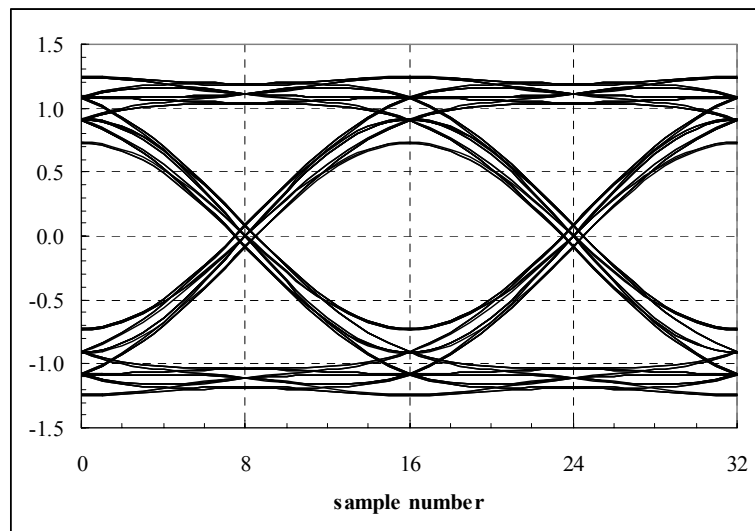
Figure 3-15: **Eye Pattern at the Output of the Receiver Filter for GMSK with BT_s=0.25**
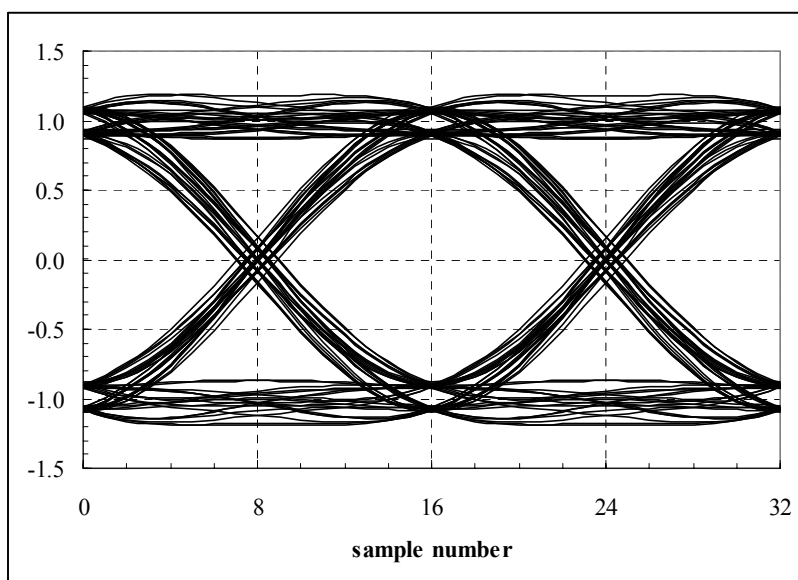
Figure 3-16: **Eye Pattern at the Output of the Wiener Equalizer for GMSK with BT_s=0.25**
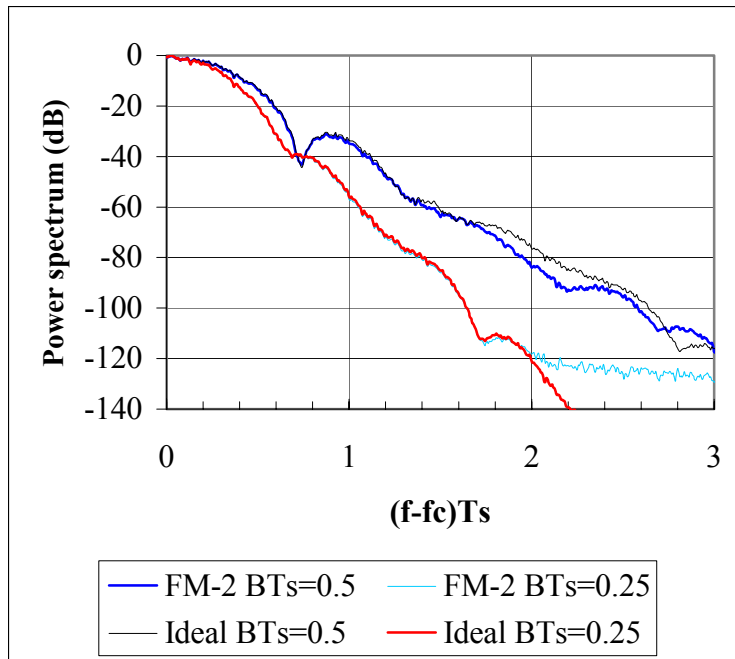
Figure 3-17: **Comparison of the GMSK BT_s=0.5 Power Spectra Obtained with an Ideal Transmitter and an FM-2 Transmitter**
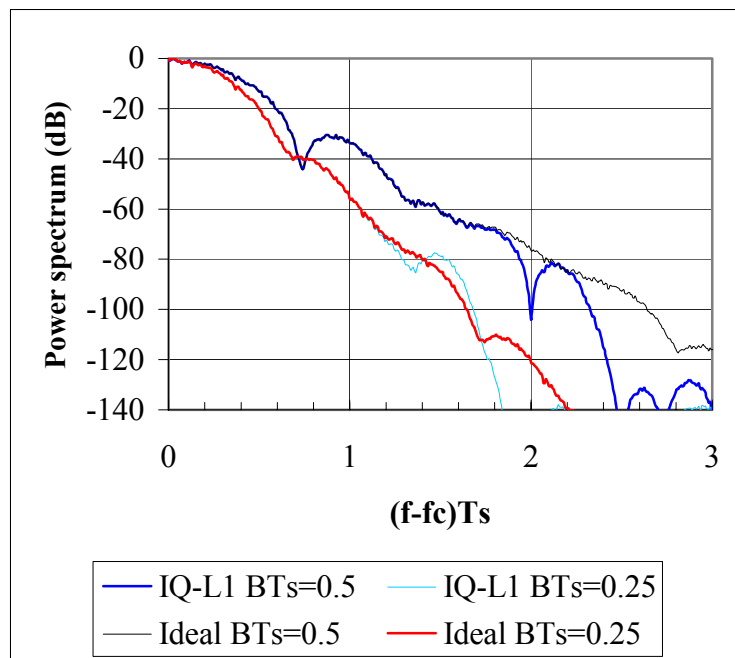
Figure 3-18: **Comparison of the GMSK BT_s=0.5 Power Spectra Obtained with an Ideal Transmitter and an IQ-L1 Transmitter**

3.2   FQPSK-B

3.2.1   INTRODUCTION

The Feher-patented Quadrature-phase-shift Keying, type B (FQPSK-B) modulation scheme is a proprietary bandwidth-efficient modulation technique (reference [5]) invented by Dr. Kamilo Feher.[7]   FQPSK-B is a variant of the cross-correlated FQPSK scheme (originally referred to as XPSK in reference [7]) which in turn was derived from a previous modulation scheme also invented by Dr. Feher known as Inter-symbol-interference and Jitter-Free (IJF) QPSK (reference [5]). With FQPSK as well as FQPSK-B, there is an intentional controlled amount of cross-correlation between the In-phase (I) and Quadrature-phase (Q) channels which allows for a quasi-constant envelope. FQPSK-B improves spectral efficiency over FQPSK because low-pass filtering is applied to the baseband I- and Q-channel waveforms. When properly designed and specified, a system using FQPSK-B is interoperable with other modulation schemes such as OQPSK, GMSK, and MSK.

3.2.2   SIGNAL MODEL

It has been shown that the FQPSK signal (or XPSK signal) can be realized using either a half-symbol cross-correlation mapping originally described in reference [7] or a full-symbol mapping given in reference [6]. In this subsection, the full-symbol cross-correlation mapping is described instead of the half-symbol mapping because the full-symbol mapping facilitates the interpretation of the FQPSK as a TCM.[8]

The unfiltered FQPSK signal can be represented by:

$$S_{XPSK}(t) = S_{FQPSK}(t) = \sqrt{P}S_I(t)\sin(2\pi f_c t + \theta_c) + \sqrt{P}S_Q(t - T_{ChS}/2)\cos(2\pi f_c t + \theta_c)$$

where $S_I(t)$ and $S_Q(t)$ are the I- and Q-channel baseband signals. The waveform of each baseband signal in a T_{ChS} second channel symbol interval is chosen from a set of wavelets $\{W_i(t) \mid 0 \le i \le 15\}$, defined as follows:

---

[7] For FQPSK-B licensing and technology transfer information, contact Digcom Inc., c/o Dr. Kamilo Feher, 44685 Country Club Dr, El Macero, CA 95618; Tel :530-753-0738; FAX :530-753-1788; Internet: www.fehertechnologies.com.

[8] See 2.4 for bit/symbol terminology definitions used in this Green Book.

$$W_o(t) = -W_8(t) = A, \qquad\qquad -T_{ChS}/2 \leq t \leq T_{ChS}/2$$

$$W_1(t) = -W_9(t) = \begin{cases} A, & -T_{ChSs}/2 \leq t \leq 0 \\ 1 - (1-A)\cos^2(\pi t/T_{ChSs}), & 0 \leq t \leq T_{ChS}/2 \end{cases}$$

$$W_2(t) = -W_{10}(t) = \begin{cases} 1 - (1-A)\cos^2(\pi t/T_{ChS}), & -T_{ChS}/2 \leq t \leq 0 \\ A, & 0 \leq t \leq T_{ChS}/2 \end{cases}$$

$$W_3(t) = -W_{11}(t) = 1 - (1-A)\cos^2(\pi t/T_{ChS}), \qquad -T_{ChS}/2 \leq t \leq T_{ChS}/2$$

$$W_4(t) = -W_{12}(t) = A\sin(\pi t/T_{ChS}), \qquad -T_{ChSs}/2 \leq t \leq T_{ChS}/2$$

$$W_5(t) = -W_{13}(t) = \begin{cases} A\sin(\pi t/T_{ChS}), & -T_{ChS}/2 \leq t \leq 0 \\ \sin(\pi t/T_{ChS}), & 0 \leq t \leq T_{ChS}/2 \end{cases}$$

$$W_6(t) = -W_{14}(t) = \begin{cases} \sin(\pi t/T_{ChS}), & -T_{ChS}/2 \leq t \leq 0 \\ A\sin(\pi t/T_{ChS}), & 0 \leq t \leq T_{ChS}/2 \end{cases}$$

$$W_7(t) = -W_{15}(t) = \sin(\pi t/T_{ChS}), \qquad -T_{ChS}/2 \leq t \leq T_{ChS}/2$$

where $A = 1/\sqrt{2}$. The wavelets are numbered according to a trellis mapping rule that determines which wavelet is transmitted. Specifically, the mapping rule specifies that during the nth channel symbol interval, $(nT_{ChS}-T_{ChS}/2) \leq t \leq (nT_{ChS}+T_{ChS}/2)$, the baseband I- and Q-channel waveforms $S_I(t)$ and $S_Q(t)$ are assigned wavelets W_i and W_j respectively, where the indices i and j are given by

$$i = I_3 \times 2^3 + I_2 \times 2^2 + I_1 \times 2^1 + I_0 \times 2^0$$

$$j = Q_3 \times 2^3 + Q_2 \times 2^2 + Q_1 \times 2^1 + Q_0 \times 2^0$$

with

$$I_0 = D_{Q,n} \oplus D_{Q,n-1} \qquad Q_0 = D_{I,n+1} \oplus D_{I,n}$$

$$I_1 = D_{Q,n-1} \oplus D_{Q,n-2} \qquad Q_1 = D_{I,n} \oplus D_{I,n-1} = I_2$$

$$I_2 = D_{I,n} \oplus D_{I,n-1} \qquad Q_2 = D_{Q,n} \oplus D_{Q,n-1} = I_0$$

$$I_3 = D_{I,n} \qquad Q_3 = D_{Q,n}$$

where $D_{I,n}$ and $D_{Q,n} \in \{0,1\}$ are the nth I- and Q-channel inputs to the modulator, respectively.

The generation of FQPSK-B signal requires additional low-pass filtering of the baseband waveform, rendering the signal

$$S_{FQPSK-B}(t) = \sqrt{P}\tilde{S}_I(t)\sin(2\pi f_c t + \theta_c) + \sqrt{P}\tilde{S}_Q(t - T_{ChS}/2)\cos(2\pi f_c t + \theta_c)$$

where $\tilde{S}_I(t)=\int_{-\infty}^{t}S_I(\tau)h(t-\tau)d\tau$ and $\tilde{S}_Q(t)=\int_{-\infty}^{t}S_Q(\tau)h(t-\tau)d\tau$ are the filtered version of $S_I(t)$ and $S_Q(t)$, respectively, and $h(t)$ is the impulse response of the low-pass filter.

The functional block diagram as shown in figure 3-19 depicts the process of generating an FQPSK-B signal for RF transmission. It shows the baseband full-symbol cross-correlation mapping followed by the transmission filters and an offset-QPSK (OQPSK) modulator.
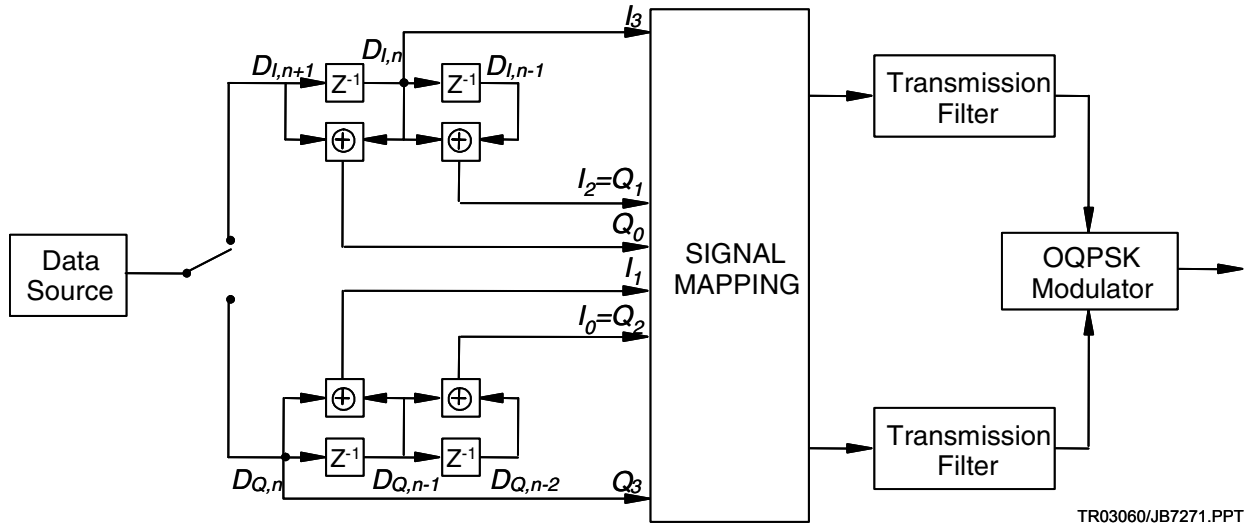
Figure 3-19: FQPSK-B Modulator

Figure 3-20 shows the phasor diagrams of both FQPSK and FQPSK-B baseband signals. Their corresponding eye diagrams are shown in figure 3-21. The spectral efficiency of the FQPSK-B signal is demonstrated in figure 3-22 where its simulated Power Spectral Density (PSD) at the output of a saturated SSPA is plotted against the spectral mask specified by SFCG Recommendation 21-2.
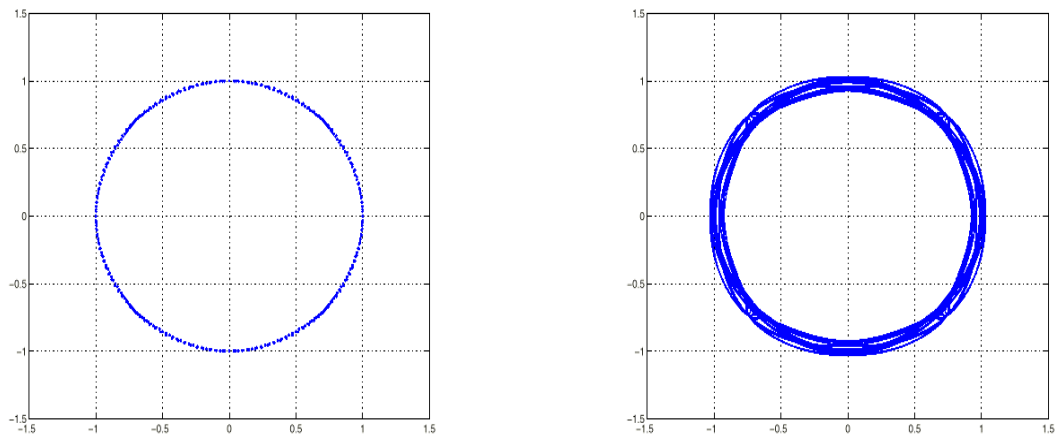
Figure 3-20: Phasor Diagrams for FQPSK (Left) and FQPSK-B (Right)
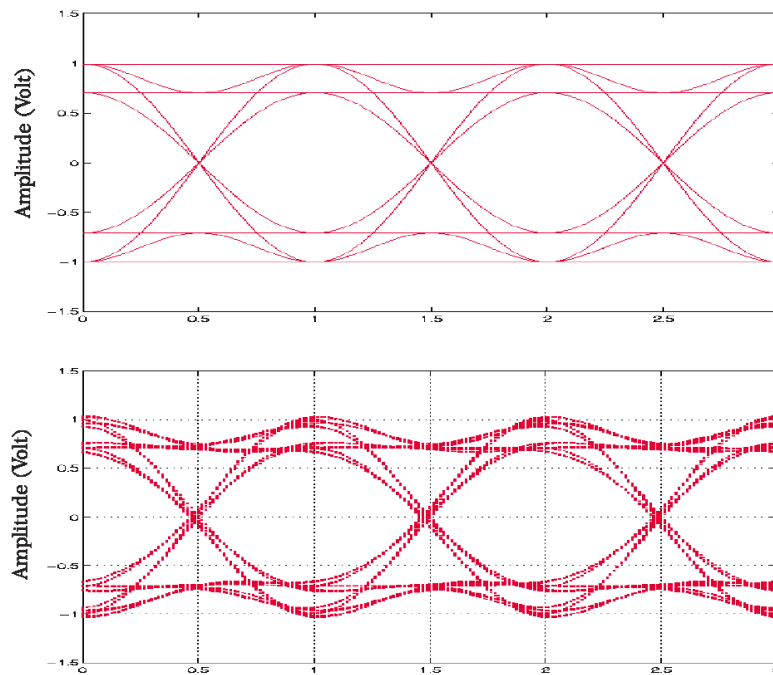
Figure 3-21: Transmitter Eye Diagrams for FQPSK (Top) and FQPSK-B (Bottom)
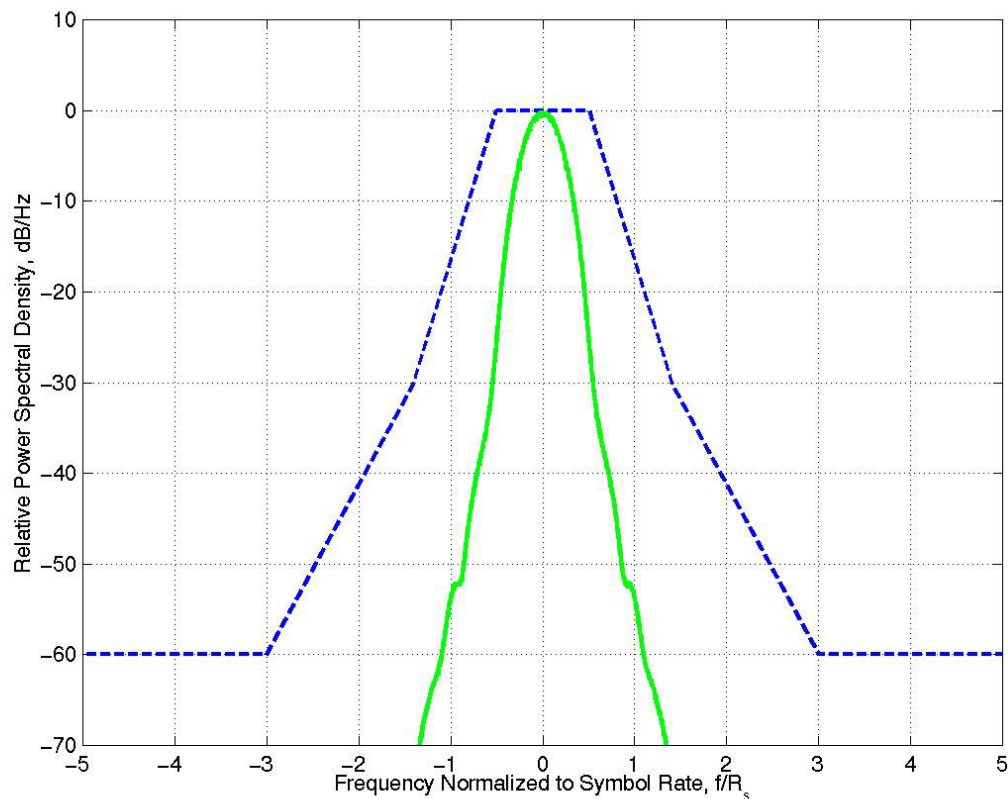
**Figure 3-22:   Simulated FQPSK-B Spectrum at Output of Saturated SSPA
(SFCG 21-2 Spectral Mask Shown in Dashed Line)**

3.3   FILTERED OFFSET-QPSK

3.3.1   INTRODUCTION

Offset-QPSK (OQPSK) is a proven modulation technique which is robust and easily implemented.   OQPSK receivers, typically employing integrate-and-dump type demodulators, are widely deployed by several international space agencies at ground stations operating downlinks in the S-band and X-band frequencies. With the use of proper filtering techniques, OQPSK modulation can meet the out-of-band emissions requirements of SFCG Recommendation 21-2 while still providing good BER performance with existing OQPSK receivers.

The majority of CCSDS studies performed on baseband filtered OQPSK modulation have used Butterworth and Square Root Raised Cosine (SRRC) filters which have been shown to have good performance; however, other filter types can also meet the high rate SFCG spectral mask requirements.

Two implementations of baseband filtered OQPSK modulation are described below: OQPSK with an I/Q modulator and OQPSK with a linear phase modulator, referred to as OQPSK/PM. Baseband filtered OQPSK with an I/Q modulator, filters the I and Q channel NRZ data signals and multiplies the filtered signals with in-phase and quadrature carrier signals. The baseband filtered OQPSK/PM signal is formed by mapping the I and Q NRZ data to a four-state phase signal, filtering the phase signal and then phase modulating a carrier with the filtered phase signal. One key point is that the filtering is done at baseband. This alleviates the additional cost, weight, and power loss (insertion loss plus filtering loss) associated with the use of RF filters, thereby allowing for a possible improvement in the overall power performance of the link.

As with all modulations, the actual BER performance of baseband filtered OQPSK is dependent on the receiver detection method used. An integrate and dump receiver with symbol by symbol detection is mathematically optimal for unfiltered OQPSK waveforms only. For filtered OQPSK, without the use of a complex maximum-likelihood receiver, the optimal receiver design would employ a receive filter precisely matched to the transmitter filter and an equalizer to remove intersymbol interference. For a modulation technique in which multiple alternative filter types have been recommended, this may seem to be a problem. Fortunately, in practice an integrate and dump filter receiver will provide good performance for most types of filtered OQPSK including those recommended.

Subsections 3.3.2.2 and 3.3.2.3 describe in detail the linear phase modulator and I/Q implementations of baseband filtered OQPSK. Subsection 3.3.2.4 presents various filtering options, including simulated power spectral density plots for three filter types.

3.3.2 MATHEMATICAL DEFINITION AND IMPLEMENTATION

3.3.2.1 General

Two modulator forms are commonly used for implementation of baseband filtered OQPSK (reference [8]). The linear phase modulator implementation is described in 3.3.2.2 and the I/Q modulator implementation is described in 3.3.2.3.[9]

3.3.2.2 Baseband Filtered OQPSK Linear Phase Modulator

OQPSK/PM uses a linear phase modulator to map a filtered phase signal onto the carrier. This configuration is shown in figure 3-23.

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[9] See 2.4 for bit/symbol terminology definitions used in this Green Book.
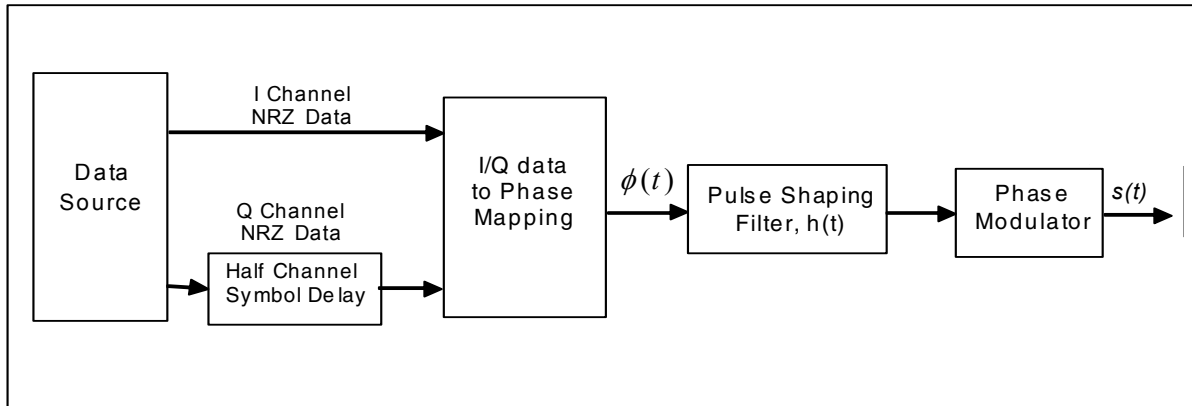
Figure 3-23: Filtered OQPSK with Linear Phase Modulator (OQPSK/PM)

The input to the modulator is the In-phase (I) and Quadrature (Q) NRZ data streams. The Q-channel data stream is delayed by ½ symbol to create offset QPSK. The I and Q data is mapped to a phase signal which then goes through a pulse shaping filter.[10] This is then used as an input to a linear phase modulator to produce the modulated output signal. The output of the modulator can be expressed as:

$$s(t) = \sqrt{2P}\cos(2\pi f_c t + \phi(t) * h(t))$$

where

P = carrier power

f_c = carrier frequency

$\phi(t)$ is the phase output from the I-Q to phase mapping

$h(t)$ is the impulse response of the pulse shaping filter

* denotes convolution

The phase modulator implementation of baseband filtered OQPSK produces a constant envelope signal, as can be seen in the phasor diagrams in figure 3-24. The constant envelope property of the signal is important because this will reduce the impact of the nonlinear AM/AM and AM/PM distortion of the saturated transmitter power amplifier.

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[10] Discrete spectral lines may be avoided if phase mapper uses the minimum phase rotation during transitions from one phase to another, e.g., +90° instead of -270°.

Butterworth Filter, BT_s = 0.5   SRRC Filter, α = 0.5
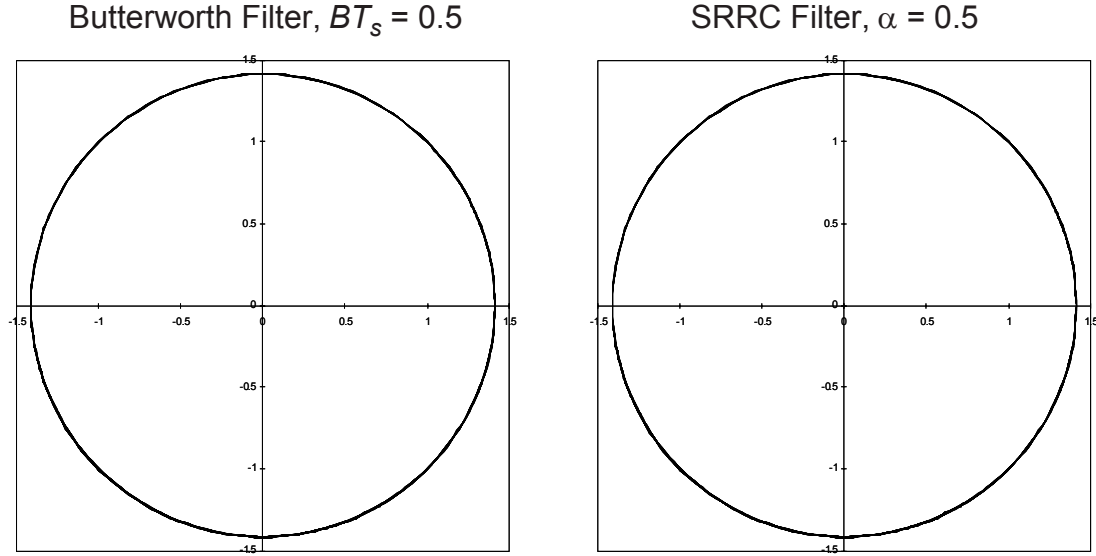
Figure 3-24: Baseband Filtered OQPSK/PM Implementation Phasor Diagrams

3.3.2.3   Baseband Filtered OQPSK I/Q Modulator

The second OQPSK implementation uses an I/Q modulator where the in-phase and quadrature carrier signals are amplitude modulated with a filtered NRZ data stream. This implementation is illustrated in figure 3-25.
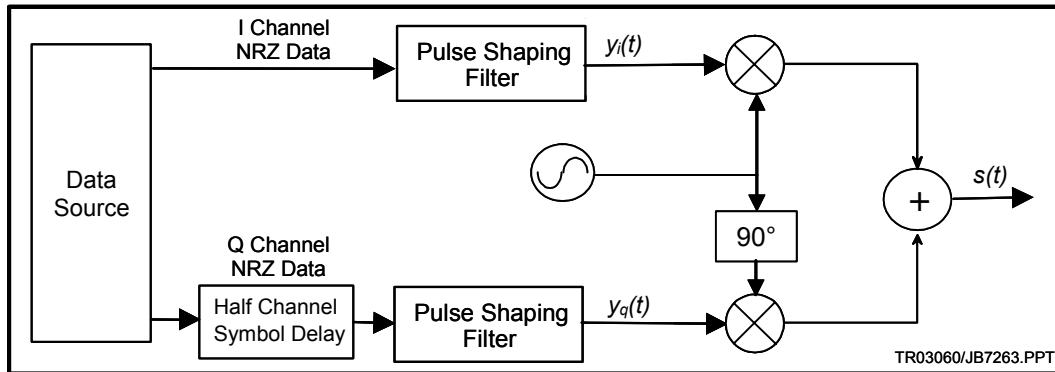
Figure 3-25: Baseband Filtered OQPSK with I/Q Modulator

The input to the modulator is the I and Q NRZ data streams. The Q-channel data stream is delayed by half a channel symbol to create Offset QPSK. The output of the modulator can be expressed as:

$$s(t) = y_i(t)\sin(2\pi f_c t + \varphi) + y_q(t)\cos(2\pi f_c t + \varphi)$$

where $y_i(t)$ and $y_q(t)$ are filtered NRZ data and φ is the initial oscillator phase.

In this implementation, the magnitude variations due to filtering are present in the output signal and thus the output signal does not have a constant envelope. This is evident in the phasor diagrams in figure 3-26. As a result, this implementation will cause spectral re-growth and Inter-Symbol Interference (ISI) when used with a non-linear power amplifier.

Butterworth Filter, BT_s = 0.5   SRRC Filter, α = 0.5
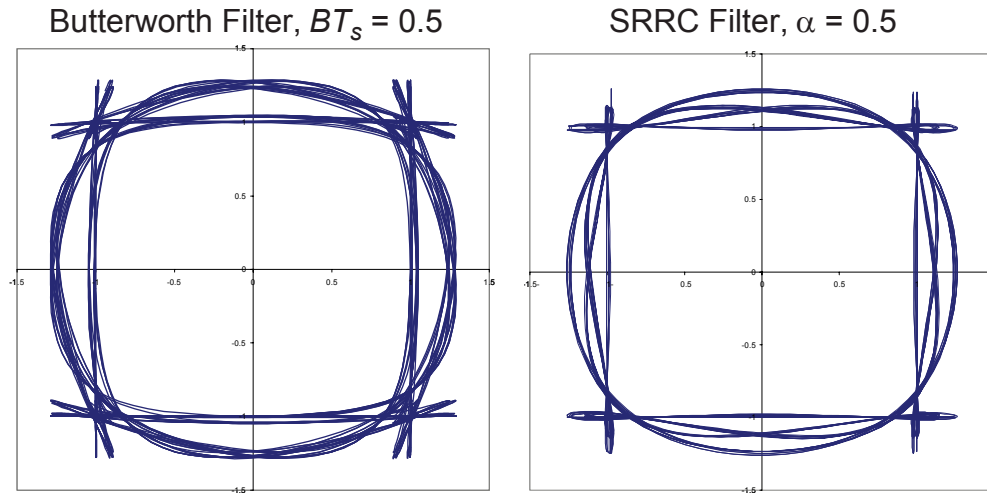
Figure 3-26: Baseband Filtered OQPSK I/Q Implementation Phasor Diagrams

In the absence of filtering, the implementations shown in figures 3-23 and 3-25 produce identical output signals.

3.3.2.4   Baseband Filtering Techniques

3.3.2.4.1   General

This subsection describes the characteristics of three example baseband filters that can be used with OQPSK modulation to meet the spectral containment requirements of the SFCG mask. The optimal filter type and parameters for any given system are a function of the receiver type and the particular distortion characteristics of that system. However, a number of defined filter types with standard parameters have been shown to provide generally good spectral containment and power efficiency performance and are thus specifically identified in the CCSDS recommendation. The two filters specifically mentioned are a 6th order Butterworth filter (BT_s = 0.5) and a Square Root Raised Cosine filter (α = 0.5). B is defined as the one-sided 3-dB filter bandwidth and T_s is the coded symbol period (or bit period if uncoded) at the input to the modulator.

Extensive simulation analyses have been performed on baseband filtered OQPSK using these two filter types. These analyses, which employed an integrate-and-dump type OQPSK demodulator and included the effects of hardware distortions typical of SRS missions, form the basis for the recommendation of this modulation technique. A limited number of additional analyses have also been performed using other filter types such as Bessel, Raised

Cosine, and Chebyshev filters. These simulations have shown that good power and spectral containment performance can be realized with alternative filter types as well.

This subsection provides the characteristics of the filter types recommended for baseband filtered OQPSK modulation. Subsections 3.3.2.4.2 and 3.3.2.4.3 address the aforementioned Butterworth and SRRC filters. Subsections 3.3.2.4.3.2 provides the characteristics of a Bessel filter which was not specifically recommended but is an example of other filter types which can meet the requirements of the SFCG mask and has good performance.

The Butterworth and Bessel filters are implemented as Infinite Impulse Response (IIR) filters, while the SRRC filter is implemented as a transversal Finite Impulse Response (FIR) filter. The implementation fidelity of these filters depends on the length of the filter, the sampling rate, and the amplitude quantization. The characteristics and design details of these filters is well documented in reference [9] and other textbooks.

3.3.2.4.2 Baseband Filtered OQPSK with a Butterworth Filter

This subsection describes the 6-pole $BT_5 = 0.5$ Butterworth lowpass filter which is one of the filter types specifically recommended by the CCSDS for baseband filtered OQPSK. The magnitude and phase response of the filter are plotted in figure 3-27. The simulated power spectral density for both the I/Q and PM implementations of baseband filtered OQPSK with the Butterworth filter are presented in figure 3-28. Note that the PSD is measured at the output of a saturated power amplifier to demonstrate the ability of the spacecraft using this modulation to meet the requirements of the SFCG emissions mask. The characteristics of the power amplifier are provided in annex B.
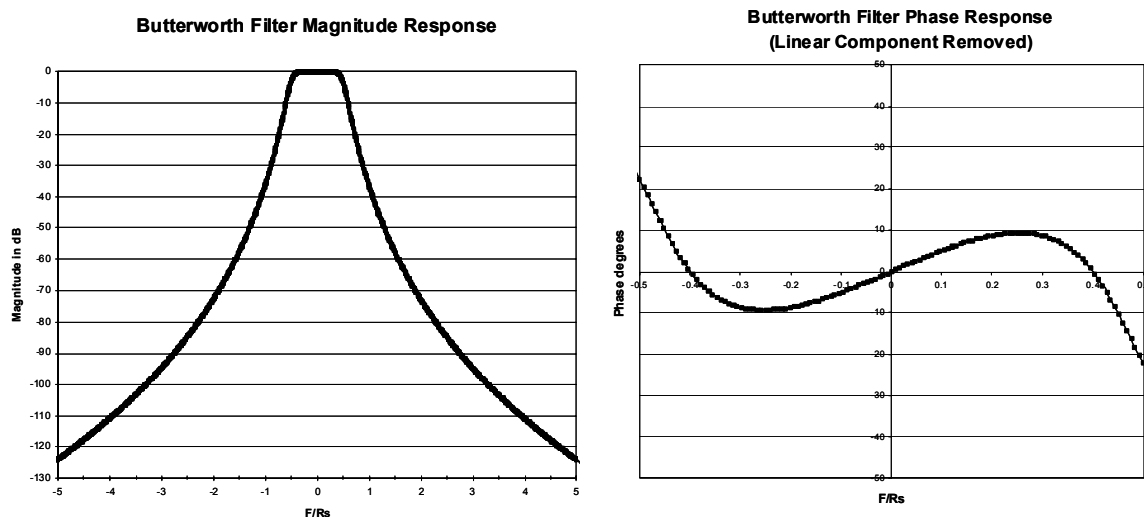
Figure 3-27: Butterworth Filter Magnitude and Phase Response
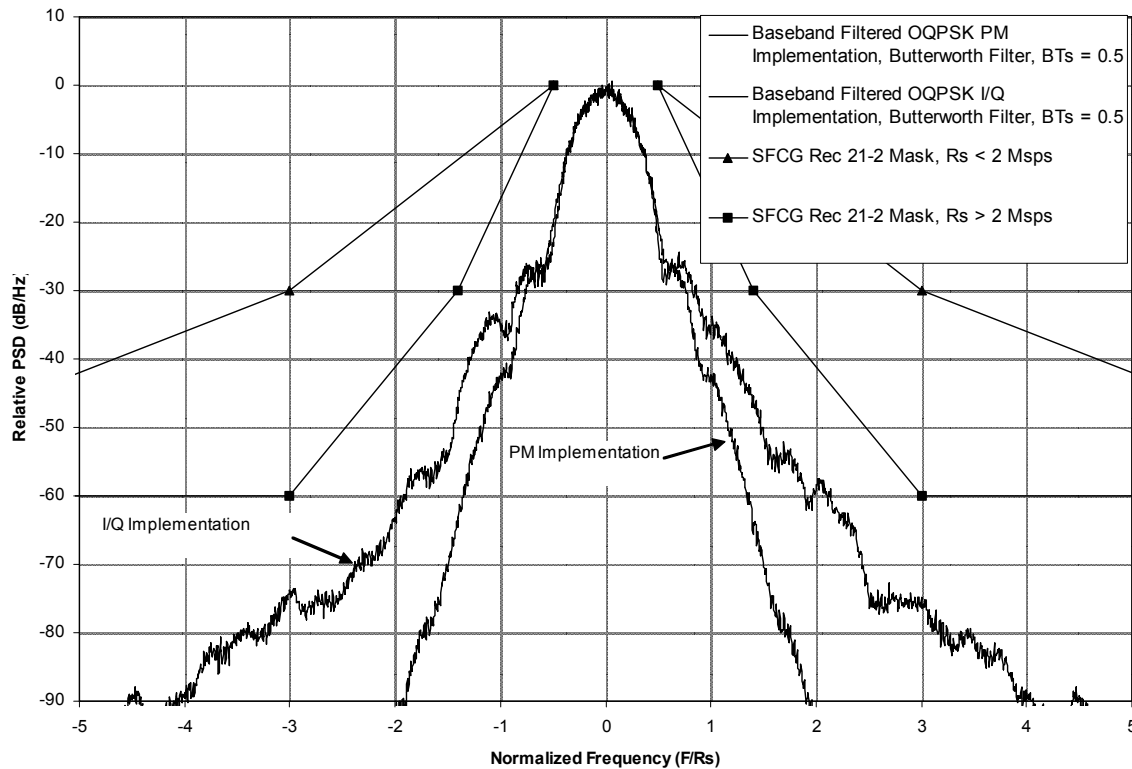
Figure 3-28: PSD for I/Q and PM Implementations of Baseband Filtered OQPSK with the Recommended Butterworth Filter

3.3.2.4.3 SRRC Filtered Offset-QPSK

3.3.2.4.3.1 General

Two variants of SRRC Offset-QPSK are described below. Square root raised cosine baseband filtered OQPSK can be formed by filtering rectangular NRZ pulses with an SRRC filter, similar to the Butterworth filtered OQPSK described in 3.3.2.4.2. A different form of SRRC OQPSK is created by using the impulse response of the SRRC filter as the signaling pulse shape. This type of SRRC OQPSK, described in 3.3.2.4.3.3, satisfies the Nyquist criterion for ISI-free signaling and is referred to as Nyquist pulse-shaped SRRC OQPSK in this Green Book to differentiate it from SRRC filtering of rectangular pulses.

3.3.2.4.3.2 Baseband Filtered OQPSK with a Square Root Raised Cosine Filter

This subsection describes the SRRC filter (α = 0.5) which is one of the filter types specifically recommended for baseband filtered OQPSK. The magnitude and phase response of the filter are plotted in figure 3-29. The simulated power spectral density for both the I/Q and PM implementations of baseband filtered OQPSK with the SRRC filter are presented in figure 3-30. Note that the PSD is measured at the output of a saturated power amplifier to demonstrate the ability of the spacecraft using this modulation to meet the requirements of

the SFCG emissions mask. The AM/AM and AM/PM characteristics of the power amplifier are provided in annex B.
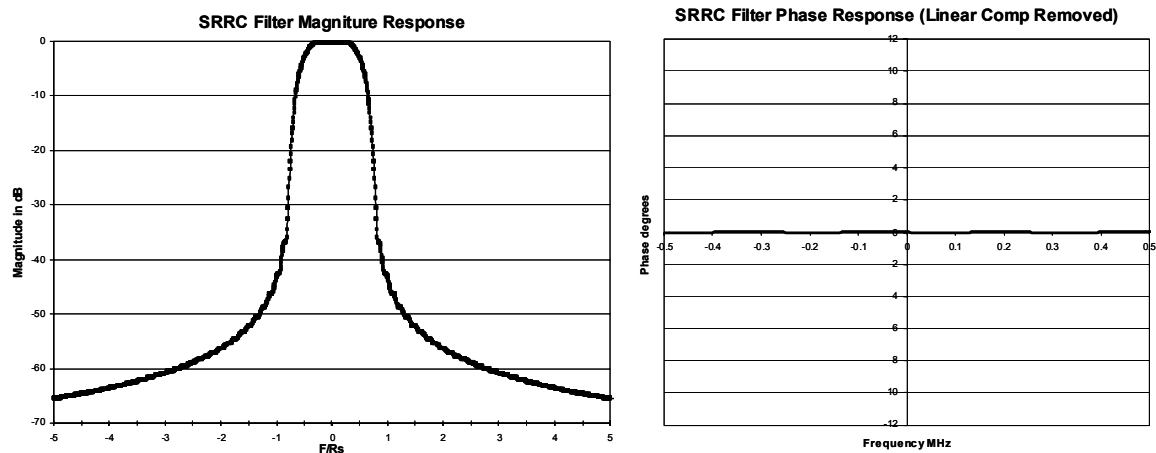

Figure 3-29: Magnitude and Phase Response of SRRC ($\alpha = 0.5$) Filter
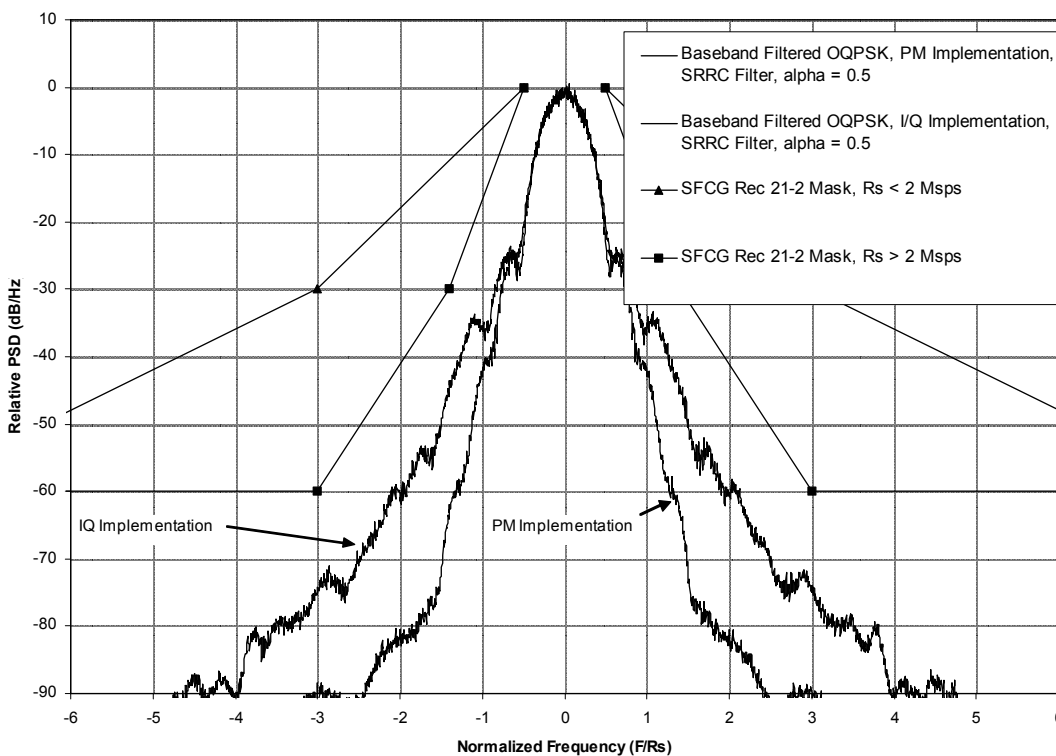
Figure 3-30: PSD for I/Q and PM Implementations of Baseband Filtered OQPSK with the Recommended SRRC Filter

3.3.2.4.3.3 Nyquist Pulse-Shaped SRRC OQPSK

A different form of SRRC OQPSK is created using the impulse response of the SRRC filter as the modulation pulse shape rather than SRRC filtering of NRZ pulses. With a matched filter receiver, this type of SRRC OQPSK fulfills the Nyquist criterion for ISI-free signaling. This means that in a linear channel with no timing errors, sampling points spaced T_{ChS} seconds apart at the output of the matched filter have no intersymbol interference. However, with distortion due to non-linear amplification, the Nyquist criterion is no longer satisfied and some ISI will occur.

Mathematically, Nyquist pulse-shaped SRRC OQPSK is defined as follows:

$$s(t) = d_I(t) * h(t)\sin(\omega_c t + \varphi_0) + d_Q\left(t - \frac{T_{Chs}}{2}\right) * h(t)\cos(\omega_c t + \varphi_0)$$

where * denotes convolution and h(t) is the SRRC filter impulse response defined by:

$$h(t) = \frac{4\alpha}{\pi\sqrt{T_{ChS}}} \frac{\cos\left(\frac{(1+\alpha)\pi t}{T_{ChS}}\right) + \frac{T_{ChS}}{4\alpha t}\sin\left(\frac{(1-\alpha)\pi t}{T_{ChS}}\right)}{1 - \left(4\alpha t / T_{ChS}\right)^2}$$

and $d_I(t)$ and $d_Q(t)$ are the I and Q impulse streams defined by:

$$d_I(t) = \sum_k I_k \delta(t - kT_{ChS})$$

$$d_Q(t) = \sum_k Q_k \delta(t - kT_{ChS})$$

where $\delta(t)$ is the Dirac delta function, and I_k and Q_k are the in-phase and quadrature-phase data symbol streams. The roll-off factor α determines the frequency from the filter passband to the stopband is very abrupt while the filter impulse response is spread out in time. For large values of α, the filter roll-off is more gradual while conversely the impulse response is more concentrated in time. The case of $\alpha=0$ corresponds to an instantaneous transition from the filter passband to the stopband at the cutoff frequency, often called a 'brickwall' filter.

Figure 3-31 shows a block diagram of a Nyquist pulse-shaped SRRC OQPSK modulator based on the theoretical equations above. With digital implementation, the SRRC filter is typically windowed since the impulse response is theoretically infinite in time. The FIR coefficients of the windowed SRRC filter can then be stored in ROM lookup tables.

Transmitter hardware distortions including amplifier nonlinearities and windowing create intersymbol interference and cause spectral regrowth for the Nyquist SRRC OQPSK signal. For smaller values of α, the effects of signal distortion will be more severe. Figure 3-32 shows the simulated Nyquist SRRC OQPSK ($\alpha=0.5$) spectrum at the output of the saturated (defined as 0 dB output back-off) SSPA whose characteristics are given in annex B.
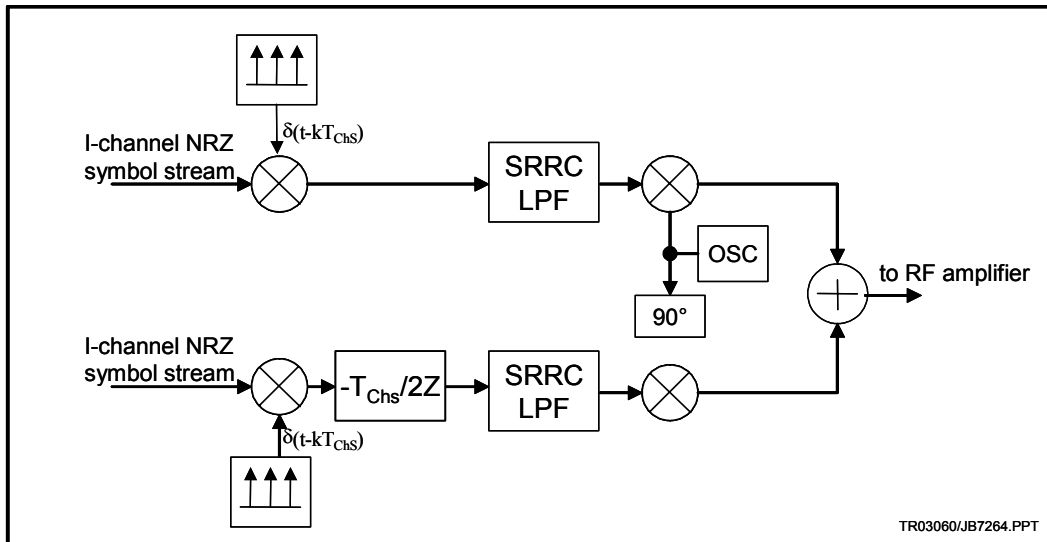
Figure 3-31: Nyquist Pulse-Shaped SRRC OQPSK Modulator Based on Theoretical Equation
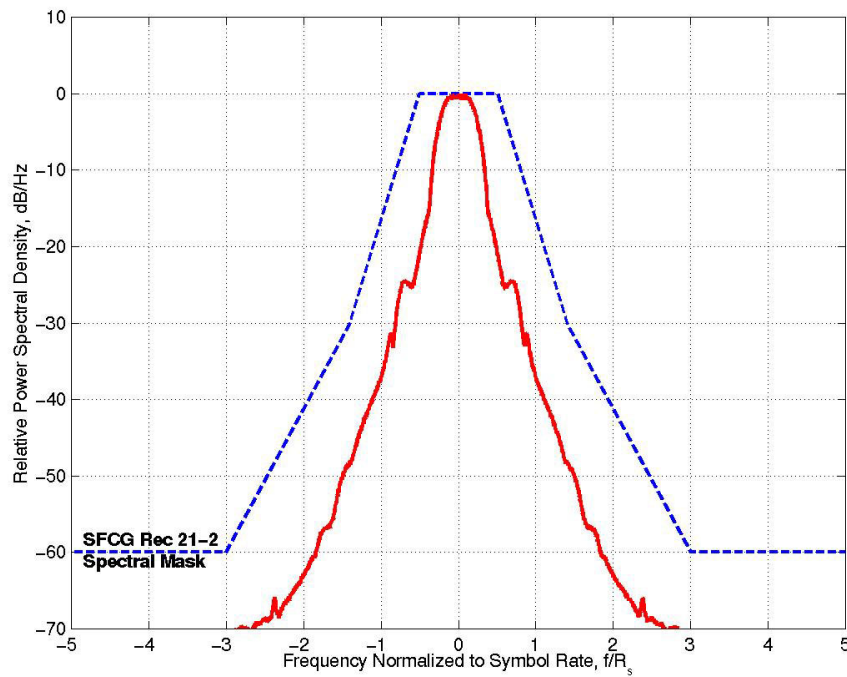
Figure 3-32: Simulated Spectrum of Nyquist Pulse-Shaped SRRC (α=0.5) OQPSK at Output of Saturated SSPA

3.3.2.4.4 Baseband Filtered OQPSK with Other Filter Types

3.3.2.4.4.1 General

As indicated above, Butterworth and/or SRRC filters are not necessarily optimum for use in baseband filtered OQPSK systems. While it would be impossible to document the performance of all possible filters, the performance of Bessel-filtered OQPSK is addressed in the following subsection as an example.

3.3.2.4.4.2 Baseband Filtered OQPSK with Bessel Filter

This subsection describes a 6th order $BT_s = 0.5$ Bessel filter. The magnitude and phase response of the filter are plotted in figure 3-33. The simulated power spectral density for both the I/Q and PM implementations of baseband filtered OQPSK with the Bessel filter are presented in figure 3-34. Note that the PSD is measured at the output of a saturated power amplifier to demonstrate the ability of the spacecraft using this modulation to meet the requirements of the SFCG emissions mask. The characteristics of the power amplifier are provided in annex B.
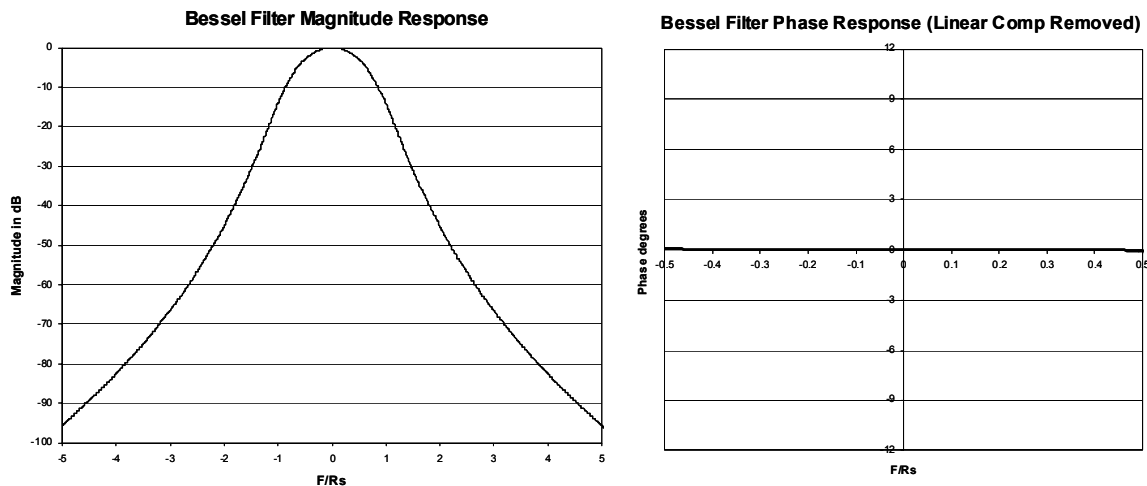

Figure 3-33: Magnitude and Phase Response of 6th Order $BT_s = 0.5$ Bessel Filter
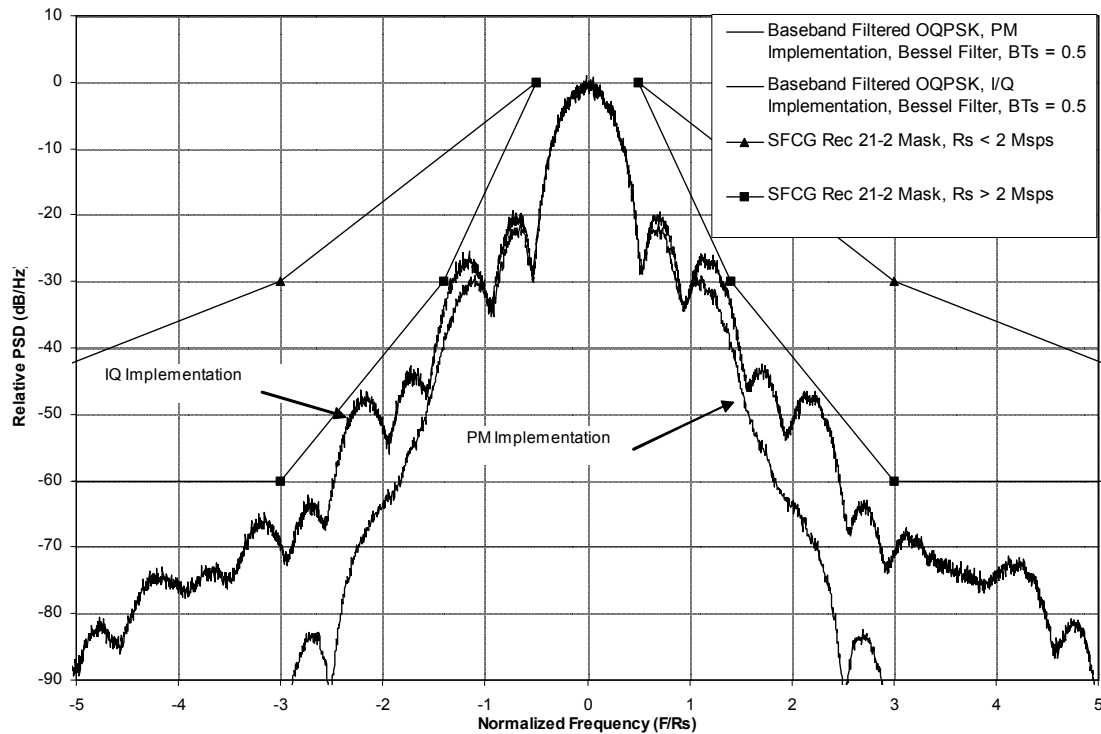
Figure 3-34: **PSD for I/Q and PM Implementations of Baseband Filtered OQPSK with a 6th Order $BT_s = 0.5$ Bessel Filter**

3.4 SHAPED OFFSET-QPSK

3.4.1 INTRODUCTION

This chapter describes two versions of Shaped Offset QPSK (SOQPSK) modulation, referred to as SOQPSK-A and SOQPSK-B, which are recommended for use with high data rate, (> 2 Msps) space-to-Earth, space research, Category A transmissions. For each of these techniques, a mathematical definition and signal structure is provided.

Shaped Offset QPSK is a continuous phase constant envelope modulation technique. The original version of SOQPSK was developed in the 1980s for use in U.S. Military UHF satellite communications links and is documented in MIL-STD-188-181 and MIL-STD-188-182. The two variants of SOQPSK discussed here and recommended in Recommendation 401(2.4.17A), SOQPSK-A and SOQPSK-B, were proposed by Terrance Hill of Nova Engineering (reference [10]). These modulations meet the spectral efficiency requirements of SFCG Recommendation 21-2 and provide acceptable BER performance for use in the Space Research Category A bands.

3.4.2 SOQPSK MATHEMATICAL DEFINITION

A QPSK-modulated signal can be represented as:

$$s(t) = \sqrt{2P} \cos(2\pi f_c t + \phi(t, \alpha(t)) + \phi_0)$$

where

P = carrier power
f_c = carrier frequency
ϕ_0 = arbitrary initial phase offset
$\phi(t, \alpha(t))$ = data sequence-driven input to the phase modulator

The input to the phase modulator, $\phi(t, \alpha(t))$, is defined as the integral of a sequence of frequency pulses

$$\phi(t, \alpha(t)) = 2\pi h \int_{-\infty}^{t} \sum_{i=-\infty}^{+\infty} \alpha_i g(\tau - iT_{ChS}/2) d\tau \qquad -\infty < t < +\infty$$

where

h = modulation index
$g(t)$ = frequency pulse
T_{ChS} = channel symbol period[11]

For standard OQPSK, $g(t)$ is a unit area delta function and $h = 0.25$. The string of delta functions integrates to sequence of discrete $\pi/2$ phase shifts at the symbol transition instants. The α_is are chosen from the set {-1,0,1} to achieve the appropriate direction for the phase transition. For MIL-STD SOQPSK, $g(t)$ is a step function and the phase integrates to a constant slope line from one phase point to another during a single bit period. This is similar to MSK; however, unlike MSK the MIL-STD SOQPSK phase can remain constant in the same phase state in successive bit periods when there is no phase transition.

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[11] See 2.4 for bit/symbol terminology definitions used in this Green Book.

The SOQPSK-A and B versions modify the frequency pulse g(t) to incorporate a raised cosine filter shape. The mathematical definition of the SOQPSK-A and SOQPSK-B frequency pulses are given by *g(t) = n(t)w(t)* where

$$n(t) = \frac{A\cos(\pi\rho Bt/T_{ChS})}{1-4(\rho Bt/T_{ChS})^2} \cdot \frac{\sin(\pi Bt/T_{ChS})}{\pi Bt/T_{ChS}}$$

$$w(t) = \begin{cases} 1, & for \quad |t/T_{ChS}| < T_1 \\ \frac{1}{2} + \frac{1}{2}\cos\frac{\pi(|t/T_{ChS}|-T_1)}{T_2}, & for \quad T_1 < |t/T_{ChS}| < T_1+T_2 \\ 0, & for \quad |t/T_{ChS}| > T_1+T_2 \end{cases}$$

The specific parameters defining the SOQPSK-A and B variants are listed in table 3-1. The parameter A is normalized such that the frequency pulse *g(t)* integrates to a value of π/2. The resulting frequency pulses are depicted in figure 3-35. Subsequent studies have identified different versions of SOQPSK that give comparable or better performance (reference [11]).

Table 3-1: SOQPSK-A and B Parameters

Parameter	SOQPSK-A	SOQPSK-B
ρ	1.0	0.5
B	1.35	1.45
T_1	1.4	2.8
T_2	0.6	1.2

SOQPSK Frequency Pulse

g(t) (vertical axis)

Normalized Time (t/T$_{ChS}$)
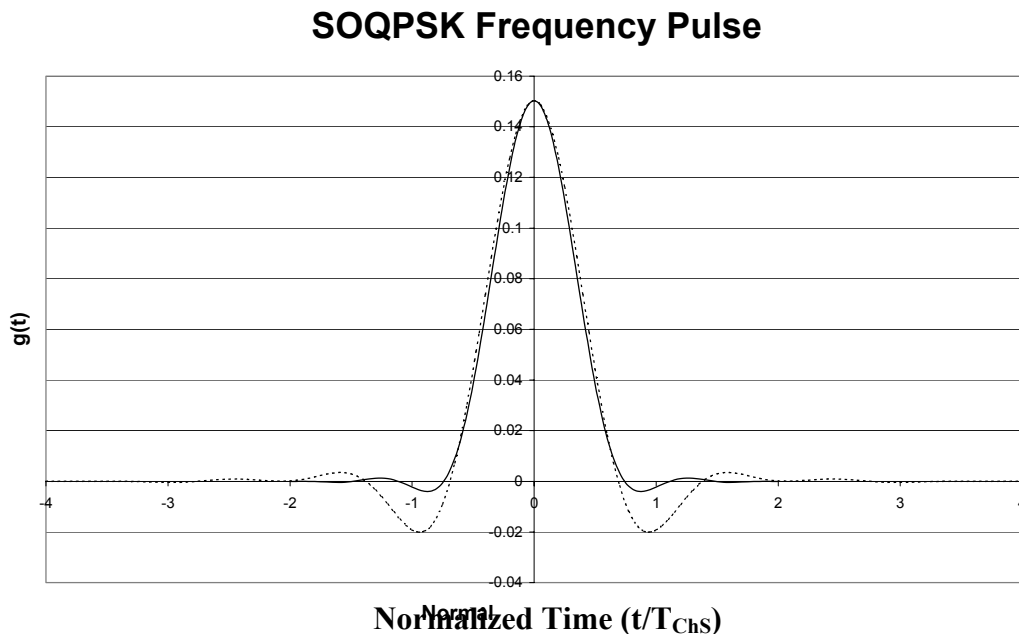
Figure 3-35: SOQPSK-A and B Frequency Pulse Waveforms

3.4.3   SOQPSK IMPLEMENTATION AND SIGNAL STRUCTURE

A modulator structure for implementing these SOQPSK techniques is provided in figure 3-36. It consists of a mapper to generate the phase transition signal $\alpha(t)$ from the input data, a frequency pulse generator to provide the $g(t)$ pulses, an integrator, and a phase modulator. The phase transition mapping is defined by table 3-2.

As indicated above, the phase transition signal $\alpha(t)$ takes on a value of ±1 or 0 during each input coded symbol period based upon the direction of the phase transition. The direction of this transition for SOQPSK, as with conventional OQPSK, is a function of the previous modulator state and the current input data. This mapping can be implemented with a simple lookup table which defines the appropriate value for $\alpha(t)$ based on the present and past values on the I and Q channels.

The left side of table 3-2 lists the various combinations of present and past values on the I and Q channels which result in $\alpha(t) = +1$. The right side of table 3-2 lists combinations which result in $\alpha(t) = -1$. All other combinations result in $\alpha(t) = 0$.
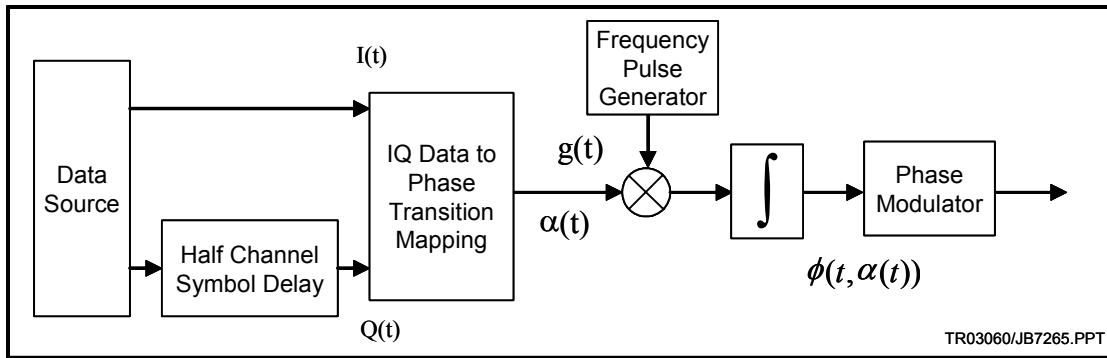
Figure 3-36: SOQPSK Modulator Implementation

The modulator output can be characterized in the time domain using the SOQPSK-A and SOQPSK-B eye diagrams depicted in figures 3-37 and 3-38. The associated simulated power spectral densities for SOQPSK-A and SOQPSK-B are depicted in figure 3-39 along with the SFCG Recommendation 21-2 high rate and low rate spectral masks.

Table 3-2: I/Q Data to Phase Transition Mapping

I(t)	Q(t)	I(t-T_s)	Q(t-T_s)	I(t-2T_s)	Q(t-2T_s)	α(t)	I(t)	Q(t)	I(t-T_s)	Q(t-T_s)	I(t-2T_s)	Q(t-2T_s)	α(t)
1	0	0	0	0	1	+ 1	1	0	1	1	0	1	- 1
0	0	0	1	0	0	+ 1	0	1	0	0	0	1	- 1
1	1	1	0	0	0	+ 1	1	1	0	1	0	0	- 1
0	1	1	1	1	0	+ 1	0	0	1	0	0	0	- 1
1	0	0	0	0	0	+ 1	0	1	0	0	1	0	- 1
0	0	0	1	0	1	+ 1	0	0	1	0	1	1	- 1
0	0	0	1	1	1	+ 1	1	0	1	1	1	1	- 1
1	0	0	0	1	0	+ 1	0	0	0	1	0	0	- 1
1	1	1	0	1	0	+ 1	0	1	0	0	0	0	- 1
0	1	1	1	1	1	+ 1	1	1	0	1	0	1	- 1
All Others						0	All Others						0
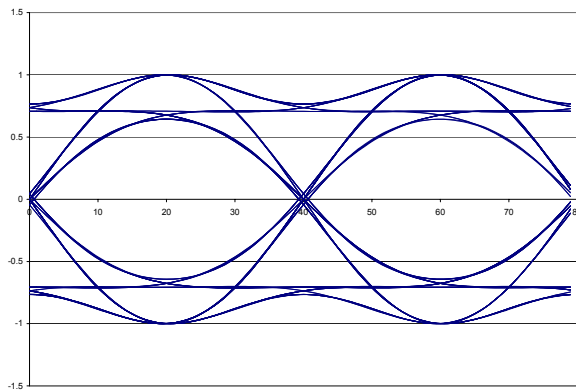
Figure 3-37: SOQPSK-A Eye Diagram
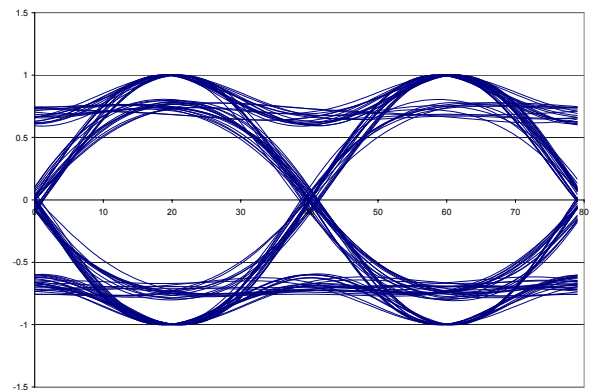
Figure 3-38: SOQPSK-B Eye Diagram
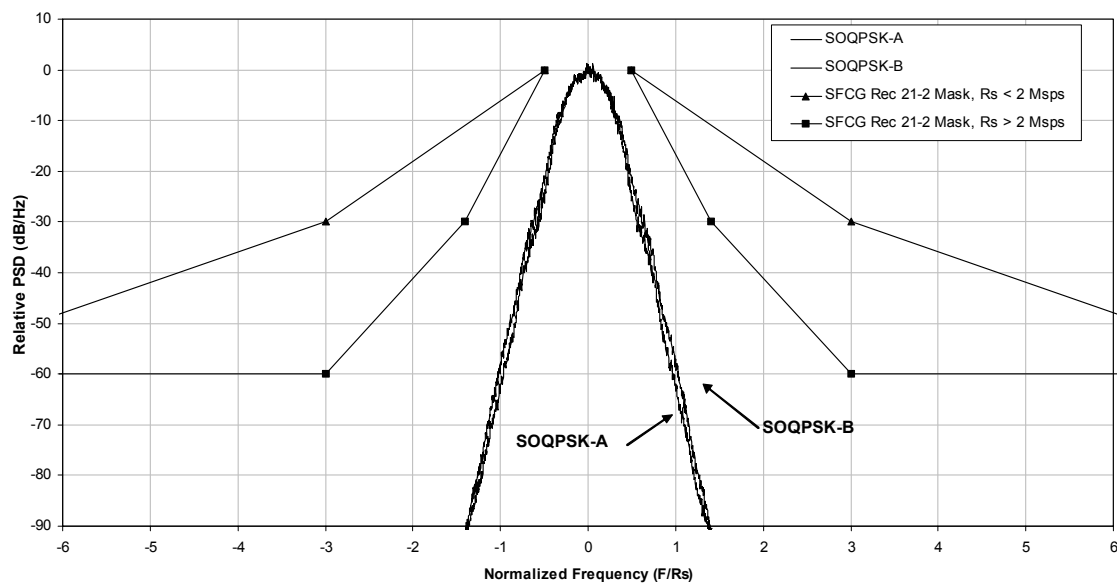
Figure 3-39: SOQPSK-A and SOQPSK-B Power Spectral Densities

3.5   TRELLIS-CODED OFFSET-QPSK

3.5.1   INTRODUCTION

Trellis-coded Offset-QPSK (T-OQPSK) (reference [12]) is a pulse-shaped trellis-coded modulation. It is one of CCSDS recommended modulations for Category B mission space-to-Earth links. T-OQPSK has a narrow spectrum, low out-of-band power, and low bit-error degradation with an optimal Viterbi receiver. With the signal formulation described in 3.5.2,

the T-OQPSK modulator implementation is simplified since there are only two distinct full-response pulse shapes which are used. T-OQPSK is an alternative implementation of a modulation type known as Staggered Quadrature Overlapped Raised Cosine Modulation (SQORC) (reference [15]).

3.5.2 SIGNAL MODEL

In this subsection, T-OQPSK is implemented using an I/Q modulator. As such, the T-OQPSK signal is mathematically expressed as:

$$s(t) = c_I(t)\sin\left(2\pi f_c t + \varphi_o\right) + c_Q\left(t - \frac{T_{ChS}}{2}\right)\cos\left(2\pi f_c t + \varphi_o\right)$$

where $c_i(t)$ and $c_j(t)$ are the I and Q pulse shapes, respectively, with the indices $i,j \in \{0,1,2,3\}$ computed as shown in 3.5.3. The waveforms are defined as follows:

$$c_0(t) = 1, \qquad\qquad -T_{ChS}/2 \leq t \leq T_{ChS}/2$$
$$c_1(t) = \sin\left(\pi t/T_{ChS}\right), \quad -T_{ChS}/2 \leq t \leq T_{ChS}/2$$
$$c_2(t) = -c_0(t), \qquad\qquad -T_{ChS}/2 \leq t \leq T_{ChS}/2$$
$$c_3(t) = -c_1(t), \qquad\qquad -T_{ChS}/2 \leq t \leq T_{ChS}/2$$

where T_{ChS} is the channel symbol period.[12] The selection of which waveform to transmit during each channel symbol period is determined by the output of the 2-state trellis encoders on the in-phase and quadrature phase arms of the modulator as shown in figure 3-40. It can be shown mathematically that T-OQPSK has a maximum of 3 dB in envelope fluctuation.

3.5.3 T-OQPSK MODULATOR

Figure 3-40 shows the block diagram of the T-OQPSK modulator. The input data is first split into In-phase (I) and Quadrature phase (Q) streams. Each stream is encoded with the 2-state encoder shown in the figure and mapped to one of four waveforms defined in the previous subsection.

Following the waveform mapping, the quadrature phase waveforms are delayed by half a channel symbol period to form an offset modulation, and then modulated onto quadrature carriers.

The oscilloscope printout of the T-OQPSK in-phase and quadrature phase baseband waveform eye diagrams is shown in figure 3-41. The T-OQPSK waveforms were generated using an FPGA. Figure 3-42 shows the simulated spectrum of T-OQPSK at the output of a saturated power amplifier whose AM/AM and AM/PM characteristics are given in annex B. The SFCG 21-2 high rate (> 2 Msps) spectral emissions mask is also presented to

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[12] See 2.4 for bit/symbol terminology definitions used in this Green Book.

demonstrate the ability of a spacecraft using this modulation to meet the requirements of the SFCG mask.
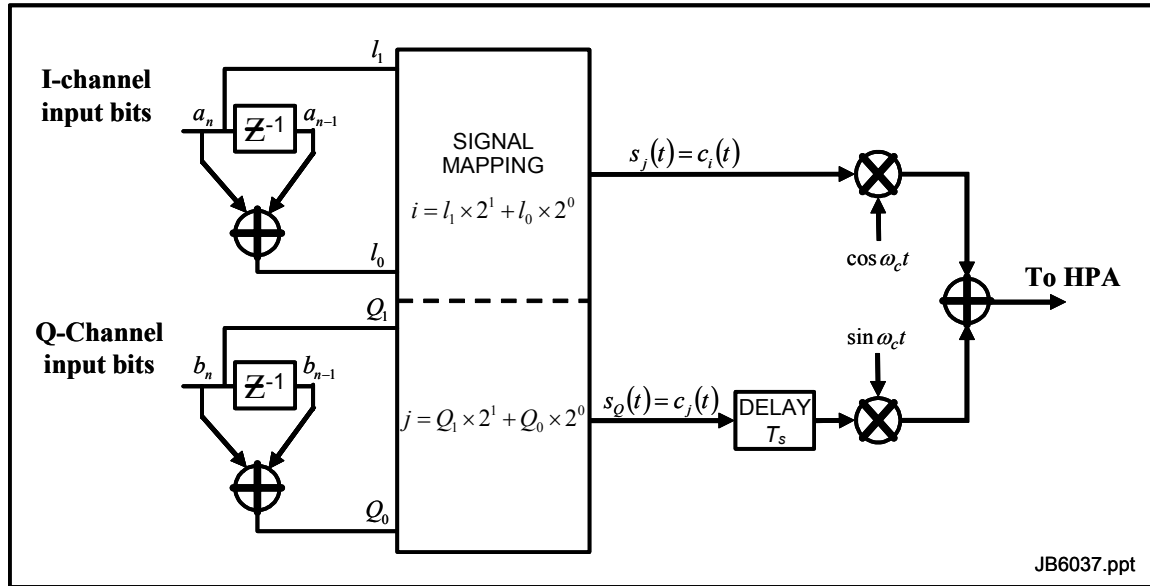
Figure 3-40: T-OQPSK Modulator
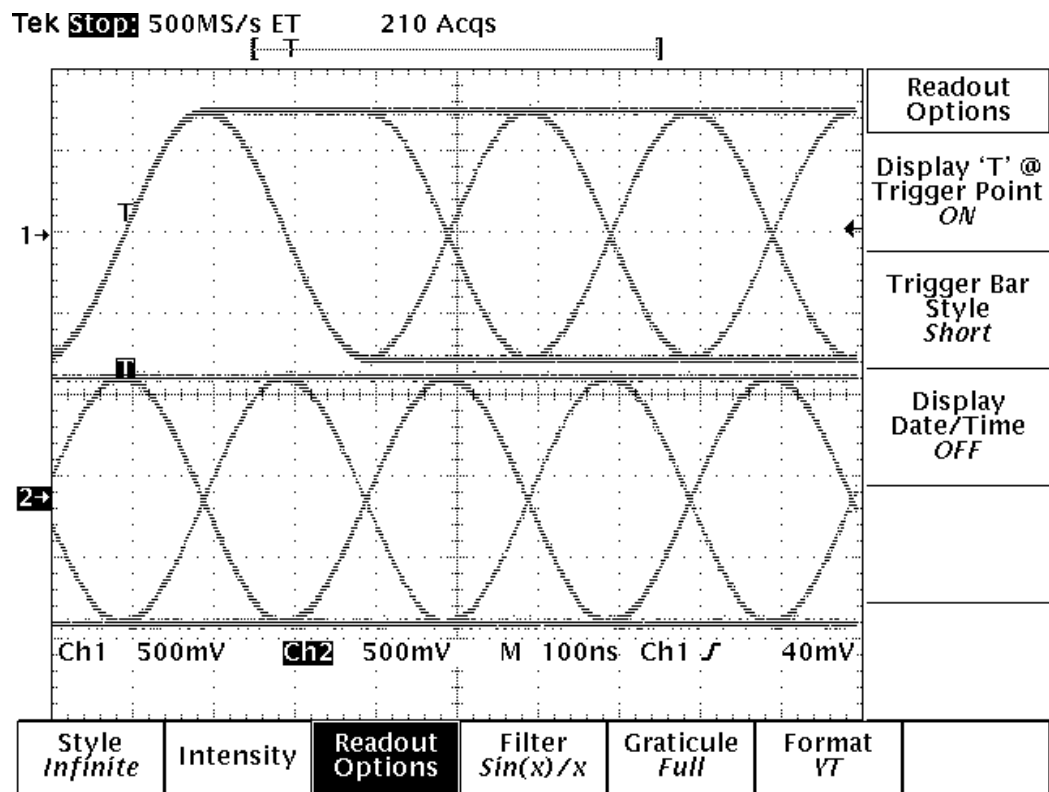
Figure 3-41: Eye Diagram of T-OQPSK Baseband Waveforms
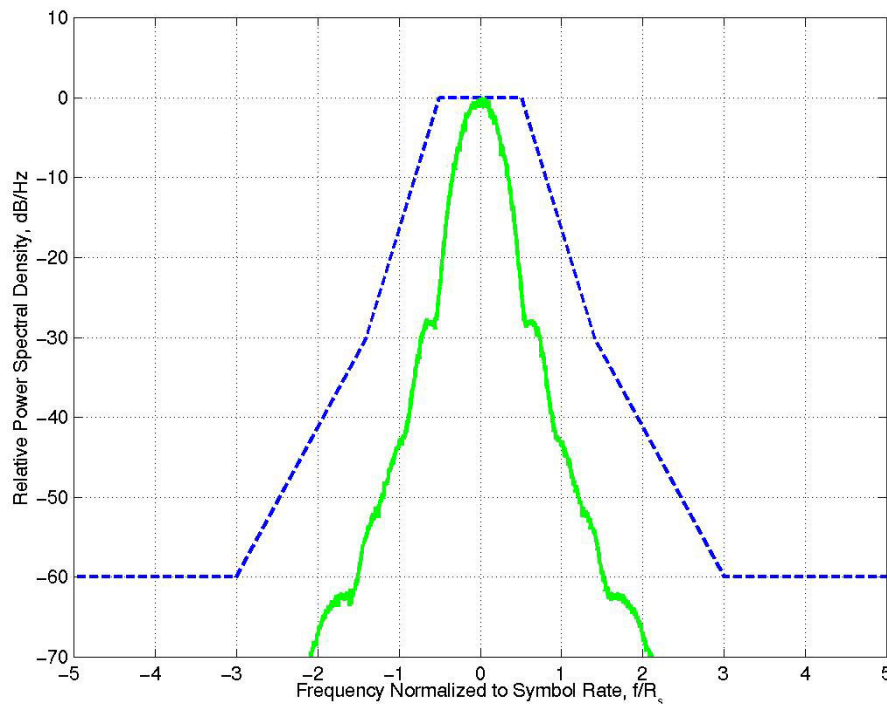
Figure 3-42:   Simulated T-OQPSK Spectrum at Output of Saturated SSPA (SFCG 21-2 High Rate Mask Shown in Dashed Line)

3.6   4D 8PSK TRELLIS-CODED MODULATION

3.6.1   GENERAL

This subsection specifies the coding and mapping techniques integral to a highly efficient multidimensional trellis coded modulation for use in bandwidth-constrained communications between remote satellites and Earth stations.   Efficiency in this context refers both to bandwidth efficiency (in bits/s/Hz and bits/channel-symbol) for a given information quantity, and power efficiency.   The basic principle and requirements for implementation of multidimensional 8PSK TCM is given in the following subsections.

3.6.2   INTRODUCTION

The L-dimensional MPSK-TCM (LD-MPSK-TCM) belongs to a family of modulations first introduced by G. Ungerboeck (reference [13]) and improved by S. Pietrobon (reference [14]) with the introduction of the multidimensional techniques.

The MPSK-TCM are based on MPSK modulations with the use of convolutional coding to introduce 'authorized sequences' between signal points linked by the trellis of the code. Note that single constellation MPSK modulations may also be referred to as 'bidimensional' in reference to the representation of the MPSK constellation points in a signal space defined

by orthogonal I and Q vectors. In any case, the application of this procedure to several parallel constellations of the same size is referred to as L-dimensional TCM, denoted LD-MPSK-TCM (with L > 1 and M ≥ 8). The trellis is constructed to maximize the minimum Euclidian distance between different paths originating and merging to the same state. The construction of the optimum trellis code and partitioning for the M points in the constellation is based on heuristic rules proposed in references [13] and [14].

With 4D-8PSK-TCM, the combination of convolutional coding, multiphase modulation and multidimensional techniques offers a substantial power gain together with bandwidth conservation or reduction, in comparison to their separate utilization as it is done frequently with binary or quaternary modulations (i.e., sequential implementation of convolutional coding). The result is an improvement of the performances in terms of BER versus signal to noise ratio for the same or better bandwidth efficiency, compared with the uncoded OQPSK or QPSK modulations.

Example: Assuming the bit rate R_b of input data equal to 100 Mbps, the 4D-8PSK-TCM channel symbol rate is 50 Msps for 2 bits/channel-symbol or 40 Msps for 2.5 bits/channel-symbol.

3.6.3 4D-8PSK-TCM CODER

3.6.3.1 General

The 4D-8PSK trellis-coded modulator consists of a serial to parallel converter, a differential coder, a trellis encoder (convolutional coder), a constellation mapper and an 8PSK modulator (see figure 3-43). Note that in this figure, wi (with index i = 1, … , m) represents the uncoded bits and xj (with index j = 0, … , m) represents the coded bits. The trellis encoder is based on a 64 state systematic convolutional coder and can be considered as the inner code if an outer block code is introduced. Carrier phase ambiguity is resolved by the use of a differential coder located prior to the trellis encoder. Spectral efficiencies of 2, 2.25, 2.5, and 2.75 bits/channel-symbol are achieved with four possible architectures of the constellation mapper. The output switch addresses successively one of the four symbols ($Z^{(0)} - Z^{(3)}$) from the constellation mapper to the 8PSK modulator.

The present standard is based on the use of a 4D-8PSK-TCM characterized by the following parameters:

- size of the constellation: M=8 phase states (8PSK);
- number of signal set constituents: L=4 (shown as $Z^{(0)}$ … $Z^{(3)}$ in figure 3-43);
- number of states for the trellis encoder: 64;
- rate of the convolutional coder used for the construction of the trellis: R=3/4;
- rate of the modulation: R_m=m/(m+1) selectable to 8/9, 9/10, 10/11, or 11/12;
- efficiency of the modulation:
  - Reff=2 bits per channel-symbol (for Rm=8/9);
  - Reff=2.25 bits per channel-symbol (for Rm=9/10);
  - Reff=2.5 bits per channel-symbol (for Rm=10/11);

- Reff=2.75 bits per channel-symbol (for Rm=11/12).
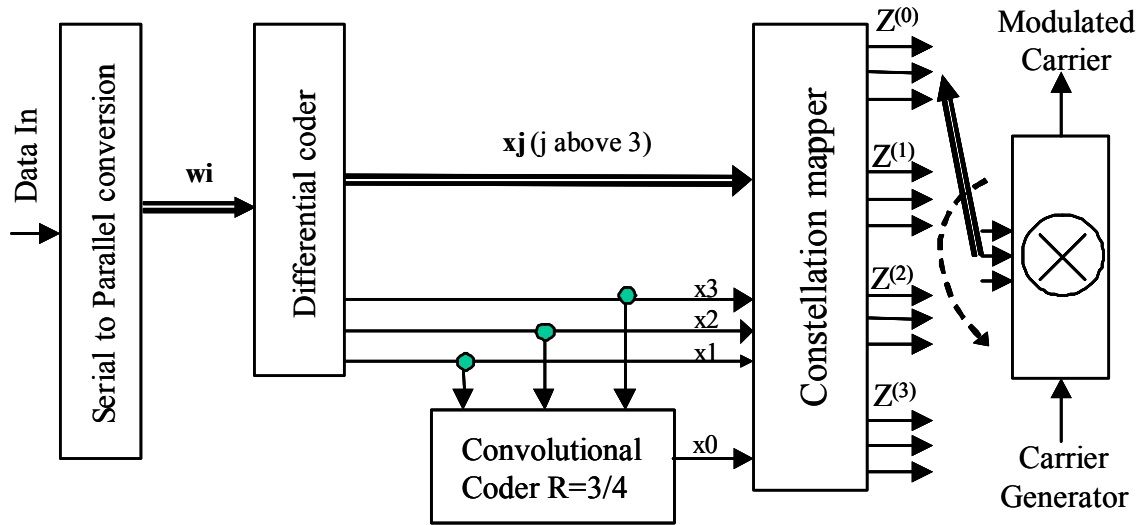
Figure 3-43: Structure of the 4D 8PSK-TCM Coder/Mapper

3.6.3.2   Differential Coder

The differential coder depicted in figure 3-44 is used to eliminate phase ambiguity on carrier synchronization for each modulation efficiency. Table 3-3 gives the bit reference at input and output of the differential coder in each case.

Table 3-3: Bit Mapping for Differential Coder

Efficiencies in bits /channel-symbol							
2		2.25		2.5		2.75	
bit IN	bit OUT	bit IN	bit OUT	bit IN	bit OUT	bit IN	bit OUT
w1	x1	w2	x2	w3	x3	w4	x4
w5	x5	w6	x6	w7	x7	w8	x8
w8	x8	w9	x9	w10	x10	w11	x11

An example of differential encoder connections is given in figure 3-44 for the 2 bits/channel-symbol case. The structure of the modulo 8 adder is also shown; it is applicable to both the coder mapper and differential coder.

b_8 b_5 b_1 IN
w_8 w_5 w_1

b_2 b_1 b_0 a_2 a_1 a_0

c_2 c_1 c_0

D

x_8 x_5 x_1
OUT

R03060.JB7253.PPT

$c_0 = a_0 \oplus b_0$ with carry r_0

$c_1 = a_1 \oplus b_1 \oplus r_0$ with carry r_1

$c_2 = a_2 \oplus b_2 \oplus r_1$

$r_0 = a_0 . b_0$

$r_1 = (a_1 . b_1) + (a_1 . r_0) + (b_1 . r_0)$

where . corresponds to a logical AND, and + to a logical OR
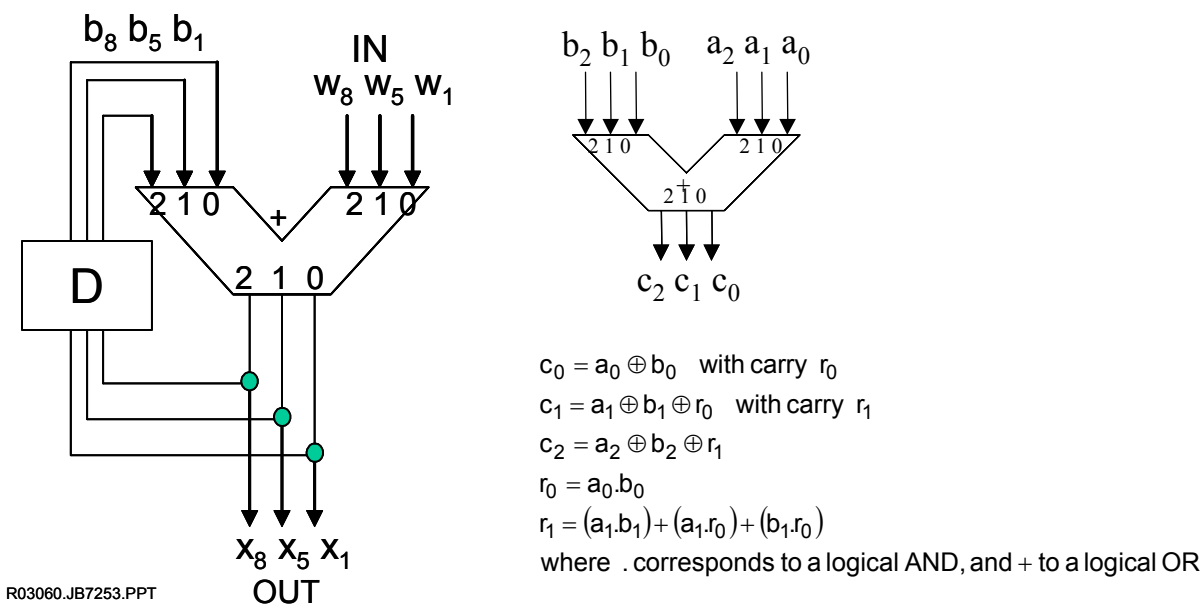
Figure 3-44: Differential Coder and Modulo-8 Adder Principle

3.6.3.3   Convolutional Coder

The convolutional coder used to implement the trellis is based on the work described in reference [14] and is depicted in figure 3-45. This code corresponds to one of the 'best' codes for phase transparency.

The systematic coder is implemented with the following characteristics:

- number of states: 64 states;
- constraint length: K = 7;
- Rate = 3/4.

The convolutional encoder is specified by the following polynomial in octal: h^3=050, h^2=024, h^1=006, h^0=103. Figure 3-44 shows the recommended convolutional encoder. The shift registers of the encoder are clocked at the rate of $R_{ChS}/4$.
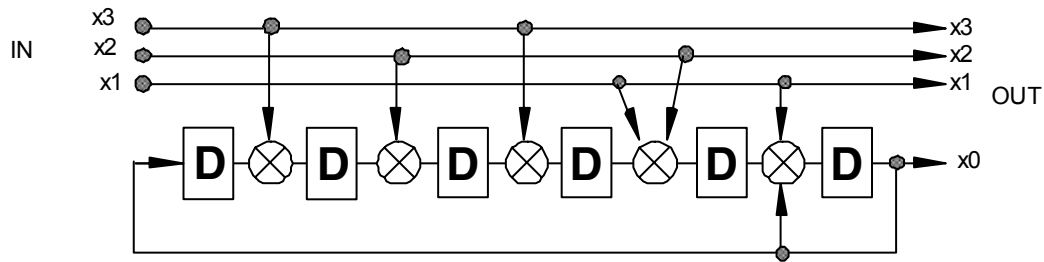
Figure 3-45: Convolutional Coder Recommended for High Data Rates

The number of coded bits is the same for the four modulation efficiencies (i.e., the same structure is used for 2, 2.25, 2.5, and 2.75 bits/channel-symbol), only the number of uncoded bits is changed. The advantage of this coder is its optimized performance and the reduced internal rate which is equal to 1/8, 1/9, 1/10, or 1/11 of the information rate.

3.6.3.4   Constellation Mapper for 4D-8PSK-TCM

The constellation mapper principles are given in figures 3-46 to 3-49 for the four possible efficiencies of this modulation (i.e., 2 bits/channel-symbol, 2.25 bits/channel-symbol, 2.5 bits/channel-symbol and 2.75 bits/channel-symbol). These mappers implement the straightforward logical mapping described in the equations below. The correspondence between the signals $Z^{(i)}$ at the input of the modular and the 8PSK phase states of the constellations follows a natural mapping (i.e., 0, 1, 2 …, 7).

If $Z^{(i)}$ represents the signals (three lines) at the input of the modulator with $Z^{(0)}$ being the signal set of the first constellation and $Z^{(3)}$ being the signal set of the fourth constellation, the signal set $Z^{(i)}$ is represented by the following equation. This representation shows that the bits which are common to each vector set (shown in the first part of right-hand side of each equation) are sensitive to a phase rotation of $\pi/4$ and will be differentially encoded (see 3.6.3.1).

(i) Equation for 2 bits/channel symbol efficiency

$$\begin{bmatrix} Z^{(0)} \\ Z^{(1)} \\ Z^{(2)} \\ Z^{(3)} \end{bmatrix} = \left[\left(4x^{(8)} + 2x^{(5)} + x^{(1)}\right)\begin{pmatrix} 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} + 4\begin{pmatrix} 0 \\ x^{(7)} \\ x^{(6)} \\ x^{(7)} + x^{(6)} + x^{(4)} \end{pmatrix} + 2\begin{pmatrix} 0 \\ x^{(3)} \\ x^{(2)} \\ x^{(3)} + x^{(2)} + x^{(0)} \end{pmatrix} \right] \mathrm{mod}\,8$$
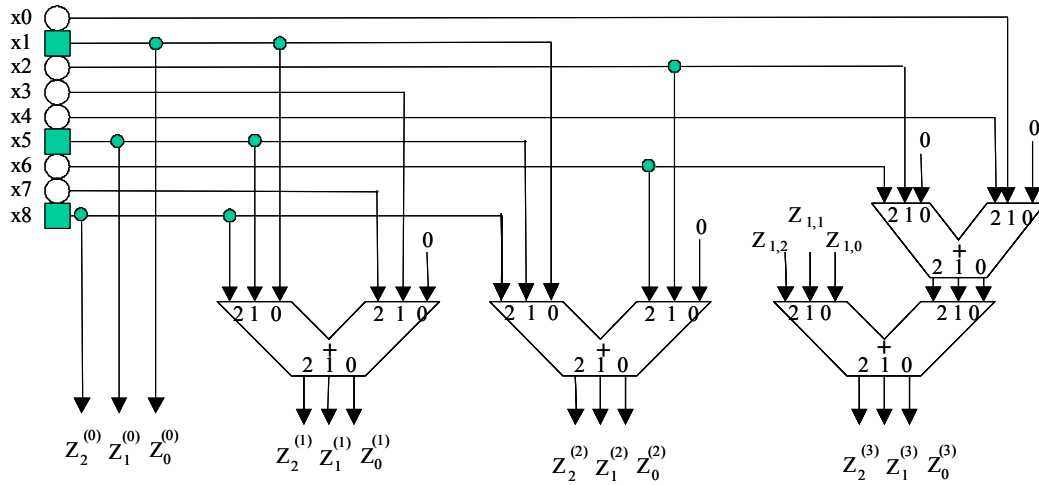
■ = line connected to differential coder

○ = line connected to serial-to-parallel converter or convolutional coder

Figure 3-46: Constellation Mapper for 2 Bits/Channel-Symbol

(ii) Equation for 2.25 bits/channel symbol efficiency

$$\begin{bmatrix} Z^{(0)} \\ Z^{(1)} \\ Z^{(2)} \\ Z^{(3)} \end{bmatrix} = \left[\left(4x^{(9)} + 2x^{(6)} + x^{(2)} \right) \begin{pmatrix} 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} + 4 \begin{pmatrix} 0 \\ x^{(8)} \\ x^{(7)} \\ x^{(8)} + x^{(7)} + x^{(5)} \end{pmatrix} + 2 \begin{pmatrix} 0 \\ x^{(4)} \\ x^{(3)} \\ x^{(4)} + x^{(3)} + x^{(1)} \end{pmatrix} + \begin{pmatrix} 0 \\ x^{(0)} \\ 0 \\ x^{(0)} \end{pmatrix} \right] \mathrm{mod}\,8$$
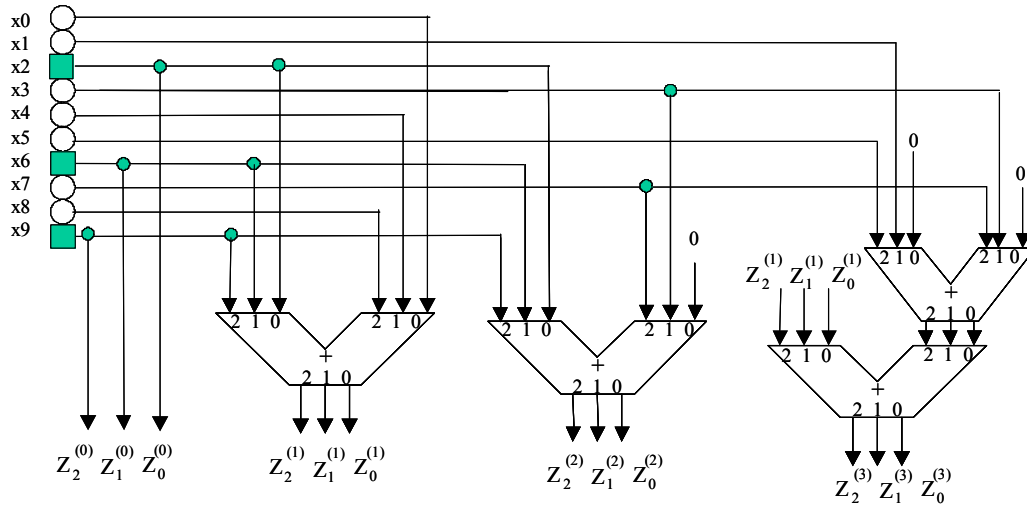
■ = line connected to differential coder

○ = line connected to serial-to-parallel converter or convolutional coder

Figure 3-47: Constellation Mapper for 2.25 Bits/Channel-Symbol

(iii) Equation for 2.5 bits/channel symbol efficiency

$$\begin{bmatrix} Z^{(0)} \\ Z^{(1)} \\ Z^{(2)} \\ Z^{(3)} \end{bmatrix} = \left[\left(4x^{(10)} + 2x^{(7)} + x^{(3)} \right) \begin{pmatrix} 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} + 4 \begin{pmatrix} 0 \\ x^{(9)} \\ x^{(8)} \\ x^{(9)} + x^{(8)} + x^{(6)} \end{pmatrix} + 2 \begin{pmatrix} 0 \\ x^{(5)} \\ x^{(4)} \\ x^{(5)} + x^{(4)} + x^{(2)} \end{pmatrix} + \begin{pmatrix} 0 \\ x^{(1)} \\ x^{(0)} \\ x^{(1)} + x^{(0)} \end{pmatrix} \right] \bmod 8$$
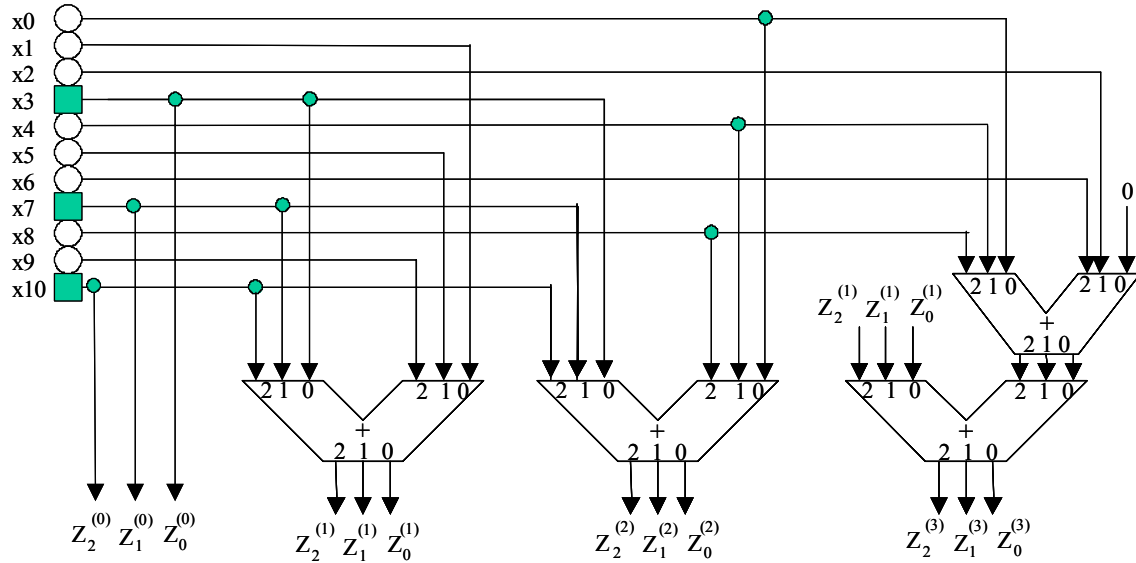
$\square$ = line connected to differential coder

$\bigcirc$ = line connected to serial-to-parallel converter or convolutional coder

Figure 3-48: Constellation Mapper for 2.5 Bits/Channel-Symbol

(iv) Equation for 2.75 bits/channel-symbol efficiency

$$
\begin{bmatrix} Z^{(0)} \\ Z^{(1)} \\ Z^{(2)} \\ Z^{(3)} \end{bmatrix} = \left[\left(4x^{(11)} + 2x^{(8)} + x^{(4)}\right)\begin{pmatrix} 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} + 4\begin{pmatrix} 0 \\ x^{(10)} \\ x^{(9)} \\ x^{(10)} + x^{(9)} + x^{(7)} \end{pmatrix} + 2\begin{pmatrix} 0 \\ x^{(6)} \\ x^{(5)} \\ x^{(6)} + x^{(5)} + x^{(3)} \end{pmatrix} + \begin{pmatrix} 0 \\ x^{(2)} \\ x^{(1)} \\ x^{(2)} + x^{(1)} + x^{(0)} \end{pmatrix} \right] \bmod 8
$$
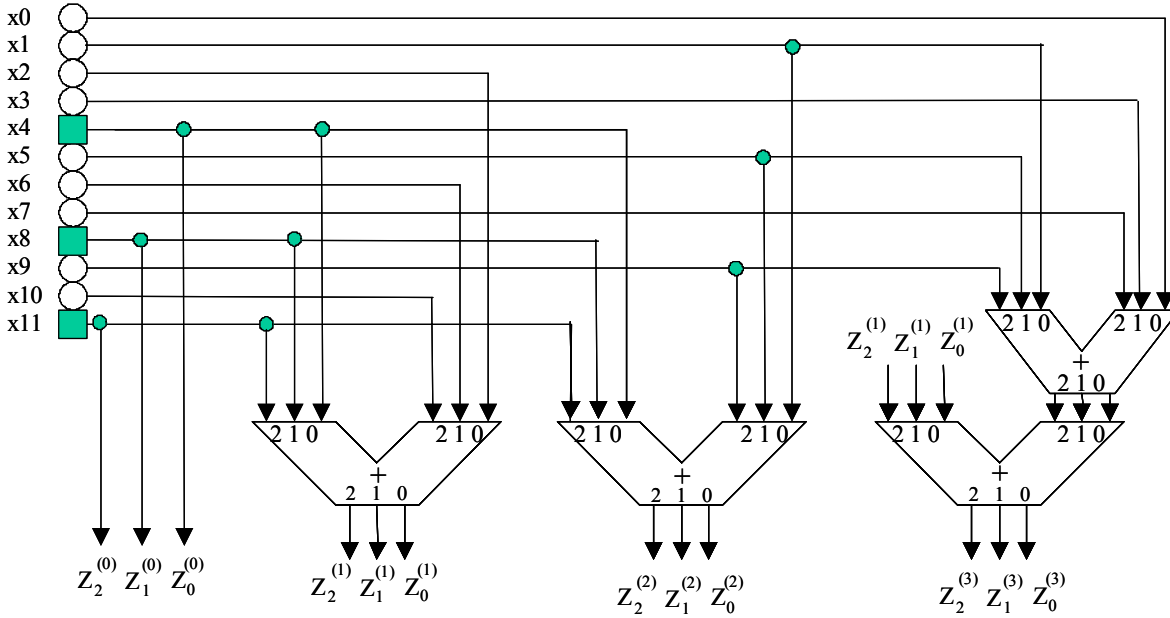
Figure 3-49: Constellation Mapper for 2.75 Bits/Channel-Symbol

3.6.3.5 Coder/Mapper Implementation at 2, 2.25, 2.5 and 2.75 Bits/Channel-Symbol Efficiency

The principle of the coder-mapper for 2, 2.25, 2.5, and 2.75 bits/channel-symbol efficiency is given in figures 3-50 through 3-53.
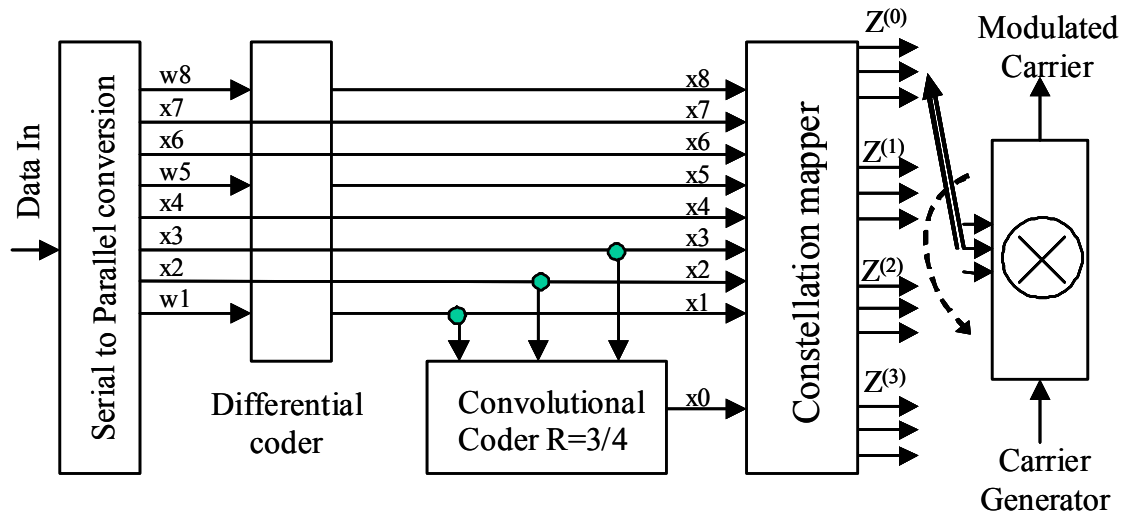
Figure 3-50: Coder and Mapper Implementation for 2 Bits/Channel-Symbol Efficiency
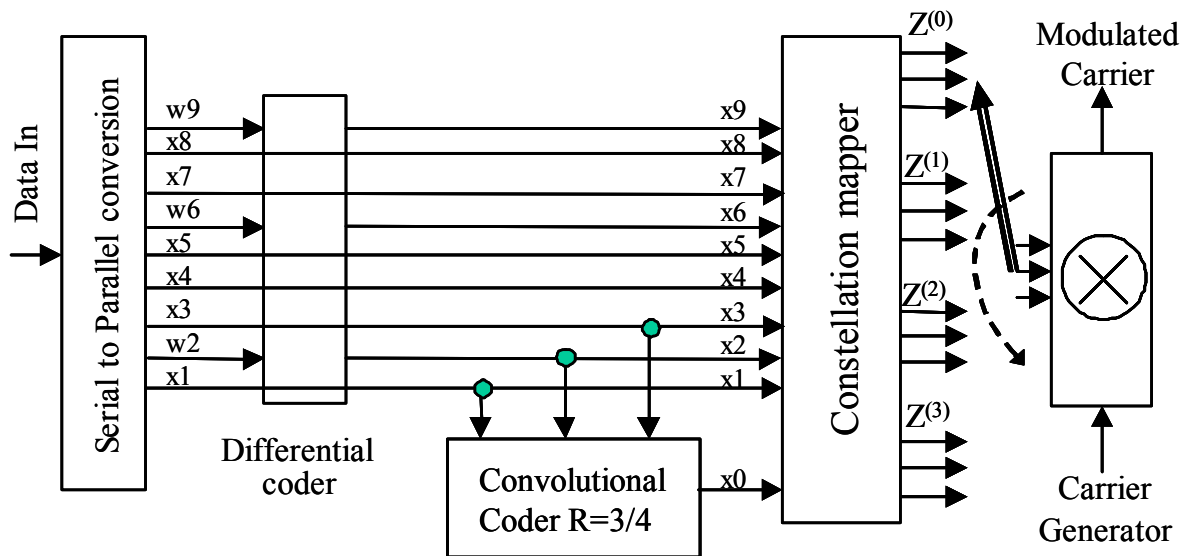
Figure 3-51: Coder and Mapper Implementation at 2.25 Bits/Channel-Symbol Efficiency
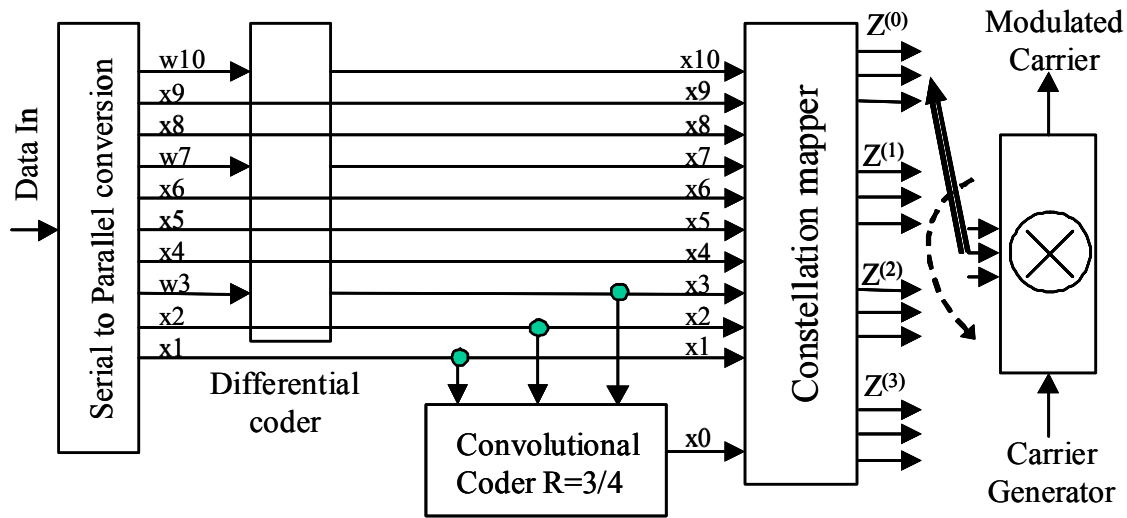
Figure 3-52: Coder and Mapper Implementation at 2.5 Bits/Channel-Symbol Efficiency
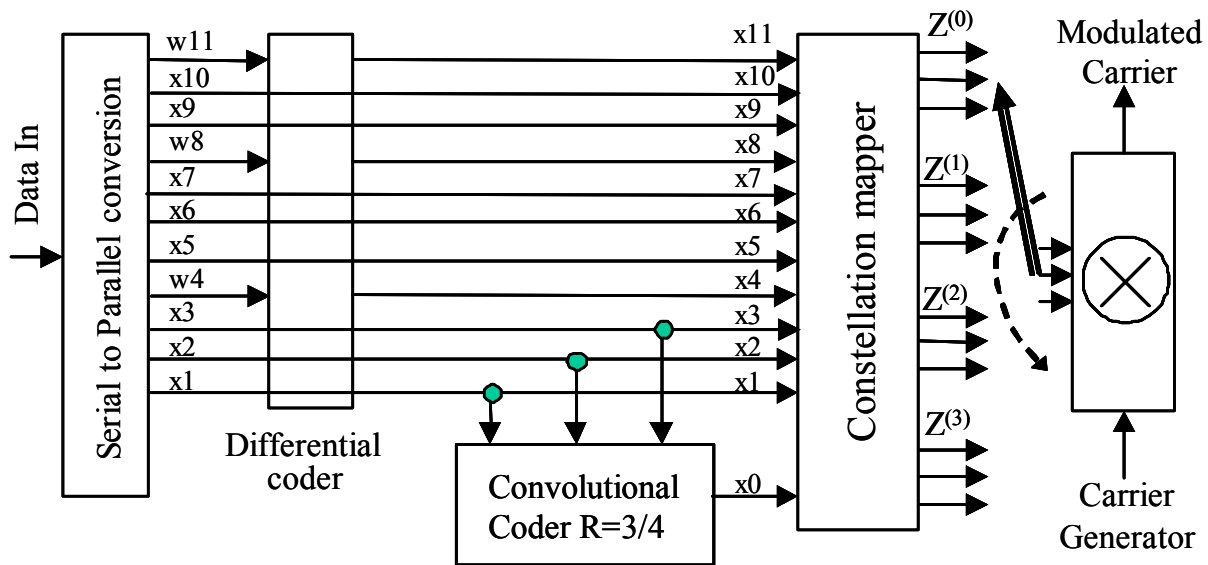
Figure 3-53: Coder and Mapper Implementation at 2.75 Bits/Channel-Symbol Efficiency

3.6.4 4D-8PSK-TCM PHASE NOISE RECOMMENDATION

It is recommended that the phase noise for all the oscillators of the 4D-8PSK-TCM communication chain be limited according to the mask given in figure 3-54 for channel symbol rates from 1 Msps up to 100 Msps. The figure shows the double sided phase noise mask 2L(f) in dBc/Hz versus frequency in Hz.
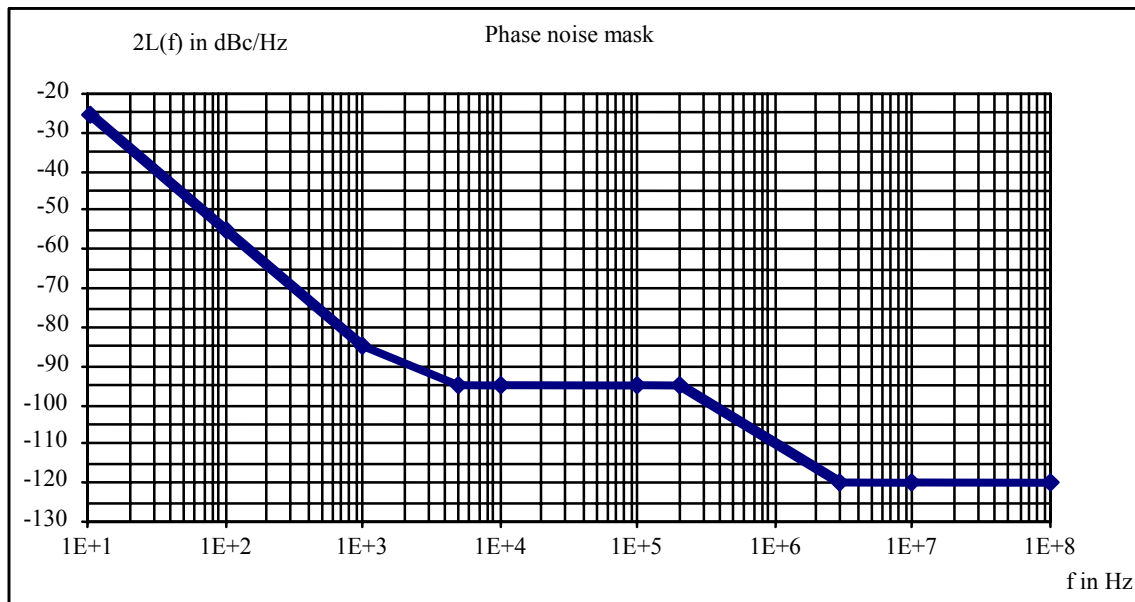
Figure 3-54: 4D-8PSK-TCM Phase Noise Mask Recommendation

3.6.5 BASEBAND SRRC SHAPING FILTER

The channel filtering is obtained with a Square Root Raised Cosine (SRRC) baseband shaping filter followed by a whitening filter located prior to the linear I/Q 8PSK modulator or equivalent device, with a channel roll-off factor $\alpha = 0.35$ or 0.5. Another solution consists of representing each point of the constellation with a pulse waveform corresponding to the impulse response of the SRRC filter. This solution does not require a whitening filter. This waveform shaping can be used in association with a linear or non-linear power amplifier. The block diagram of the transmitter with channel filtering is shown in figure 3-55.

The predetection filter (matched filter) in the receiver must be a square root raised cosine filter with the roll-off factor α of 0.35 or 0.5, according to the roll-off factor used at the transmitter. The frequency response of the SRRC filter is given by:

$$H(f) = \begin{cases} 1 & |f| < f_N(1-\alpha) \\ \sqrt{\dfrac{1}{2} + \dfrac{1}{2}\sin\left(\dfrac{\pi}{2f_N}\left[\dfrac{f_N - |f|}{\alpha}\right]\right)} & f_N(1-\alpha) \le |f| \le f_N(1+\alpha) \\ 0 & |f| > f_N(1+\alpha) \end{cases}$$

where $f_N = 1/(2T_{ChS}) = R_{ChS}/2$ is the Nyquist frequency, α is the roll-off factor, and R_{ChS} is the channel symbol rate.

The corresponding impulse response of the SRRC filter is given by:

$$h(t) = \frac{4\alpha}{\pi\sqrt{T_{ChS}}} \frac{\cos\left(\dfrac{(1+\alpha)\pi t}{T_{ChS}}\right) + \dfrac{T_{ChS}}{4\alpha t}\sin\left(\dfrac{(1-\alpha)\pi t}{T_{ChS}}\right)}{1 - \left(4\alpha t / T_{ChS}\right)^2}$$
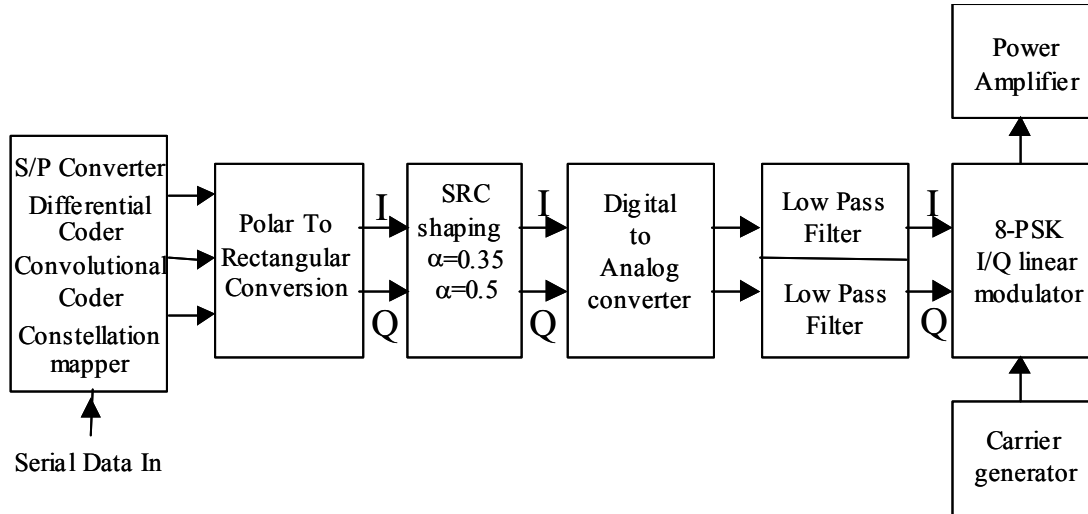
Figure 3-55: Principle of the Transmitter

Since SRRC shaping does not produce a constant envelope signal and causes some intersymbol interference when not matched with another SRRC filter, the phasor diagrams exhibit bowls around the phase points as shown in figure 3-56. For simplicity, transactions are not represented in the figure.
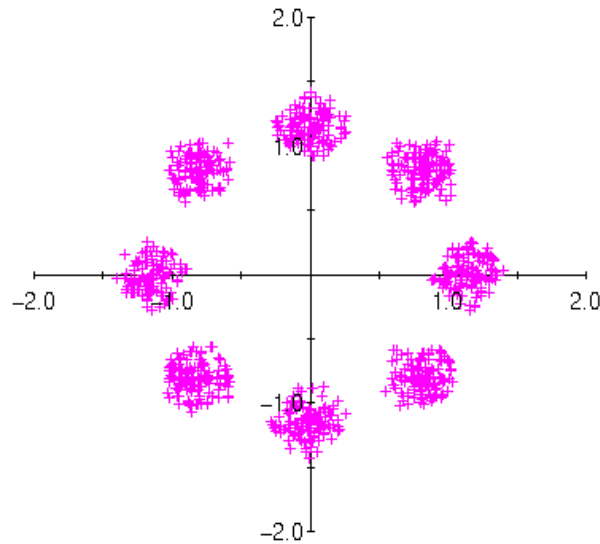
Figure 3-56: SRRC ($\alpha = 0.35$) Shaped 4D-8PSK-TCM Phasor Diagram

After SRRC matched filtering at the receiver, the resultant waveform consists of overlapping Raised Cosine (RC) pulse shapes. The eye diagram of the phase values between $-\pi$ to π is shown in figure 3-57. As the figure shows, good symbol synchronization is needed to avoid degradation due to ISI. The time axis is normalized by T_{ChS} with a $T_{ChS}/2$ offset so that the maximum eye opening is centered in the figure.
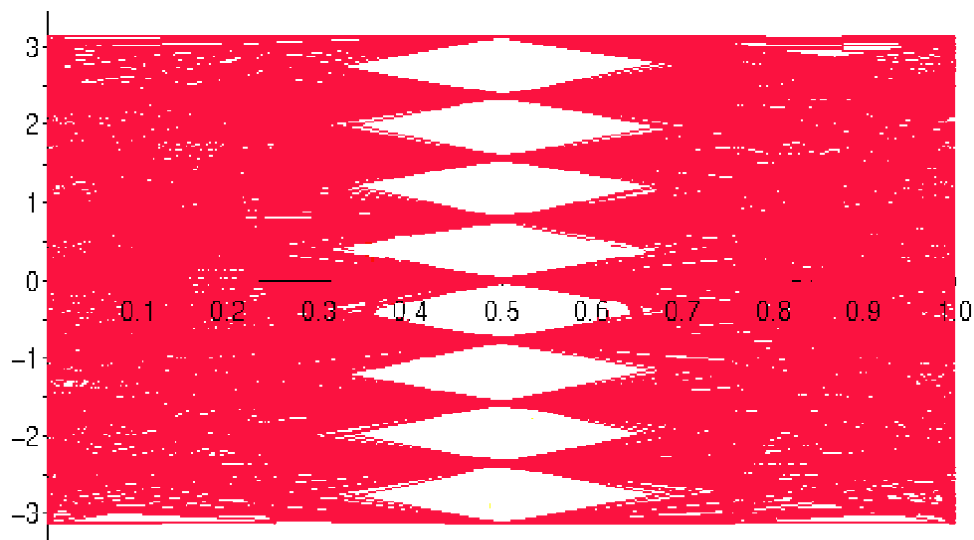
Figure 3-57:   RC ($\alpha = 0.35$) Shaped 4D-8PSK-TCM Phase Eye Diagram at Output of Matched Filter

4 SUMMARY

With more missions at high data rates demanding use of limited spectral resources for space-to-earth telemetry, the SFCG issued Recommendation 21-2 to limit the spectral bandwidth of the Category A missions in the SRS and EESS bands. A recommendation for Category B missions is currently under consideration by SFCG. The CCSDS was commissioned by the SFCG to recommend bandwidth efficient modulations, which could meet the SFCG spectral masks and provide good end-to-end performance.

After extensive study and analysis, the CCSDS approved Recommendations 401 (2.4.17A) B-1, 401 (2.14.17) B-1, and 401 (2.4.18) B-1 addressing the use of bandwidth-efficient modulations for high data rate missions in the SRS and EESS frequency allocations. Table 3-3 summarizes the CCSDS recommended bandwidth-efficient modulations and their respective frequency bands. A record of the CCSDS studies can be found in the CCSDS Yellow Book, *Proceedings of the CCSDS RF and Modulation Subpanel 1E on Bandwidth-Efficient Modulations* (reference [1]).

This Green Book on bandwidth-efficient modulations supplements the three CCSDS Recommendations on bandwidth-efficient modulations by providing technical descriptions of these modulations. The performance of these modulations are dependent on the many factors including channel coding, power amplifier nonlinearities, receiver type, channel characteristics, and transponder hardware distortions. In annex B, simulated end-to-end BER performance and spectral characteristics of most of the recommended modulations are provided for a selected channel model (the SSPA reference model in annex B) and no hardware distortions.

Table 4-1: CCSDS Recommendations on Bandwidth-efficient Modulations

Frequency Band	Applicable CCSDS Recommendation(s)	Recommended Modulations
2200-2290 MHz 8450-8500 MHz	401 (2.4.17A) B-1	• GMSK BT_s=0.25 with precoding • FQPSK-B • Filtered OQPSK
2290-2300 MHz 8400-8450 MHz	401 (2.4.17B) B-1	• GMSK BT_s=0.5 with precoding • T-OQPSK
8025-8400 MHz	401 (2.4.18) B-1	• 4D-8PSK-TCM

ANNEX A

GLOSSARY

AM/AM	Amplitude-dependent amplitude distortion
AM/PM	Amplitude-dependent phase distortion
AGC	Automatic Gain Control
BER	Bit Error Rate
BPSK	Binary Phase Shift Keying
Category A mission	Missions whose altitude above Earth is less than 2×10^6 km
Category B mission	Missions whose altitude above Earth is greater than 2×10^6 km
CCSDS	Consultative Committee on Space Data Systems
CPM	Continuous Phase Modulation
dB	Decibel
E_b/N_o	Energy per bit to Noise spectral density ratio
E_s/N_o	Energy per symbol to Noise spectral density ratio
EESS	Earth Exploration Satellite Service
FQPSK	Feher Quadrature Phase Shift Keying
FSK	Frequency Shift Keying
GHz	Gigahertz
GMSK	Gaussian Minimum Shift Keying
I&D	Integrate-and-Dump
ISI	Inter-Symbol Interference
ITU	International Telecommunication Union
LPF	Low Pass Filter
Msps	Mega Symbols Per Second
NRZ	Non-Return to Zero
OBO	Output Back-off
OQPSK	Offset Quadrature Phase Shift Keying

OQPSK I/Q	I/Q Modulated Offset Quadrature Phase Shift Keying
OQPSK/PM	Phase Modulated Offset Quadrature Phase Shift Keying
OSC	Oscillator
PM	Phase Modulated
PSD	Power Spectral Density
R_s	Coded symbol rate at input to modulator
R_b	Information bit rate
R_{ChS}	Channel symbol rate
RF	Radio Frequency
SFCG	Space Frequency Coordination Group
SOQPSK	Shaped Offset Quadrature Phase Shift Keying
SQORC	Staggered Quadrature Offset Raised Cosine
SRRC	Square Root Raised Cosine
SRS	Space Research Service
SSPA	Solid State Power Amplifier
T_s	Coded symbol period at input to modulator
T_b	Bit period
T_{ChS}	Channel symbol period
TCM	Trellis Coded Modulation
T-OQPSK	Trellis-coded Offset Quadrature Phase Shift Keying
TWTA	Traveling Wave Tube Amplifier
VCO	Voltage Controlled Oscillator
XPSK	Cross Correlated Phase Shift Keying

ANNEX B

SIMULATED MODULATION PERFORMANCE WITH SSPA OPERATING IN SATURATION

This annex provides simulated performance data of the efficient modulations described in this Green Book when amplified by an SSPA operating at 0 dB output backoff referenced to maximum output power (corresponding to Input Backoff at –3 dB for the reference SSPA in this annex). This data includes occupied bandwidth, BER with matched filter and I&D receivers, and interference susceptibility. The reader should be aware that the performance of these modulations is highly dependent on the actual receiver and transmitter hardware characteristics including but not limited to the power amplifier linearity and operating point, symbol asymmetry, data imbalance, modulator gain/phase imbalance, local oscillator phase noise and, for digital applications, time/amplitude quantization. **The data provided in this annex are indicative of system performance expected using the reference model. Actual performance is highly dependent upon transmitter and receiver characteristics.**

Only distortions caused by amplifier AM/AM and AM/PM are considered in the results presented in this annex. The AM/AM and AM/PM curves used in the simulations originated from measurements of a 10W SSPA provided by ESA and are shown in figures B-1 and B-2, respectively . The performance data in this annex has been extracted from study reports which can be found in the CCSDS Yellow Book, *Proceedings of the CCSDS RF and Modulation Subpanel 1E on Bandwidth-Efficient Modulations* (reference [1]).
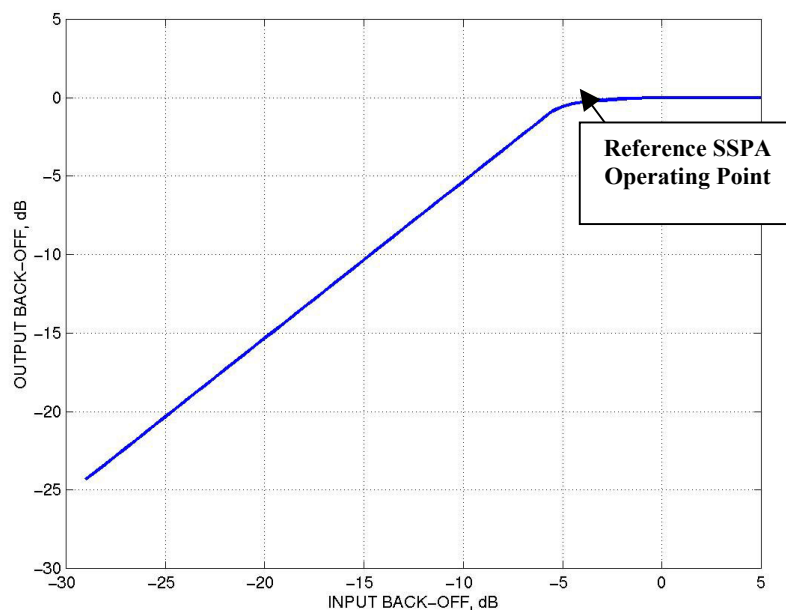
Figure B-1: AM/AM Characteristic of Reference SSPA
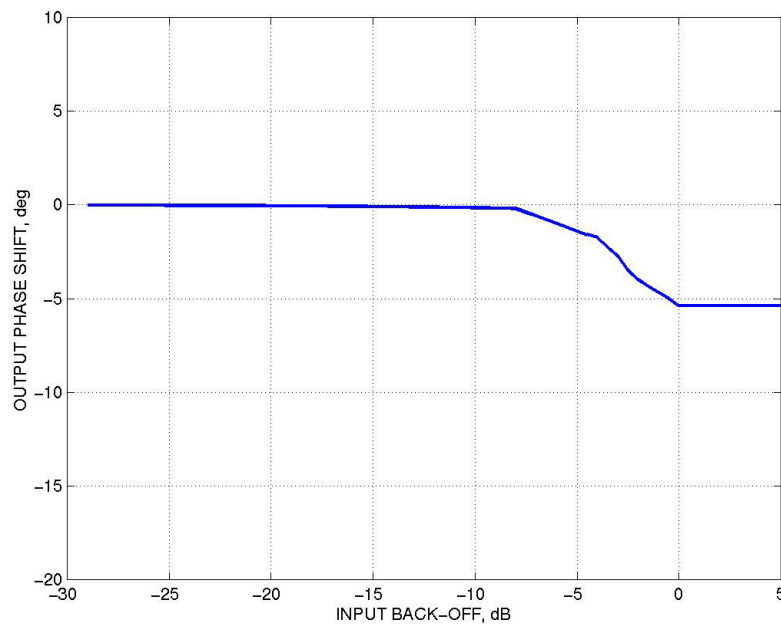
Figure B-2: AM/PM Characteristic of Reference SSPA

B1   OCCUPIED BANDWIDTH

In the CCSDS studies on bandwidth-efficient modulations (reference [1]) which provided the data for this subsection, the user spacecraft power amplifier was assumed to be operated at 0 dB OBO reference point. This mode of operation allows for the most efficient use of limited spacecraft onboard power and is consistent with the vast majority of Category B missions as well as many Category A missions. A side effect of operating near saturation is that the amplifier will introduce nonlinear distortions to a non-constant envelope signal which can result in the regeneration of filtered sidelobes. This effect is known as spectral regrowth. In this subsection, the spectral containment of the recommended modulations after a saturated power amplifier as measured by the occupied bandwidth is detailed.

Occupied bandwidth is defined by article 1.153 of the ITU Radio Regulations (ITU RR) as *the width of a frequency band such that, below and above the upper frequency limits, the mean powers emitted are each equal to a specified percentage β/2 of the total mean power of a given emission*, where β is taken to be 1%. For β = 1%, this is often referred to as the 99% power containment bandwidth.

Table B-1 shows the simulated occupied bandwidths normalized to the symbol rate[13] at the input to the modulator of selected bandwidth-efficient modulations recommended for Category A space-to-earth links at the output of a saturated SSPA. In addition, the

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[13] See 2.4 for bit/symbol terminology definitions used in this Green Book.

normalized –60 dB bandwidths[14] are given. Table B-2 shows the occupied bandwidths for Category B recommended efficient modulations.

Table B-1: **Occupied Bandwidth of Category A Recommended Efficient Modulations after Spectral Regrowth Due to Saturated SSPA**

Modulation Type	Two Sided -60 dB Bandwidth [14]	Occupied Bandwidth
Unfiltered BPSK[15]	635 R_s	20.56 R_s
Baseband Filtered OQPSK/PM		
Butterworth 6th order	2.70 R_s	0.88 R_s
SRRC (α=0.5)	2.68 R_s	0.88 R_s
Bessel 6th order	3.69 R_s	0.93 R_s
Baseband Filtered OQPSK I/Q		
Butterworth 6th order	4.06 R_s	0.86 R_s
SRRC α=0.5	4.24 R_s	0.88 R_s
Bessel 6th order	4.95 R_s	1.34 R_s
Precoded GMSK BT_s = 0.25	2.14 R_s	0.86 R_s
SOQPSK		
Version A	1.94 R_s	0.77 R_s
Version B	2.06 R_s	0.83 R_s
FQPSK-B	2.18 R_s	0.78 R_s

Table B-2: **Occupied Bandwidth of Category B Recommended Efficient Modulations after Spectral Regrowth Due to Saturated SSPA**

Modulation Type	-60 dB Bandwidth	Occupied Bandwidth
Precoded GMSK BT_s=0.5	3.02 R_s	1.03 R_s
T-OQPSK	3.02 R_s	0.81 R_s

---

[14] The –60 dB bandwidth is defined here as the frequency band such that, below the lower frequency limit and above the upper frequency limit, the continuous power spectral density does not exceed –60 dB/Hz below the peak PSD over any 1 Hz bandwidth. This level is chosen to coincide with the floor of the SFCG 21-2 spectral emissions mask.

[15] For reference purposes only, not part of bandwidth efficient modulation recommendation

B2 SIMULATED END-TO-END BER PERFORMANCES

B2.1 Uncoded Bit Error Rate (BER) Performance in a Non-Linear Channel

As a general matter, all of the bandwidth-efficient modulation techniques included in these recommendations provide acceptable BER performance for use in space data systems. However, for each of these modulations, the precise BER performance of any given system is dependent upon the detection algorithm used in the receiver. Accordingly, a meaningful characterization of the BER performance of each modulation type must include some insight into the performance of the modulation type with the receiver types likely to be used.

The optimal receivers needed to achieve the theoretical BER performance for these modulation types incorporate precisely matched filters and, in some cases, the use of a Viterbi detection algorithm. In many cases, nearly optimal performance can be achieved using a considerably simpler and less costly receiver structure. The uncoded performance of some bandwidth-efficient modulations, including those recommended by the CCSDS, using the receiver types deemed most likely to be employed are summarized in table B-3 below.

Table B-3: Simulated Uncoded BER Performance of Recommended Category A Efficient Modulations with Distortions Due to Saturated SSPA

Modulation Type	Receiver Type	E_b/N_o for 10^{-3} BER	E_b/N_o for 10^{-5} BER	CCSDS Yellow Book Reference
Unfiltered BPSK (for reference only)	Integrate and Dump	6.8 dB	9.6 dB	1-05, 1-12

Baseband Filtered OQPSK/PM
  Butterworth 6th order
  SRRC α=0.5
  Bessel 6th order
	Integrate and Dump	7.6 dB
		7.6 dB
		7.6 dB
			10.5 dB
			10.6 dB
			10.8 dB
				1-07

Baseband Filtered OQPSK I/Q
  Butterworth 3rd order
  Butterworth 6th order
  SRRC α=0.5
  Bessel 6th order
	Integrate and Dump	7.4 dB
		7.4 dB
		7.4 dB
		7.4 dB
			10.5 dB
			10.5 dB
			10.5 dB
			10.5 dB
				1-07

Pulse-Shaped SRRC α=0.5	Matched Filter	7.4 dB	10.5 dB	1-05, 1-12
Precoded GMSK BT_s=0.25	Viterbi Receiver	7.0 dB	10.0 dB	1-05, 1-12

SOQPSK
  Version A
  Version B
	Viterbi Receiver	7.4 dB[16]
		7.0 dB[17]
			10.6 dB[16]
			9.8 dB[17]
				3-05

FQPSK-B	Viterbi Receiver	7.4 dB	10.4 dB	1-12

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[16] 8 State Viterbi Matched Filter Receiver.

[17] 32 State Viterbi Matched Filter Receiver.

Table B-4:   Simulated Uncoded BER Performance of Recommended Category B Efficient Modulations with Distortions Due to Saturated SSPA

Modulation Type	Receiver Type	E_b/N_o for 10^{-3} BER	E_b/N_o for 10^{-5} BER	CCSDS Yellow Book Reference
Precoded GMSK BT_s=0.5	Viterbi Receiver	6.8 dB	9.7 dB	1-05, 1-12
T-OQPSK	Viterbi Receiver	7.2 dB	10.1 dB	1-12

B2.2   Coded Bit Error Rate (BER) Performance in Non-Linear Channel

Forward error correcting codes can be used to reduce the E_b/N_o required to meet BER requirements.   This subsection provides simulated BER of selected bandwidth-efficient modulations using the CCSDS standard rate ½, k=7 convolutional inner code concatenated with a (255,223) Reed-Solomon outer code. The BER simulations included a model of a 10W ESA SSPA whose AM/AM and AM/PM characteristics are shown in figures B-1 and B-2, respectively. The Viterbi decoder in the simulations used 3-bit quantization of the metrics and a decoding depth of 70 bits. In the simulations, a Reed-Solomon interleaving depth of 5 was used. A coding gain on the order of 0.1 dB can be obtained by using 8-bit quantization instead of 3-bit quantization.

Table B-5:   Simulated BER Performance of Category A Efficient Modulations with Concatenated Code in Non-linear Channel

Modulation Type	Receiver Type	E_b/N_o for 10^{-6} BER	CCSDS Yellow Book Reference
Unfiltered BPSK (reference only)	Integrate and Dump	2.55 dB	1-06, 1-14

Baseband Filtered OQPSK/PM
    Butterworth 6th Order
    SRRC α=0.5
	Integrate and Dump	3.09 dB
		3.16 dB
			N/A

Baseband Filtered OQPSK I/Q
    Butterworth 3rd order
    Butterworth 6th order
    SRRC α=0.5
	Integrate and Dump	2.91 dB
		3.04 dB
		3.06 dB
			1-06, 1-14

Pulse-Shaped SRRC α=0.5	Matched Filter	2.77 dB	

Shaped Offset QPSK
    Version A
    Version B
	Integrate and Dump	3.74 dB
		3.46 dB
			N/A

Precoded GMSK BT_s=0.25	Quasi-Matched Filter + 3 tap equalizer	2.73 dB	1-06, 1-14
FQPSK-B	Quasi-Matched Filter + 3 tap equalizer	2.88 dB	1-14

Table B-6: Simulated Uncoded BER Performance of Recommended Category B Efficient Modulations with Concatenated Code in Non-linear Channel

Modulation Type	Receiver Type	E_b/N_o for 10^{-6} BER	CCSDS Yellow Book Reference
Precoded GMSK BT_s=0.5	Quasi-Matched Filter	2.58 dB	1-06, 1-14
T-OQPSK	Quasi-Matched Filter + 3 tap equalizer	2.81 dB	1-14

B2.3   4D-8PSK-TCM BER Performance

Figure B-4 shows the simulated bit error performance of 4D-8PSK-TCM with 2, 2.25, 2.5 and 2.75 bits/channel symbol efficiencies. The simulation results were obtained under the assumptions of a linear communications chain (i.e., linear power amplifier and linear 8PSK modulator in AWGN channel). As such, these results should not be compared with the BER results from B2.1 and B2.2 which assume non-linear power amplification.

The TCM decoder used for simulations is based on the implementation of the Viterbi algorithm (see figure B-3) but simplified with the 'trace-back' method (reference [16]), which consists to choose the survivor from the first node of the trellis only, assuming a sufficient truncation length. The number of parallel information bits m obtained before coding is 8, 9, 10 or 11 bits, according to the channel efficiency. The Branch Metrics (BM) are coded with 4 bits while cumulated metrics in 'Add Compare and Select' (ACS) operator are coded with 5 bits. The Viterbi algorithm is applied to a 64 states decoder with 8 branches per state and a truncation path length equal to 36. The output delivers m bits at a time which corresponds to the decoded information after processing of four successive phase states.
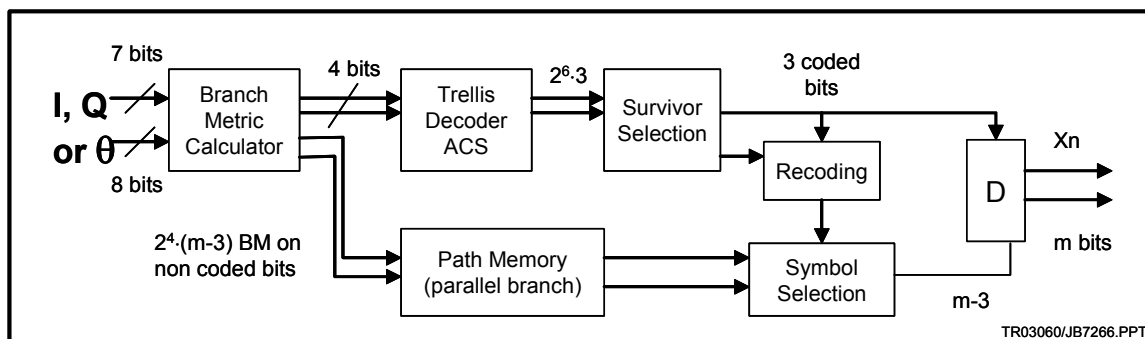
Figure B-3: Principle of the 4D-8PSK-TCM Decoder Used in Simulations

The BER obtained with the simulations is given in figure B-4 for the four efficiencies (plain curves). The dotted curves correspond to the lower bound (asymptotic curves) obtained from calculations taking into account the different minimum Euclidian distances obtained for each efficiency. Theoretical uncoded QPSK and 8PSK BER are given as reference.
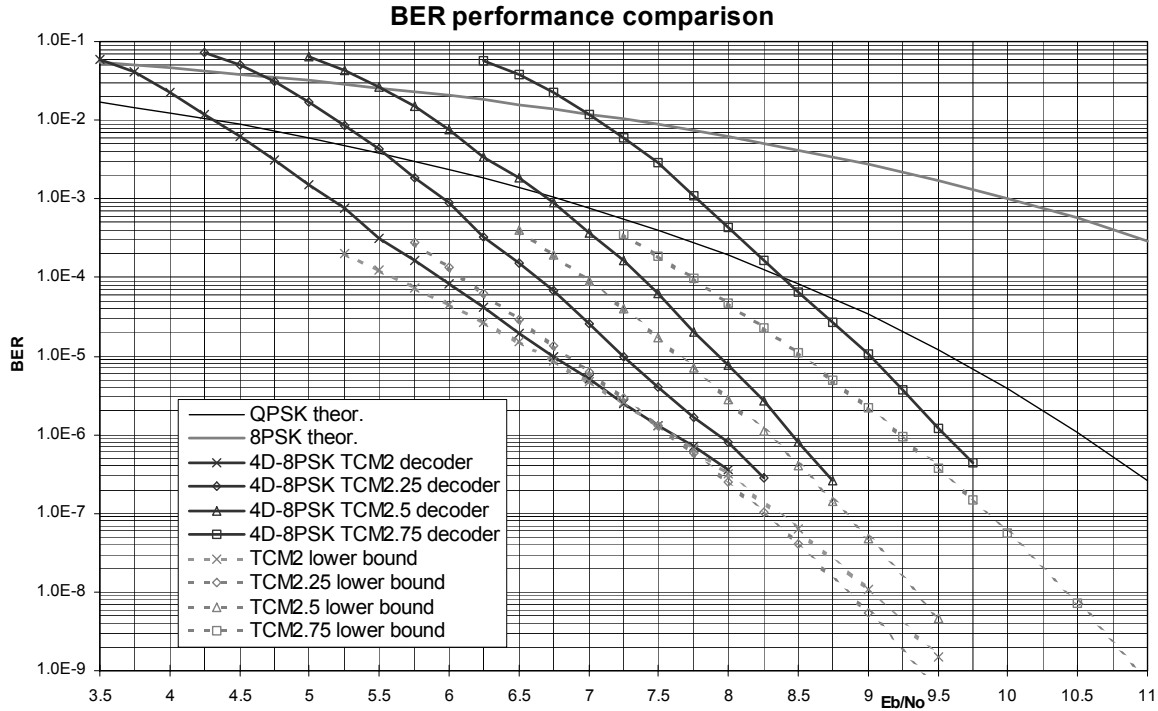
Figure B-4: **4D-8PSK-TCM BER vs. E_b/N_o in dB for 2, 2.25, 2.5, and 2.75 Bits/Channel Symbols**

B3   END-TO-END PERFORMANCES – INTERFERENCE SUSCEPTIBILITY

B3.1   GENERAL

Interference susceptibility is defined as the degradation in E_b/N_o to the victim modulation caused by an interfering signal source operating in the same or adjacent allocated frequency band. To a first order, interference susceptibility of a modulation is determined by the characteristics of the receiver detection filter. Thus the recommended bandwidth-efficient modulations with matched filter receivers are in general more susceptible to narrowband interference close to the carrier frequency than unfiltered BPSK but less susceptible to interference away from the carrier frequency due to the frequency response of the matched filter. This also holds true for wideband interference, although to a lesser extent as the interference is spread over a wider frequency range. In the limit as the interference becomes so wideband that it looks like white noise, the recommended modulations are roughly equally susceptible.

Likewise, if the same detection filter is used to detect all modulations (e.g., an integrate-and-dump filter), the interference susceptibility of the modulations is also roughly equivalent (reference [8]). Second order effects that affect interference susceptibility include the relative phase of the interferer with respect to the victim signal, the receiver Automatic Gain Control (AGC) and the carrier tracking loop.

B3.2   Narrowband Interference

Table B-7 shows simulation results (see reference [17]) on the minimum frequency separation between a narrowband interferer and the efficient modulation before the victim modulation suffered a specified E_b/N_o loss. The smaller the minimum interference frequency offset, the less susceptible the modulation is to narrowband interference. As the table shows, the more bandwidth-efficient the modulation, the closer the interfering tone could be before a 1 dB degradation occurred.

In these simulations, the narrowband interferer was modeled as a tone with equal power as the victim. The channel model consists of the reference SSPA operating at 0 dB output backoff with respect to maximum output power. The loss is measured with respect to the E_b/N_o required for each modulation to achieve 10^{-3} uncoded BER (including the effects of the SSPA) when there was no interference. Thus the degradation in the tables is the loss solely due to the interference and excludes any inherent modulation loss. Matched filters or quasi-matched filters were used in the simulations.

Table B-7: Narrowband Interference Susceptibility

Modulation	Minimum Interference Offset from f_c for Specified E_b/N_o Loss			
Type	0.25 dB Loss	0.50 dB Loss	0.75 dB Loss	1.00 dB Loss
Unfiltered BPSK	± 2.5 R_s	± 1.7 R_s	± 1.6 Rs	± 1.5 R_s
Filtered OQPSK[18]	± 0.7 R_s	± 0.47 R_s	± 0.45 R_s	± 0.43 R_s
SRRC-OQPSK	± 0.38 R_s	± 0.37 R_s	± 0.36 R_s	± 0.35 R_s
Precoded GMSK BT_s=0.5	± 0.6 R_s	± 0.58 R_s	± 0.53 R_s	± 0.5 R_s
Precoded GMSK BT_s=0.25	± 0.52 R_s	± 0.49 R_s	± 0.47 R_s	± 0.46 R_s
FQPSK-B	± 0.52 R_s	± 0.49 R_s	± 0.47 R_s	± 0.42 R_s

[18] 3rd order baseband Butterworth filter with BT_s = 0.5.

B3.3 Wideband Interference

B3.3.1 General

When bandwidth-efficient modulations are first deployed, a likely source of wideband interference will be legacy BPSK systems overlapping into the victim's frequency allocation. Table B-8 shows the wideband interference susceptibility (see reference [17]) of selected CCSDS-recommended bandwidth-efficient modulations with the wideband interference modeled as an unfiltered BPSK signal with equal power and data rate but with random phase offset to the victim modulation. The smaller the interference frequency offset, the less susceptible to interference the modulation is. The simulated channel model consisted of a SSPA operating at 0 dB output backoff referenced to maximum output power. As in table B-7, loss is measured with respect to the E_b/N_o required for 10^{-3} BER with no interference (i.e., loss due to interference only).

Table B-8: Wideband Interference Susceptibility

Modulation Type	Minimum Interference Offset from f_c for Specified E_b/N_o Loss			
	0.25 dB Loss	0.50 dB Loss	0.75 dB Loss	1.00 dB Loss
Unfiltered BPSK	$\pm > 3\,R_s$	$\pm 2.5\,R_s$	$\pm 2.4\,R_s$	$\pm 1.8\,R_s$
Filtered OQPSK[19]	$\pm 1.05\,R_s$	$\pm 0.96\,R_s$	$\pm 0.88\,R_s$	$\pm 0.8\,R_s$
SRRC-OQPSK	$\pm 1.3\,R_s$	$\pm 1.0\,R_s$	$\pm 0.93\,R_s$	$\pm 0.9\,R_s$
Precoded GMSK $BT_s=0.5$	$\pm 1.3\,R_s$	$\pm 1.18\,R_s$	$\pm 1.12\,R_s$	$\pm 1.09\,R_s$
Precoded GMSK $BT_s=0.25$	$\pm 1.06\,R_s$	$\pm 0.98\,R_s$	$\pm 0.90\,R_s$	$\pm 0.85\,R_s$
FQPSK-B	$\pm 0.79\,R_s$	$\pm 0.77\,R_s$	$\pm 0.75\,R_s$	$\pm 0.72\,R_s$

B3.3.2 Co-Channel Interference

Table B-9 shows the interference susceptibility of the recommended modulations assuming that the interferer is of the same modulation type as the victim (see reference [18]). Here, the interference susceptibility is measured by the required victim-power-to-interferer-power ratio, P_S/P_I, that caused a degradation of 1 dB with respect to ideal BPSK in AWGN at BER equal to 10^{-1}, 10^{-2}, and 10^{-3}. The higher the value of P_S/P_I, the more susceptible to interference the modulation is. Table B-9 shows the values for P_S/P_I with the co-channel interferer centered at the victim carrier frequency, and at a frequency offset a quarter times the coded symbol rate at the input to the modulator. The simulated channel model consisted of the reference SSPA operating at 0 dB output backoff with respect to maximum output power. In the results in table B-9, the interferer is assumed to have a worst-case phase and timing offset that causes the largest amount of degradation.

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[19] 3rd order baseband Butterworth filter with $BT_s = 0.5$.

Table B-9: Co-Channel Interference

Interference Frequency Offset	Modulation Type	P_s/P_I for BER=10^{-1}	P_s/P_I for BER=10^{-2}	P_s/P_I for BER=10^{-3}
0	Unfiltered BPSK	9.21 dB	13.69 dB	15.45 dB
	Filtered OQPSK[20]	9.69 dB	15.50 dB	18.81 dB
	SRRC OQPSK	9.39 dB	15.71 dB	19.84 dB
	Precoded GMSK $BT_s = 0.5$	7.40 dB	12.24 dB	14.39 dB
$1/(4T_s)$	Unfiltered BPSK	5.20 dB	10.06 dB	12.19 dB
	Filtered OQPSK[20]	7.63 dB	13.39 dB	16.69 dB
	SRRC OQPSK	7.32 dB	13.63 dB	17.78 dB
	Precoded GMSK $BT_s = 0.5$	5.55 dB	10.80 dB	13.21 dB

B4   CROSS-SUPPORT BER PERFORMANCE

B4.1   Integrate and Dump Receiver

Cross-support is defined here as the ability for a modulation to be successfully demodulated and detected by a receiver designed for a different modulation.   The modulations recommended in Recommendations 401 (2.4.17A) B-1 and 401 (2.4.17B) B-1 can all be viewed as OQPSK-type modulations. Thus it is not surprising that in many cases a matched filter receiver designed for a particular recommended OQPSK-type modulation is able to cross-support other recommended OQPSK-type modulations, although with some E_b/N_o degradation due to filter mismatch. However, this is true only for receivers with symbol-by-symbol detection; receivers based on trellis demodulation in general will not be compatible with other modulations unless the trellis codes are compatible. Also, 4D-8PSK-TCM in Recommendation 401 (2.4.18) cannot be cross-supported by an OQPSK-type receiver without substantial receiver modifications.

Of particular interest in terms of cross-support is the integrate-and-dump-type receiver that is present in many ground stations at the present time. Table B-10 shows the simulated uncoded E_b/N_o degradation of some recommended Category A bandwidth-efficient modulations using an I&D receiver and assuming the reference SSPA model operating at 0 dB output backoff with respect to maximum output power. Table B-11 shows the same data except for uncoded Category B recommended efficient modulations. The loss in tables B-10 and B-11 is measured with respect to ideal BPSK.

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[20] 3rd order baseband Butterworth filter with BT$_s$ = 0.5.

Table B-10:   Simulated Uncoded Loss of Category A Efficient Modulations Using I&D Receiver

Modulation Type	Loss at BER = 10^{-3}	Loss at BER = 10^{-5}
Baseband Filtered OQPSK/PM		
Butterworth 6th order	0.8 dB	1.1 dB
SRRC α=0.5	0.8 dB	1.4 dB
Bessel 6th order	0.5 dB	0.8 dB
Baseband Filtered OQPSK I/Q		
Butterworth 3rd order	0.6 dB	0.9 dB
Butterworth 6th order	0.6 dB	0.9 dB
Pulse-Shaped SRRC α=0.5	1.1 dB	1.7 dB
SRRC α=0.5	0.6 dB	0.9 dB
Bessel 6th order	0.6 dB	0.9 dB
SOQPSK		
Version A	2.5 dB	3.4 dB
Version B	1.0 dB	1.4 dB
Precoded GMSK BT_s = 0.25	1.2 dB	1.7 dB
FQPSK-B	2.1 dB	2.9 dB

Table B-11:   Simulated Uncoded Loss of Recommended Category B Efficient Modulations with I&D Receiver

Modulation Type	Loss at BER = 10^{-3}	Loss at BER = 10^{-5}
Precoded GMSK BT_s = 0.5	0.8 dB	1.2 dB
T-OQPSK	1.5 dB	2.1 dB

B4.2   Other Receivers

Table B-12 shows the simulated uncoded E_b/N_o required for 10^{-3} BER of some recommended bandwidth-efficient modulations using different types of receivers assuming the reference SSPA model operating at 0 dB output backoff with respect to maximum output power.

Table B-12:   Cross Support BER Performance of Recommended Modulation Formats Using Other Receiver Types

Receiver Type	Transmitter Type		
	GMSK	FQPSK-B	Filtered OQPSK
GMSK	7.1 dB	7.8 dB	7.1 dB
FQPSK-B	7.5 dB	8.2 dB	7.5 dB
Filtered OQPSK	7.5 dB	8.6 dB	7.3 dB
OQPSK	8.0 dB	9.2 dB	7.4 dB