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ENGINEERING DESIGN HANDBOOK

DESIGN FOR CONTROL OF PROJECTILE FLIGHT CHARACTERISTICS

HEADQUARTERS, U.S. ARMY MATERIEL COMMAND

SEPTEMBER 1966

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AMCP 706-242, Design for Control of Projectile Flight Characteristics, forming part of the Army Materiel Command Engineering Design Handbook Series, is published for the information and guidance of all concerned.

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FOR THE COMMANDER:

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PREFACE

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The Engineering Design Handbook of the Army Materiel Command is a coordinated series of handbooks containing brais information and fundamental data useful in the design and development of Army materiel and systems. The Handbooks are authoritative reference books of practical information and quantitative facts helpful in the design aud development of materiel that will meet the news of the Armed Forces.

This handbook, one of a series on ammunition, presents a general envey of the principal factors affecting the flight of projectiles, and describes the methods commonly used for predicting and influencing the flight performance.

The coefficients which characterize the aerodynamic forces and moments on a moving body are identified, methods for determining the coefficients applicable to a projectile having a given shape and center of gravity location are described, and the coefficients of a number of projectiles and projectile shapes are given.

The use of serodynamic coefficients in predicting stability, range and accuracy is described. The effects of variations in projectile shape and conter of gravity location on range, accuracy and lethality are discussed. Some material on prototype tasting and the effects of round-to-round variations in production lots is presented.

It is no longer possible, if it ever was, to crass into a few hundred pages all of the information required to intelligently design every type of conventional projectile. The author must choose between constructing a digest of a raisable information, or directing the designer to the sources pertinent to his problem, together with enough background material to make it possible for him to use the data in the original reports. The second approach has been chosen in this handbook; the material presented is intended to place the designer is a position to use new information as it is preduced by the various research facilities.

This text was prepared by B. L. Kessler, assisted by D. Vineberg, both of the staff of The Budd Company. Much of the material and many helpful comments were supplied by the U.S. Army Ballistis Research Laboratories and by the Piostinny and Frankford Arsenals. Final editing and arranging were by the Engineering Handbook Office of Duke University, prime contractor to the Army Research Office-Durham.

Elements of the U.S. Army Materiel Command having need for handbooks may submit requisitions or efficial requests directly to the Publications and Reproduction Agency, Letterhenny Army Depet, Chambersburg, Pennsylvania 17201. Contractors should submit such requisitions or requests to their contracting officers.

Commonts and suggestions on this handbook are welcome and should be addressed to Army Research Office-Durham, Box CM, Duke Statist, Durham, North Carolina 27796.

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list of symbols

| 4 | A constant describing the kind and | D | Drag, lb |
|------------------------------------|--|-----------------|---|
| | degree of asymmetry of a projectile, | đ | Maximum body diameter, ft |
| ^ ' | • | e | Base of natural logarithms |
| A . | Bore area, ft ³ | fps | Feet per moond |
| • • | Setback acceleration, ft/sec ² Constant in Q function | 0 | Acceleration of gravity, ft/sec* |
| . . | Fin span, tip-to-tip, ft | h | Altitude above sea level, ft |
| | Constant in Q function | I. | Axial moment of inertia, alug-ft ² |
| 6 | Fin chord, ft Constant in Q function | 17 ₂ | Transverse moment of inertia, alug- ft ² |
| 0.g. | Center of gravity | i | $\sqrt{-1}$; in complex notation indicates rotation by 90° |
| c.p. | Center of pressure Drag coefficient | K, | Modal vector, radians |
| C _P | Caliber | , ka | Axial radius of gyration, calibers |
| Ca. | Drag coefficient at zero yaw | r. | Transverse radius of gyration, |
| - | - · · · · · · · · · · · · · · · · · · · | F(| colibers |
| C _{Py} C _{Le} | Yaw-drag coefficient, per rad ^a Lift coefficient, per radian | L | Lift, lb Bore travel, ft |
| C _{He} | Normal force coefficient, per radian | ln | Natural logarithm |
| | $(C_{N_0} = C_{L_0} + C_0 \text{ for small yaw})$ | м | Mach number |
| C _{Npo} | Mangus force coefficient, per rad/sec, per radian | m | Mass, slugs |
| C _{Ma} | Static moment coefficient, per radian | N | Normal force, lb |
| C _{Mga} | Magnus moment coefficient, per rad/ | n . | Twist of rifling, cal/turn |
| ~e | sec, per radian | N, | Magnus force, lb |
| Си, + Си. | Damping moment coefficient, per rad/see | Ρ. | Chamber pressure, lb/ft [*] |
| Cy, | Rolling daraping moment coefficient, | P | Roll rate, rad/seq |
| · . | per rad/sec | p. | Equilibrium roll rate, rad/sec |
| Cip | Roll moment coefficient due to fin cant (at zero spin), per radian | ` Q | $=\sqrt{c+C_{D_{a}}M^{2}}=a+bM$ |

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LIST OF SYMBOLS (coat'd)

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| ilynamic pressure, ib/ff | Subscripts | |
|--|--------------|--|
| $(q = \frac{1}{2}p^{1/2})$ | 1 | Pertains to nutation vector |
| Anguiar velocity of a nonrolling missile-fixed coordinate system about | 1 | Periains to precession vector |
| a horizontal axis, rad/sec (in | 3 | Pertains to asymmetry vector |
| damping moment expression) | maz | Maximum value |
| Radiaza | aid . | Stendard value |
| Frontal area ft ² | | Dummy index: to be replaced by a |
| Travel of projectile, calibers | ž | sequence of specific indices when |
| Dynamic stability factor | | the subcripted quantity is used in a computation |
| Dynamic stability factor for | | • |
| $\sum_{i=1}^{n} \leq 0$ |) | Same definition as subscript i |
| Gyroscopic stability factor | J | Acrodynamic jump |
| Temperature, °F Time of flight, see | λ, | Damping exponent, per caliber of travel |
| Ause, sec | · • | Repose |
| Utility | - | Resonant |
| Velocity or airspeed, fpa | £ | Derivative with respect to angle of |
| Volume of projectile (including | | stack |
| boundary haver over the boattail, if present), ft ¹ | . 6 | Accustic ($V_* =$ speed of sound) |
| Weight, ib | B | Boty |
| Range | • | Bese |
| Distance along trajectory, ft | e | Efective |
| Vertical component of yaw, rad | | Equilibrium |
| Herisontal component of yaw, rad | \$ | ₹n. |
| Yaw angle, rol | ٠ | Initial conditions Sere-yow value |
| Static meaner factor, Ib-ft/radian Conficient of viscosity | 7 | Derivative with respect to spin |
| Spin (nondimensional) $r = pd/V$ | 7 | Terminel Tail |
| Acute used between a horisontal places and the tangent to the trajes- tory at the e.g. of the projectile | · | Trim |
| Angle of roll Angle of eccentation of a model | Supersoripte | Derivative with respect to time |
| vector, radians | | Derivative with respect to eslibera |

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CHAPTER 1

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INTRODUCTION

1-1. GEBERAL This handbook is concerned with the design of projectiles fired from guns. The projectiles considered are of greater size and weight than eas normally be fired from a hand-held weapon, and they are not equipped with guidance systems. It will be assumed that they are bodies of revolution, sometimes equipped with fins, and fly in the general direction of the longitudinal axis.

1-2. MEASURES OF PERFORMANCE

The principal measures of the performance of a projectile are:

- a. Range
- b. Lethality
- e. Ascuracy
- d. Time of fligh;

The values takes on by three measures when a round, or group of rounds, is fired are determined by atmospheric conditions, mussle velocity, gun orientation, target or burst elevation relative to gun, and by flight characteristics draigned and built into the projectile.

The primary flight characteristics which directly influence the trajectory are :

a. Drag

b. Aerodynamic jump

but both drug, which chiefly affects range and time of flight, and jump, which chiefly affects assuracy, are themselves determined by a number of projectile characteristics which we will call accordary flight characteristics, namely :

- a. Lero-yaw drag coefficient
- h. Yaw-drag spellcient
- c. Sectional density
- d. Lift coefficient
- e. Stability
- f. Asymmetry effects
- g. Wind sensitivity
- h. Mussle blast sensitivity

The lift and drag coefficients are functions of projectile shape and airupeed. Stability is primarily a function of shape, airupeed, air density, and spin rate, and of the manner in which the mean of the projectile is distributed. Muzzle blast sensitivity depends on ementially the same parameters as stability. Wind sensitivity depends on the lift and drag coefficients, on stability, and, in the case of rocket-amisted projectiles, on the ratio of thrust to drag. Practically all projectile bodies (and first) are designed with rotational symmetry; their asymmetry arises in the manufacturing process. Funn, however, are usually asymmetric internally; the center of gravity of the fune does not he in the projectile axin.

All of the above accordary flight characteristim, and therefore the primary flight characteristics, are controllable by the designer to within a narrow range; round to round variations arise owing to manufacturing tolerances and to changes in measle velocity, air density and wind patters. Stringent manufacturing tolerances may be imposed by the designer if the assuracy improvement obtained can justify the increased cost of manufacture.

I-I. LOGISTICAL CONSIDERATIONS

This above extrement leads into the area of legistics. The designer court countantly beer in

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mind the elements of cost, storability, and transportability. He should avoid, where possible, the use of materials likely to be in short supply during wartime. He will often be limited by the facilities for loading the projectile into the gun, and by the design of the gun chamber. Most of these considerations are beyond the scope of this particular handbook, but are covered in other design handbooks of this series.

It is not difficult to design a projectile having long range, a relatively short time of flight, and a small round-to-round dispersion. However, the projectile might, and probably would, have such a small destructive value, or lethality, that it would be uncleas as a weapon. THE PRIME FUNCTION OF THE PROJECTILE DESIGNER IS TO FIND THAT COMPROMISE AMONG RANGE, ACCURACY AND LETHALITY WHICH WILL BEST SUPPORT THE MISSION OF THE WEAPON SYSTEM UNDER CONSIDERA-TION.

For example, modification of an existing pro-

jectile by increasing the length of its ogive, while preserving the overall length of its ogive, while should decrease its drag coefficient and, therefore, increase its range. However, the stability of the round will be altered, with some effect on accuracy; the volume of the projectile will be decreased, with resulting decrease in lethality (or other measure of usefulness, as in the case of smoke or illuminating projectiles). These trade-offs are discussed in detail in the body of this kandbook.

In most of the discussions in this handbook it will be tacitly assumed that the designer is given the projectile diameter and the characteristics of the gun from which it is to be fired, i.e., upper limits, on chamber pressure, muscle energy and muscle momentum have been established by the gun designer. Occasionally, but not often, the projectile designer may be able to specify the twist of the rifling. If the designer is equipped to make correct design decisions for any one caliber, he will be able to cope with the problem of choosing an optimum caliber for a given mission, should that problem arise.

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CHAPTER 2 TRADE-OFFS

2-1. GEFERAL

If the solution of a trade-off problem is expressed in numbers, an intelligent compromise between conflicting goals can only be reacted when the cost of falling short of each goal can be expressed in numbers. Furthermore, these penalty sumbers must be in the same system, i.e., they must be expable of being added or multiplied together to give a significant number.

One useful concept, horrowed from economics, is that of "utility", expressed as a number which lies between zero, standing for uselsm, and unity, standing for maximum usefulness attainable in the given situation. If the utility of each element of a situation can be computed, the utility of the overall situation can be found by multiplying, or. in some cases, adding, the utilities of the elements. (The sum may be divided by the number of components if the envestion that utility cannot encouponents if the envestion that utility cannot encou-

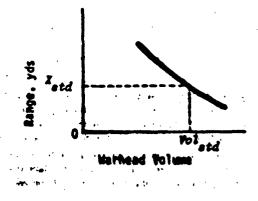
In order to construct the curves which express the utilities of the various elements of projectile performance, the dasigner must obtain, from the agency responsible for defining the military requireont, statements shout the relative values of weris of different volumes for the purposes, and at it ranges, pertiment to the mission of the prointile. Similar statements want be obtained about the metalnons of increased range, destruced time of flight, and improved assuracy. While the statements obtained may be mainly evaluative, such as "we can stand a little reduction in warhard volume, but a 50% reduction would be unacceptable," w anything than twice the present range is d to be beyond the min ion of this proetile." they can be translated into sur

utility curves. The designer should discuss the utility curves with the coustomer before proceeding with the design; some clarification of design objectives is likely to result. Reamples of tradeoff are given below.

2-2. INCREASED RANGE VS WARHEAD VOLUME

2-2.1 Utility of Standard Projectile Assumed Repui to Zero for Standard Range

As an emaple, suppose that the problem is the design of a rector-assisted projectile to be firefrom an existing gun. Range is increased by the addition of rocket fuel; however, the overall length of the projectile is limited by stability or handling considerations, so that as the amount of rocket fuel is increased, the volume of the warhead, and therefore its lethality, is decreased. The designer can compute the trade-off curve of range vs warhead volume, and fit this curve with a simple algebraic expression. For example, the curve might be an above below.





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Here X_{red} and Vol_{set} represent the range and warhead volume, respectively, of the standard projectile fired from the given gun. The design problem is to increase the range above X_{ret} without merificing "too much" warhead volume. The remation for the curve above would be:

$$\frac{X - X_{out}}{X_{out}} = \frac{Val_{out}}{Val} - 1, \text{ or }$$

replacing the fractions by symbols :

$$S = \frac{1}{R} - 1 = \frac{1 - R}{R}$$

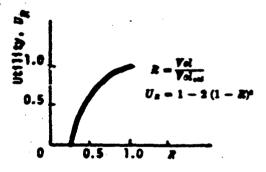
- I.u I.u

there -

and
$$R = \frac{Val}{Val}$$

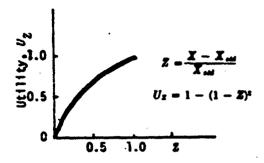
This equation might fit the curve well only over the range $\frac{1}{2} < R \leq 1$, but it will term out that in this example we are not interested in solutions outside of this range.

Suppose that an examination of the user's preferences has antablished the two utility enrors shown below:



This ensure shows that the utility of the warhood dealines at first showly with decreasing volume, then precipitonsly, and that volumes less than 0.3 the standard volume are worthless, i.e., $T_{\rm o} = 0$.

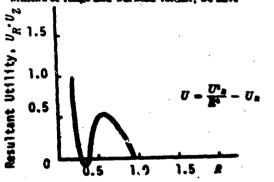
The following curve above that any range lying between the standard range and twice standard range is of interval, and that the rate of increase of range usefulness approaches zero as the range approaches the upper limit.



Since we know the relation between S and R, we can express U_S in terms of Σ ,

$$U_{\mathcal{E}} = 1 - \left(\frac{1}{\mathcal{E}} - 2\right)^2 = \frac{U_{\mathcal{E}}}{\mathcal{E}^2} - 1$$

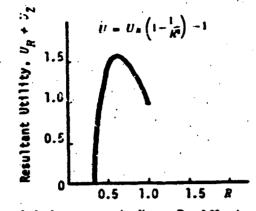
On the assumption that the utility of the compromise solution is proportional to the product of the utilities of range and warhoad volume, we have



There is no interest below R = 0.5 and the best compromise lies at R = 0.64, where U = 0.00, and $X = 1.55 X_{co}$. The solution may be reached by either graphical or analytical methods. Note that the resultant utility of the standard projectile is zero by this oritorion.

2-2.2 Utility of Standard Projectile Assumed Equal to Unity for Standard Range

If it should be thought more realistic to give the standard projectile a resultant utility of ene, then we might deside to add utilities to find the resultant. In this case



and the best compromise lies at R = 0.00, where U = 1.58, and $X = 1.67 X_{obs}$. The resultant stilling of the standard projectile being 1.0 by the criterion, we have an estimate of the increase in unfulness gained by going to the rocket-assisted projectile, viz. 58%.

2-2.3 Comparison of Results for Utility Equal to Zero and Utility Equal to Unity

In our examples it does not make much difference which criterion we use, however, this will not always be the case. In general, it can be said that the use of the additive criterion places the optimum at the point where the sum of the slopes of the utility curves is zero. In the multiplicative method each slope is multiplied by the product of the other utilities before being summed to zero. After leasting the area of optimum solutions, the final solution will be pispointed only by conmiderations of accuracy, time-of-flight, and legistics.

2-3. TABULATION OF POSSIBLE TRADE-OFFS

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Design changes which increase accuracy sometimes decrease range; range and accuracy might both be improved by increasing the cost of manufacturing the round. The trade-off method outlined above can be useful in these and similar situations.

Many different trade-off situations are mentioned in the Caromions in this handbook. For example:

- a. Computing time for accuracy of simulation in trajectory calculations.
- b. Warhend volume for abort time-of-flight by use of a subcaliber projectile.
- c. Range or time-of-flight for accuracy where improved stability may be obtained by employing a high drag configuration.
- d. Warbend volume for range or time-of-flight by boattailing, or by lengthening the ogive. Unfortunately, increasing range usually diminishes the unefulness of even an undiminished warbend by increasing the dispersion (in meters) at the target.
- e. Drag for manufacturing cost in the choice of in prefile.
- f. Range or time-of-flight in reduced storage and handling space in the case of a spikenessed round.
- g. Simplicity for warhead volume by using folding fits.

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CHAPTER 3

AERODYNAMIC COEFFICIENTS

3-1. GENERAL

A large part of this handbook is concerned with the interactions between a projectile and the air through which it flies. Frequent use is made of the fact that many aspects of this interaction are independent of which of the two, projectile or air, is actually moving; their relative velocity is the significant quantity. The basic characteristics of the flow of a fluid, such as air, around a body are described in Poundations of Aerodynamics by Kuethe and Schetzer, and in Physical Principles of Mechanics and Acoustics by Pohl, which present many interesting drawings and photographs of the flow of finide, using dye or reflecting Tarticles to make the motion visible. The Bibliography at the end of this handbook lists these and other books on acredynamic theory.

3-2. BODY ARRODYNAMICS

A projectile fiying through the als creates vertexes, turbulence and, if its speed is sufficiently great, shock waves in the air. Both the air and the projectile are heated. The energy content of these motions is supplied by the kinetic energy of the projectile, and this transfer of energy implies a force, or force system, between the air and the projectile. This force system may be analyzed into components which produce changes in the linear and angular velocities associated with each of the three orthogonal axes which may be chosen as a coordinate system for the description of the motion of the projectile.

3-2.1 Coordinate System

The coordinate system employed in this handbook. Figure 3-3, for describing the forces and moments acting on a projectile has its origin at the center of gravity (e.g.) of the projectile, its X-axis pointing in the direction of the tangent to the trajectory (note that this direction changes as the projectile moves along the trajectory) and its Yand Z-axes in a plane normal 20 the X-axis. The Y-axis is horizontal; the Z-axis is normal to the other two.

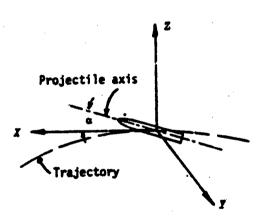


Figure 3-1. Coordinate System

Many different coordinate systems are employed by writers on projectile serodynamics, the obsice of a system being influenced by case of development of the mathematics involved. However, nearly all of these systems agree in having the origin at the center of gravity of the projectile since the motion of a body can always be received into

translation of, and relation about, its center of gravity.

3-2.2 Yaw

The aerodynamic forces are functions of the attitude of the projectile with respect to the direction of motion of the e.g. relative to the surrounding air. If there is no wind, this direction of relative motion is along the tangent to the trajectory. (Since wind velocities are small compared with projectile velocities, wind effects are usually introduced as corrections.) Yaw is defined as the angle between the tangent to the trajectory and the direction of the longitudinal axis of the projectile. This angle varies continuously throughout the flight, rapidly at first, but, in a well behaved projectile, less rapidly as time goes on; spinstabilized projectiles should quiet down to a nearly constant yaw, called the yaw of repose, while the yaw of fin-stabilized projectiles should damp to very small values. In mathematical analyses, the position of the projectile axis is usually projected onto the Y, Z-plane, giving a horizontal and a "vertical" component of yaw. These components are related to the yaw by the cosine and sine of the yaw orientation angle, and are usually handlond mathematically by the use of complex numbers.

3-2.3 Conter of Pressure

The acrodynamic forces on a projectile are determined by the pressure distribution which exists over the whole exterior surface, but in order to simplify the measurement and mathematical manipulation of these forces, we deal only with a specified set of the resultants of the distributed forces. These resultants have a magnitude and direction, and also a point of application on the body, i.e., a point through which the resultant acta. This point, called the center of pressure (e.p.) of the force in question, is assumed to lie in the longitudinal axis of the projectile, but its position on that axis depends on the shape of the projectile, its six-opeed (Mach number), axial spin rate, and, unfortwastely, sometimes on the magnitude of the magnitude of the

In this handbook, the center of pressure of the lift forces is assumed to be independent of yow angle; this is made possible by considering only "linear" projectile behavior in which the yaw seldom exceeds 10°. One purpose of good design is to keep the yaw well below this figure; not greater than 5°. However, the center of pressure of the magnus forces can move an appreciable distance when the yaw angle changes as much as 10°, and some attempt to describe the effects of this e.p. movement will be made.

3-3. AERODYNAMICS FORCES AND MOMENTS

3-3.1 General

The (resultant) forces and moments which are significant for projectile design are:

- a. Normal force
- b. Lift
- e. Drag
- d. Maxnus force
- e. Static moment
- f. Damping moment
- g. Magnus moment
- h. Roll damping moment

3-3.2 Lift and Drag

The resultant of the pressure forces on a symmetrical nonspinning projectile lies in the plane containing the tangent to the trajectory and the longitudinal axis of the projectile, called the "yaw plane"; the point on the projectile axis through which this resultant passes is called the center of pressure of the lift or normal force, since the resultant may be resolved either into lift and drag components, or into normal force and axial drag. Lift is parallel to the Y, Z-plane, drag is parallel to the X-axis; sormal force is perpendicular to, and axial drag is in line with, the axis of the projectile. Each possible pair of components lies, of course, in the yaw plane.

3-3.3. Magnus Force

When a projectile is spinning about its longitudinal axis, the pressure distribution over its surface is altered so that the resultant force no longer lies in the plane of yow. The nerodynamicist tubes care of this situation by introducing a force component normal to the yow plane, together with its

associated moment. This force, called the "magnus force", is also perpendicular to the longitudinal axis of the projectile, and passes through its own center of pressure. Vector subtraction of the magnus force from the total force on the projectile leaves a force in the yaw plane, which can be resolved into lift and drag.

3-3.4 Static Moment

The static moment is the product of the normal force and the distance between its c.p. and the c.g. of the projectile, which is considered positive when the c.p. is forward of the c.g. as it practically always is for spin-stabilized projectiles. The axis of this moment is a transverse axis through the c.g., normal to the yaw plane. Fin-stabilized projectiles have the c.p. aft of the c.g., so that the static moment opposes an increase in yaw (in normal flight), and can be called a "restoring moment".

3-3.5 Damping Moment

When the yaw of the projectile is changing, the swinging of the projectile about its e.g. changes the pressure distribution so as to produce a couple about an axis through the e.g. normal to the plane of the yawing velocity (which is not necessarily the plane of yaw). This couple, called the "damping moment", usually opposes the yawing velocity.

3-3.6 Magpus Memout

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The magnus force produces a moment about an axis through the e.g. parallel to the normal force. This magnus moment changes the yawing velocity in a way which depends on the location of the center of pressure of the magnus force, and on its direction. The magnus force and moment are a result of spinning the projectile, and are absent on a nonrutating projectile; however, even fin-stabilized projectiles may have spin.

3-3.7 Roll Damping Moment

The roll damping moment is a couple about the longitudinal axis of the projectile; this moment on a spinning body is related to the friction he-

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tween projectile and air. Fins produce large roll damping moments owing to the angle of attack induced by spin.

3-4. FORCE AND MOMENT COEFFICIENTS

It has been found that the aerodynamic forces and the static moment are proportional to the dimensions of the projectile, to the dynamic pressure of the air, and to the yaw of the projectile. The three moments arising from rotations are also proportional to their appropriate angular velocities. The factors of proportionality are known as "aerodynamic coefficients". They are not constant for a given projectile, but are themselves functions of Mach number, Reynolds number, spin rate, and yaw. A brief discussion of the force and moment coefficients follows. For a more complete discussion of the aerodynamic forces and moments are Murphy, The Free Flight Motion of Symmetric Missiles, Ref. 12a.

3-4.1 Aerodynamic Force Coefficients

The most significant of the aerodynamic force coefficients are defined as follows; where

is the dynamic pressure, $\mathcal{S} = \frac{\pi}{4} d^2$ is the frontal area of the projectile, and a is the yaw in radians:

| <u> </u> | $\rho = \operatorname{air density}, \operatorname{slug}/ft^4$ |
|--|---|
| $C_{H} = \frac{N}{qS}$ | V == speed of projectile rel- |
| | ative to air, ft/ase |
| $C_L = \frac{L}{qS}$ | p == roll rate, rad/sec |
| , I. | d == maximum body diam- |
| $C_{\mathbf{p}} = \frac{D}{\mathbf{q}\mathbf{S}}$ | eter of projectile, ft |
| | N == normal force, lb |
| C. N. | $L = \operatorname{lif}$, lb |
| $C_{H_{p}} = \frac{N_{p}}{qS} \left(\frac{pd}{T}\right)$ | D = drag, lb |
| · (7) | N _p = magnus force |

All of these coefficients are expected to be functions of the yaw angle, a. For small angles (a < 0.17 radian), all, except C_D , can be assumed to vary linearly with yow; this leads to the use of the aloge of the surve of coefficient versus yaw angle as a more convenient description of the observativities of the projectile. Using the subscript a, to denote a derivative with report to a, we can write:

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$$N = \frac{dC_H}{da} gSa = C_{N_0} gSa$$

$$L = \frac{dC_L}{da} gSa = C_{L_0} gSa$$

$$N_{\mu} = \frac{dC_{N_0}}{da} gS\left(\frac{pd}{V}\right) \beta = C_{N_{\mu\nu}} gS\left(\frac{pd}{V}\right) \beta^{\circ}$$

Drag varies with the square of the yaw, so we write

$$D = (C_{P_{A}} + C_{P_{A}}) qS$$

where $C_{B,a}$ is the drag coefficient at zero yaw and $C_{B,a}$ is the rate of change of C_B with a^3 .

3.4.2 Moment Coefficients and Moments

The moments produced by the acrodynamic forces are referred to the center of gravity of the projectile, unless otherwise stated. The moment coefficients, in the terminology of this handbook, are derivatives with respect to yaw, or with respect to appropriate angular velocities.

3-4.2.1 Moment Coefficients

These coefficients are defined as follows:

$$\frac{dC_{M}}{da} = C_{M_{a}} = \text{static moment coefficient}$$

$$\frac{1}{\frac{1}{20} \frac{\partial M_{2}}{\partial G}} \left(\frac{\partial M_{2}}{\partial (\frac{\partial M_{2}}{V})} + \frac{\partial M_{2}}{\partial (\frac{\partial M_{2}}{V})} \right) = C_{M_{a}} - C_{M_{a}},$$

damping moment coefficient

 $\frac{dC_{Hp}}{ds} = C_{Hps} = \text{magnus moment coefficient}$

3-4.2.2 M., Moment About Horizonta' Azis

The total moment about a horizontal axis, through the e.g. is given by

$$M_{\bullet} = \frac{dC_{H}}{da} \exp Da + \frac{\partial M_{+}}{\partial \left(\frac{\partial A}{V}\right)} \left(\frac{\partial A}{\partial V}\right) + \frac{\partial M_{+}}{\partial \left(\frac{\partial A}{V}\right)} \left(\frac{\partial A}{\partial V}\right) + \frac{dC_{H}}{da} \left(\frac{\partial A}{V}\right) \exp \left(\frac{\partial A}{\partial V}\right) + \frac{dC_{H}}{da} \left(\frac{\partial A}{V}\right) \exp \left(\frac{\partial A}{\partial V}\right) + \frac{\partial A}{\partial a} \left(\frac{\partial A}{V}\right) + \frac{\partial A}{$$

where q in the second term is the angular velocity about the hovincetal axis when a, the yawing veloc-

"Many the magnes force in the S direction is propertional to the year in the Y direction. See paragraph 3-43. ity about that axis, is zero; i.e., the total angular velocity about the horizontal axis is $q + \dot{a}$. q arises from the curvature of the trajectory. Therefore, in coefficient form

$$M_{\tau} = \frac{1}{2} \rho V^{2} \operatorname{Sel} \left[C_{H_{0}E} + C_{H_{0}} \left(\frac{\rho d}{V} \right) + C_{H_{0}} \left(\frac{\delta d}{V} \right) \right. \\ \left. + C_{H_{p_{0}}} \left(\frac{p d}{V} \right) \beta \right]$$

The first term of the expansion is the static moment, the next two are the damping moments, and the last term is the magnus moment. (Note the each term inside the brackets must be multiplied by $\frac{1}{2} = V^2 R d$

to obtain the moment.)

3-4.2.3 Mr. Moment About Vertical Aris

M, the aerodynamic moment about the "vertical" axis through the e.g., is obtained by a similar expansion, interchanging a and β , substituting $\dot{\beta}$ for $\dot{\alpha}$, and τ for q, where $\tau + \dot{\beta}$ is the angular velocity about the s-axis.

3-4.2.4 Mr. Moment About Longitudinal Axis

The acrodynamic moment about the longitudinal axis of the projectile is, in the absence of a spininducing torque such as might be provided by canted fine, simply

$$M_{\bullet} = C_{i_{0}} \operatorname{qSd} \left(\frac{\mathcal{P}_{i}}{\mathcal{T}} \right)$$

and C_{t_p} is called the roll damping moment coefficient. The dimensionless ratio pd/V which appears above is aften designated by s_i the spin in radians per caliber.

3-4.2.5 Relationship Between Ballistic and Accodynamic Systems of Coefficients

The earlier work in this area uses a system of coefficients within which ρV^2 takes the place of the dynamic pressure, and d² takes the place of the frontal area. This system is, of course, dimensionally correct. It was the system used in AMCP 706-246, Engineering Dasign Handbook, Ammunition Series, Section 3, Design for Control of Flight Characteristics, and is discarded here in the interest of unifying the notation of aerodynemicists and hallisticians, since the latter are forced to use

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a large amount of wind tunnel data obtained by aerodynamicists.

The ballistic notation will be around for a long time, so it is necessary to know that coefficients in the ballistic system (which are usually denoted by the capital letter K with a subscript) can be converted into the corresponding aerodynamic coefficient slopes (or directly into those coefficients which are not functions of yaw) by multiplying the

ballistic syst.m coefficient by $8/\pi$, e.g., $C_{N_{\alpha}} = \frac{8}{\pi}K_N$. For example,

$$N = C_{H_{\alpha}} \left(\frac{1}{2} \rho V^2 \frac{\pi}{4} d^2 \right) \alpha = K_{\mathcal{H}} \left(\rho V^2 d^2 \right) \sin \alpha$$

When $\sin \alpha = \alpha$, $C_{H_{\alpha}} = \frac{8}{\pi} K_N$ by cancellation. It should be noted that for C_{l_p} , $C_{M_q} + C_{M_{\alpha}}$, and $C_{M_{pn}}$ the multiplier is $-\frac{8}{\pi}$. (Some authors use $-\frac{16}{\pi}$ as a multiplier, since they use 2V as the

denominator of their spin terms, e.g., pd/2V instead of yd/V.)

3-4.3 Complex Yaw

In the foregoing discussion, for the sake of simplicity, the symbol α was used for yaw angle. In the notation of Ref. 12a, α is the component of the yaw angle in the "vertical" direction; the component in the horizontal direction is β , and the total yaw angle, δ , is given by

where the orientation of the yaw is $\tan^{-1} \frac{a}{a}$.

The aerodynamic coefficient slopes, or "aerodynamic derivatives", can be defined in terms of a because of the rotational symmetry of a projectile; their values can be derived from measurements made on a model which is given a yaw in one plane, identified as the e-plane. (See McShane, Kelley and Rene, Exterior Ballistics, Ref. 7.)

3-4.4 Magnus Moment Sign Convention

If the projectile is viewed from the front, β is positive to the right and σ is positive upward. A projectile with righthand spin (counter-clock-wise when looking from the front) experiences a magnus force downward when β is positive. If the center of pressure of this magnus force is aft of the e.g. of the projectile, then the magnus moment is positive since it adds to the static moment produced by positive a and $C_{M_{e^*}}$. In the study of the effect of e.g. position on the aerodynamic properties of the A-N spinner (Ref. 49), it will be seen that $C_{M_{pos}}$ increases as the e.g. moves forward.

3-5. METHODS OF MEASURING TH.* COEFFICIENTS

3-5.1 General

In order to be able to predict the performance of a proposed design, a good bit must be known about the probable pattern of the air flow over the projectile in flight. This air flow is mathematically described by the aerodynamic coefficients, so these must be measured or estimated. Estimation, by methods referred to below, is adounate in the preliminary design stages; however, if the coefficients are not well established before prototype rounds are manufactured, the designer runs a great risk of a totally unacceptable performance when the first test firings are made. Furthermore, the process of maximizing one desirable characteristic, such as lethality, which involves reducing other performance characteristics, such as stability, to their minimum acceptable values can not be intelligently carried out if the principal acrodynamic coefficients are not known to a close approximation.

3-5.2 Methods of Measurement

Two methods are in common use for the measu rement of coefficients, both of which yield values which are adequate to permit confident design compromises. That is, they yield not only sufficiently accurate values of the coefficients of the design being tested, but also good estimates of the changes in those coefficients which would result from small changes in the design. The two methods are:

a. Ballistic range testing

b. Wind tunnel testing

The method chosen in a particular case may depend on the technical considerations listed be-



2.5

low; if not, it depends on factors of time and cost. Major considerations are the availability of the range or the tunnel, and the speed with which the necessary data reduction can be performed at the available facility because costs are usually not widely different.

Estimated accuracy of aerodynamic coefficients obtained by ballistic range and wind tunnel tests is shown in Table 3—1.

3-5.3 Factors to be Considered in Selection of Method

The conditions and objectives of the test should be thoroughly discussed with personnel of the facility chosen before any work is started on test models or prototypes. However, to assist the designer in the preliminary discussion, significant differences between the two methods of testing are described below.

3-5.3.1 Free Flight (Bullistic Range)

- a. Good control of Mach number, velocity, temperature, and pressures.
- b. Little control of modul attitude.
- e. Model must be statically or gyroscopically stable.
- d. No strut to interfere with base flow.
- e. One test covers a range of Mach numbers.
- f. Data obtained from shadowgraphs, photographs, and yaw cards, with the possibility of telemetering some data.
- g. Data reduction is complicated.
- h. Models usually full scale.
- i. Reynolds number can be varied by varying model size.

3-6.3.2 Wind Tunnel

- a. Excellent control of Mach number, velocity, temperature, and pressures.
- b. Excellent control of model attitude.
- e. Can obtain data on both stable and unstable configurations.
- d. Model support may interfere with base flow.
- e. Only one Mach number per tast.
- Data obtained from force and moment halances, pressure taps, schlieren photographs or shadowgraphs.

- g. Data reduction is simple.
- h. Models usually reduced in size.
- i. Reynolds number can be varied by varying tunnel pressure (it may not be possible to test at free-flight Reynolds number).

3-5.4 Data Resulting from Ballistic Range Tests

For a test of this type a projectile is manufactured in accordance with the preliminary design drawings; if length or diameter is too great, a geometrically scaled model with a proper mass distribution may be made. The projectile is fired along a nearly flat trajectory in a suitably instrumented building. For a description of such a range, its instrumentation and method of operation, see Ballistic Research Laboratories Report 1044 (Ref. 13). (The U.S. Army Ballistic Research Laboratories at Aberdeen Proving Ground, Maryland, will be hereinafter referred to by the initials BRL.) The designer should be familiar with the capabilities of BRL, as this installation can be of major assistance to him in any design problem.

As the projectile flies along the instrumented range, a number of parameters of its motion are very carefully measured at successive stations along the range. They are

- A. Velocity
- b. Boll rate
- e. Yaw angle
- d. Yaw orientation
- e. Swerving motion

From the position versus time (velocity) data, the deceleration of the projectile can be inferred. Knowing the mass and diameter of the projectile, and having observed the current values of barometric pressure, temperature, and humidity; we are able to compute the drug and drag coefficient, C_p . Repeat firings at the same velocity can give the variation of C_p with yew angle (squared), and sets of firings at different mumble velocities will give the variation of C_p with Mach number. If the projectile is rechet-amisted, test firings with reaket ignition will give not thrust.

All of the coefficients listed above can be determined in a ballistic range, except that G_{H_q} and G_{H_q} are always determined as a sum. The yawing frequencies and the damping are deter-

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| | | Entimated Maximum Broot in Percen | | |
|--------------------------|---------------------|-----------------------------------|-------------|--|
| | Carfficient | Ballistic Range | Wind Tunnel | |
| C _D | Drag | ± 0.5 | ± 2. | |
| C _L | Lift | ± 5. | ± 1. | |
| C _M | Statie moment | ± 2. | ± 1. | |
| $C_{M_q} + C_{M_{\Phi}}$ | Damping moment | ±10. | ± 10. | |
| C _{Mpa} | Magnus moment | ±15. | ± 10. | |
| C1, | Roll damping moment | ± 1. | ± 1. | |
| c.pc.g. | · Separation | ± .10 cal | ± 0.10 cm | |
| C _{H pe} | Magnus force | ±25 | ±10 | |

TABLE 3---1 ESTIMATED ACCURACY OF AERODYNAMIC COEFFICIENTS OBTAINED BY BALLISTIC RANGE AND WIND TUNNEL TESTS

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•Maximum error equals 3 std. deviations

mined early in the process of the reduction of the data, and indeed the dynamic stability of the projectile at various Mach numbers can be directly observed. Dynamic instability may be catastrophically apparent; observation of the projectile in a free flight condition is one of the major advantages of testing in a ballistic range. If it is desired to assess the effects of varying initial roll rate, this may be accomplished if suitable gun tubes are available. Usually, however, the designer does not have roll rate at his disposal because even if the projectile is not designed to fit an existing gun, rotating band strength or tube wear usually puts a limit on the allowable spin rate.

Coefficients of typical projectiles, determined in a bullistic range, with estimates of their accuracy, are given in Table 3-2, and in the Aerodynamic Data Sheeta, Appendixes VIII-A through VIII-Z. A list of the ballistic ranges in North America which are usually used for projectile testing appears in Table 3-3.

3-5.5 Data Resulting from Wind Tunnel Tests

A test of this type is usually made on scaled models having the exterior configuration of the projectile's preliminary design. The interior of the model is hollow and contains suitable provisions for mounting the model on a sting or strut which in turn is supported by a structure attached to a stationary portion of the wind tunnel. If the model is to spin, the internal provisions include bearings and often a drive motor. Internal strain gage balances are generally used to measure the aerodynamic forces and moments.

All of the aerodynamic coefficients previously discussed can be determined in wind tunnel tests. $C_{H_{\phi}}$ and $C_{H_{\phi}}$ can be determined separately if desired. Very accurate determinations can be made if the need for such accuracy justifies the cost.

Coefficients of a typical projectile, determined in a tunnel, with estimates of their accuracy, are given in Appendix VIII-Y.

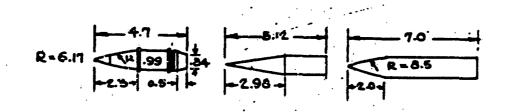
3-5.6 Test Facilities

A partial list of ballistic ranges and wind tunnels in North America which are suitable for artillery projectile model testing appears in Table 3-3 and Table 3-4, respectively.

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TABLE 3-2 COEFFICIENTS OF TYPICAL PROJECTILES MEASURED IN FREE FLIGHT AND ESTIMATED



| Identification: | | <u>105-mm M1</u> | Come-Cylinder | 7-Cal A-N Spinner |
|-----------------------------|--------------|----------------------------|---------------|--------------------|
| $C_{P_{*}}$ (peak value) | | 0.40±.01 | 0.41±0.01 | $0.46 \pm .01$ |
| Constants | (= | 1.54 | 1.52 | 1.50 |
| in Q function | { Ъ | 0.22 | 0.20 | 0.25 |
| (See par. 4-7.7.1) | le | .2.70 | 2.50 | 2.60 |
| Range of validity | | 1.1≤ M ≤2.5 | 1.2≤₩≤3.2 | 1.1≤ M ≤2.6 |
| $C_{D_{\delta}^{\pm}}(avg)$ | | 6.0 | 7.0 | 8.0 |
| Coefficients at M = 1.5 | : determined | by free flight measurement | . . | |
| C | | 2.3±0.2 | 2.6 ± 0.1 | 2.65±0.15 |
| c.p. (cal. from base) | | 3.45±0.2 | 2.7±0.1 | 5.4±0.1 |

| orby (same stores perio) | A1.20 T A19 | a T | A+# 7 A+ 7 |
|-----------------------------------|---------------------------|-----------|-------------|
| e.g. (cal. from base) | 1.75 | 1.65 | 2,95 |
| Cz. | 3.9±0.1 | 2.75±0.06 | 6.2±0.06 |
| $C_{H_q} + C_{H_q}$ | -7±1 | -9 | -26±0.5 |
| Carpa | 0.03±0.05 | 0.25 | 0.40±.08 |
| Cy | | | -0.19± .001 |
| Coefficients at M = 1.3: estimate | d by Simmons-Wood methods | | • |
| Cr. | 2.40 | 2.80 | 2.80 |
| e.p. (oal. from base) | 3.10 | 2.00 | 4.90 |
| C _{Ma} | 3.25 | 2.65 | 5.40 |
| | | | |

3-6. METHODS OF ESTIMATING THE CORFFICIENTS

Since it is wasteful to construct a projectile or projectile model for range or wind tunnel test which has no chance of success, and which may even destroy walls or instrumentation of the ballistic range when fired, it is necessary to make preliminary estimates of the principal aerodynamic coefficients before testing. The methods of making such estimates are given in the list of reports, Table

3.8

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TABLE 3-3 PARTIAL LIST OF BALLISTIC TEST RANGES IN NORTH AMERICA

| Location | Keference | Commoni |
|--|---|--|
| Ballistic Research Laboratories Aberdeen Proving Ground Maryland | Ref. 19 BRL Report 1048, W. Braun | Two ranges. Projectiles up to 8 inches max. diameter |
| Naval Ordnance Laboratory Whate Oak, Maryland | NAVORD 4063 | Three ranges, two pressurised |
| NASA Ames Research Center Moffett Field, California | NACA Report 1222 | Several ranges |
| Canadian Armamont Research and Development Establishment Quebec City, Canada | Canadian Asro- neutical Journal, May 1956 | Large range |

TABLE 3-4 PARTIAL LIST OF WIND TUNNELS IN NORTH AMERICA*

| Location | Bynipment | Mash Number Range |
|---|---|---|
| Arnold Engineering Development Center (/EDC) Arnold Air Porce Station, Tennemee | Two presence tunnile Three seconomic Three hypersonic | 0.5-1.6 1.5-6 5-6, 10, 12 |
| Ballistic Remarch Laboratorics Abordeen Proving Ground, Maryland | Two supervasie tunnels One hyportonie | 1.28-6 6, 7.8, 9.2 |
| NASA Amer Bernarch Center Moffett Fuid, California | Three extenses tunnels Four transmis Four expenses Beven hypertense | 9-1.0 0-2.2 0.65-0.15 5-30, 25, 35 |
| NASA Longery Remarch Conter Longery Field, Virginia | Three extensis tunnels Right transmis Six experience Sixteen hyperenic | 0-0.6 0-1.4 1.25-7 2-36 |
| NABA Lowie Research Carter Cirveland 25, Okee | One subsonie tunnel One transcase Broon supervene One hyperusec | 0-0.46 0.8-3.1 1.3-6 7 |
| Naval Ordnance Loberatory White Oak, Maryland | Pour trisonie tanach Oto hypertone | 0.3-8 8-8, 10 |

"This hat is in-raded to instands only desilition which do a in-yea convent of projectile testing. Not ()) of it's tunnels belief are used for projectile work. Some tensors appear more than easy in the bot. More information about them and many other what instants will be found in the *MATIONAL WIND TOWNEL SOMMART*, 1961, propared by the Astrotastics and Astronomics Constitution Beard, Department of Defenge.

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| Quentity | References | Comment |
|----------------------------------|---|---|
| Cr. and Cr. | Simmons (Ref. 20) Hitchcock (Ref. 81) Wood (Ref. 21) Kelly (Ref. 16) | Not readily available · Limited range of usefulness Based on Simmons; used in this handbook (See Appendix III-A) |
| C _{*+} + C _* | Hitchcock (Ref. 81) | Conventional spin-stabilized projectiles of length L $C_{N_{e}} + C_{N_{e}} = 0.9 \left(\frac{L}{d}\right)^{1.5}$ (fairly good for $3 < L < 5$) |
| | Dorrance (Ref. 15) | Reproduced in Murphy and Schmidt (Ref. 49) |
| C _{Kpe} | Martin (Ref. 40) Kelly (Raf. 39) | See also Ref. 49 |

TABLE 3-5 LIST OF REPORTS CONTAINING METHODS OF ESTIMATING COEFFICIENTS

3-5. Sample calculations are shown in the Appendixes.

These methods are fundamentally based on an interpolation of data from very many wind tunnel and ballistic range tests of a wide variety of projectile shapes. Use is made of linear aerodynamic theory in constructing formulas for performing the interpolations. While these formulas should of course not be used for shapes which his outside of the range of the data on which they are based, it may be necessary to use them for unusual ahapen when no other method of estimation is available. Such shapes should be tested in a wir^{*} tunnel; most ballistic range operators would ref to fire them.

Estimated coefficients of typical projectile shapes, for comparison with values obtained in ballistic range tests, are presented in Table 3-2.

CHAPTER 4

TRAJECTORY CALCULATIONS

4-1. GETERAL

The purpose of a calculation of a trajectory, the curve is space traced by the center of gravity of the projectile, is usually the prediction of the expected point of impact of the projectile, when fired at a given mumb velocity and quadrant elevation, along with the prediction of associated quantities such as time of flight, angle of fall, and velocity at impact. Sometimes the range is stated, and the purpose of the calculation is to find the corresponding mustle velocity and/or quadrant elevation; the three collisteral quantities are still of interest. Or the trajectory may be a ground-to-sir type, as for an antiaircraft projectile, for which maximum altitude, time to runch a given altitude, and trajectory envature are important runch.

4-2. DEFFRENTIAL CORFFICIENTS OR SEMIITIVITY FACTORS

One can, by varying the inputs to the trajectory colculation by small amounts, one at a time, compute the shange in expected range, time of flight, or other quantity of interest, second by a small change in each input parameter. The percent change in range (or other output quantity) produced by a 1% change in an input parameter is called by some writers a "differential coefficient", by others a "unmitivity factor." The factors are different for each design, so well as for different intervals of the values of the input parameters, which is why they must be determined by small perturbations and the particular act of conditions for which they are did must be stated. A sample set of sensitivity fastors for a realist-ansisted projectile fired for manimum range is given in Table 5-1.

4-3. DIGITAL COMPUTER PROGRAMS FOR TRAJECTORY CALCULATIONS

inaumerable trajectory calculations have been made, and are still being made, for the production of firing tables. Up to the advent and general adoption of the high speed digital computer, these calculations were performed by approximate metheds which employed average or effective values of the drag coefficient. The various methods were named for their developers, the Gavre Commission. Sineci, and Mayeveki among others. These methods are still useful for rapid estimations of the effects of variations in projectile shape, manile velocity and quadrant elevation on range and time of flight. The necessary charts and tables, with directions for their use, are given in AMCP 706-140 (Ref. 97). Digital computer programs fall into two classes, particle trajectories and siz-degree-of-freedom trajectories; each is discussed below.

4-3.1 Simple Particle Trajectory

The relatively simple particle trajectory program assumes that the only forces on the projectile are gravity, drag, and, if present, thrust. The horizontal and vertical associarations due to these forces are computed at successive points in time, and the resulting horizontal and vertical compensate of the projectile's velocity and position are computed for each time point. If the time interval is small enough, the simulation of the trajectory can be very good. With a time interval of 0.25 accord, the time required to simulate a typical trajectory on an IBM 1650 computer was about ton times the time of flight of the projectile being simulated. This resulted in an accuracy of

simulation better than 1%, assuming that the drag coefficient curve used averaged within 2% of the true C_B at all Mach numbers traversed. If no computation of yaw is made, C_{B_0} , the axile drag coefficient, is the coefficient used. Since projectile velocity and altitude are known at each time point, Mach number is always available for entering a stored table of C_{B_0} vs Mach number.

The particle trajectory is very useful in computing trade-offs of range, time of flight, and lethality, particularly in case of a rocket-assisted projectile. Extensions of the program to compute muzzle velocity under the limitations on muzzle energy and muzzle momentum, and then the meximum: set-back acceleration, can further axtymute the doing process.

4-3.2 Siz-Degree-of-Freedom Particle Traje-tery

The six-degree-of-freedom system is seldom coded for anything smaller than the equivalent of an IBM 704. This program computes the position and velocity of the projectile relative to all three axes of the coordinate system(s) chosen, as well as the pertinent angles and angular velocities. All of the aeroxiynamic coefficients can be used (although many second order terms are usually left out), and the resulting simulation of the trajectory is complete, down to yaw angle, yaw erientation, and surviving motion. Aerodynamic jump is an automatic by-product of this system. Wind can be introducerd as a variable.

If roll rate, C_{Ip} and the variation of C_{Ho} with Mach numler were included in the particle trajectory program, then either program could continuously check the gyrescopic stability of the projectile and calculate the yaw of repose. The nizdegree-of-freedom system could also continuously shock the dynamic stability of the projectile.

4-3.3 Emmple of Simple Particle Trajectory Calculation (FORTRAN Program)

The PORTRAN particle trajectory program presented below was written for an 1234 1630 computer with 20,000 units of memory. It will compute trajectories of conventional and single-stage rocket-assisted projectiles, either spin- or finstabilized, and single-stage rockets. The spin, yaw of repose, and gyroscopic stability computations do not allow for the presence of fin cant or noszle cant.

The limited memory available made it pecessary to read the headings for the output (see Table 4-1 for a sample output) from eards. Appendix IX describes the input eards forming the data deck; the numbers on the input cards describe the projectile and its launching environment. Heading eards are a part of the data deck and follow the numerical data, except that the first eard of the data deck identifies the projectile being processed.

An experienced programmer, or one having access to a computer having a larger memory, will be able to make many improvements in and extensions to the program presented here. For example, this program interpolates linearly in finding C_{B_0} or C_{B_0} from the tables provided by the data dock; it may be difficulty to represent a given curve sufficiently well with only nine data points. Furthermore, while the computer will print out UNSTABLE when S_0 is less than unity, dynamic stability must be computed by hand.

A typical output produced by the program given helow is presented in Table 4-1. Projectile data are for the sample projectiles used to illustrate the methods of estimating gyroscopic stability (Appendizm I-VII).

The form factor relating the drug of the sample projectile to that of the 5-inch/54 Navy projectile stored in the computer memory was estimated to be 1.05 since the only significant difference in shape is the shorter ogive of the sample projectile. The form factor relating the static memorie coefficient of the sample projectile to the C_{H_0} table stored in memory was estimated to be 1.142, based on the Wood-Simmon estimate at H = 1.72.

The last line of the computer output gives the time of flight in accords, the range in motors, the velocity at impact, angle of fall, and the spin and gyraccopic stability factor at impact. The target is at the same elevation as the gun (sea level) in this example, but any desired target elevation can be fed with the data.

The fundamental equations underying the computer program presented below are:

$$\Delta V = \left(\frac{\text{Thrust} - \text{Drag}}{\text{Projectile Mass}} - g \sin \Theta\right) \Delta t$$
$$\Delta \Theta = \frac{-g \cos \Theta}{V} \Delta t$$
$$\Delta X = (V \cos \Theta) \Delta t$$
$$\Delta X = (V \cos \Theta) \Delta t$$

Averaging techniques are used to improve the accuracy of the simulation.

4-4. DESK COMPUTER METHOD FOR TRAJECTORY CALCULATION

Reference is made to Table 4-2 for the format of the desk computation. Note that the conditions, Θ_0 and V_{∞} appear in columns 2 and 5 in the first row. Starting with these initial craditions, we now proceed with the computation as follows:

- a. Compute the remaining ertries in first row.
- b. Proceed to next row: locate C_B on the drag curve of the projectile; calculate the drag, D, acceleration, D/m, where m is the projectile mass in slags.
- e. Compute:

(1)
$$\frac{dV_s}{dt} = -\frac{D\cos\Theta}{\pi}$$

(2) $\frac{dV_s}{dt} = -\frac{D\sin\Theta}{\pi}$

- d. Multiply the above derivatives, dV_{σ}/dt and dV_{σ}/dt , by the carrently chosen time interval. The results are ΔV_{σ} and ΔV_{σ} in the third results.
- e. Compute V, and V, at the end of the time interval (they appear in the fourth row) and use average velocities over the first time interval to compute Δx and Δz (third row) and the new x and z (fourth row).
- f. Compute the new V from $V = \sqrt{V_o^2 + V_o^2}$ determine Θ from $\Theta = \tan^{-1} V_o / V_o$; find one Θ and $\sin \Theta$; and complete the fourth row, using $\rho/\rho_0 = \exp \{-3.2 \times 10^{-3}e\}$ and $V_0 = 1116 - 0.004e$.
- g. Continue as above for remaining entries to complete the table.

-5. METHOD OF CALCULATING DIRECTION OF TANGENT TO TRAJECTORY

It may be of interest to discuss the equation used in the computer program for the calculation of the direction of the tangent to the trajectory at the end-of each time interval. In a particle trajectory, where lift and magnus force are neglected and drsg is assumed to act in line with the velocity vector, the only force acrisg to change the direction of motion is the weight of the projectile.

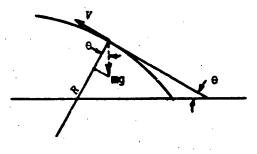


Figure 4-1. Diagram of Gravity Force on Projectile

The inertial force, or centrifugal force, arising from the curvature of the trajectory, is given by mV^3/R , where m is the projectile mass and R is the least radius of curvature of the trajectory. This is balanced (Figure 4-1) by the component of the projectile weight in the direction of the radius of curvature, mg ons Θ , as we can write

$$\frac{mV^{1}}{R} = -mq \cos \theta$$

But V/R is the time rate of change of the direction of the radius, and is therefore also the time rate of change of the direction of the trajectory tangent, since the tangent is always normal to the radius verter. Denoting the rate of change of direction by $d\theta/dt$, we have

or, as it appears in the computer program,

40 - - g ein 0; 44/V



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TABLE 4--1 TYPICAL OUTPUT OF FORTRAN SIMPLE PARTICLE TRAJECTORY PROGRAM

S-INCH SAMPLE PROJECTILE (SEE APPENDIX I)

| 1.050 1. | FM T1 142 5. VO | 19F RG | A RGT 81 1.93 SBT | 0.4 | 150 | ÚE . | • |
|---------------------------|--------------------------|----------------|-------------------------|----------------|---------------------------|----------------|----------------|
| 46.08 WTB | | TEMP | .0 | .400 | 28.00 4 | | |
| 46,08 | * | 59. | | | | 014 | |
| . 601189 | 1116.0 | | | • | | | |
| TINE THETA | X Z | DIST THRUST | V URAG | | CNA DR IACH SPI | | · · |
| 00 78 | • | | 1925.0 197.4 | | | 1:000 | 1:43 1.49 |
| .11 2.56 .75 | 3210. 3109. | 4469. | 1578.0 131.3 | . 362 .001 | | .905 .261 | 1:43 2,11 |
| 14 5.85 69 18 | 6682. 6188. | | 1265.9 84.1 | | 4,14 1,16 | .820 .311 | 1:43 3.03 |
| 10.38 58 | 10713. 9235. | 14166. | 993:0 34.3 | | 4.91 .92 | • 744 • 379 | 1.43 4.20 |
| .29 17:72 .34 | 16 400. 12203. | 20596; | 786.3 11.3 | .168 .010 | 4.32 | . 676 . 456 | 1.43 7.57 |
| 25.72 | 22088. 13269. | 26412. | 684.8 8.3 | .169 | 4.21 | 654 502 | 1.43 9.76 |
| 40 26,12 01 | 22361. 13267. | 26686; | 682;4 8,2 | .169 | 4.20 | -654 -503 | 1, 43 9, 80 |
| .40 34.12 38 | 27631. 12171. | 32099: • | 686.1 8.6 | .168 .014 | 4,20 | .677 .481 | 1.43 8,66 |
| .40 42.12 69 | 32522: 9173. | 37859. | 762.2 11.7 | .168 | 4.28 | -745 | 1.43 5.73 |
| .40 50:12 91 .40 | 37001. 4464. | 44371. | 866.5 18.1 | . 176 . 004 | 4.42 .78 | - 866 - 344 | 1.43 3.29 |

TINE, S RANCE, H V, FPS THETA, D SPIN S6 56, 13 12201. 929. -59.5 .303 2, 19

| TAB | TAB | TAB | TAB. —2 Ajectory C <iculated des<br="" on="">Ple projectile (see table 5- ctory using electronic com</iculated> | TAB | -2 TED ON DES E TABLE 5- TRONIC COM | 이 나무 | K COMP -1 FOR PUTER) | UTER Same | • | | |
|---|-------------------------------|-----------|--|----------------|--|---------|----------------------------|--------------|--------|----------------|------------------|
| | cos 8 atn 8 tps | , v A | | > [×] | >" | | ř. | 66 °. | 0, e | ~ | X (|
| | | | | | | ¥ | Δ× | 8 | | n | |
| | • 9986 • 0523 1925 1922 | 1925 1922 | 1922 | | 101 | | 0•0 | 0•0 | 1.0 | 1116 | 1.72 |
| -138 | -138 | -138 | -138 | | 66- | | | | 138 | 197 | .33 |
| -124 | -124 | -124 | -124 | | 5. | _ | 1674 | 26 | | | |
| | .9993 .0367 1799 1798 | 1799 1798 | 1798 | | 3 | | 1674 | 76 | • 998 | 1116 | 1.61 |
| ÷124 -3 | -124 | -124 | | | ņ | ~ | | (| 124 | 178 | .342 |
| - 11 - | - 17 - | - 17 - | - 17 | • | | ŝ | 251 | 0 | | | 1 |
| | .9994 . 0342 1782 1781 | 1782 1781 | 1781 | | | 61 2 | 1925 | 85 | . 997 | 1116 | 1.60 |
| | | | | | 1 1 | 0 | 1217 | 36 | 771 | C/1 | |
| 1.74 1.21 .9998 .0 212 1696 1696 | .9998 .0212 1696 1696 | 1696 1696 | 1696 | | | 36 | 3142 | 119 | 966. | 1116 | 1.52 |
| -113 | -113 | -113 | -113 | | • | -35 | | | 113 | 162 | .351 |
| -135 | -135 | -135 | -135 | | ť | -42 | 1955 | 18 | | | |
| | 1.000038 1561 1561 | 1561 1561 | 1361 | | • | - Q | 5097 | 137 | .996 | 1115 | 1.40 |
| - 99 | - 99 | - 99 | | | + | -32 | × | | 66 | 242 | .365 |
| -114 | -114 | -114 | -114 | | | -37 | 1730 | -28 | | | 1 |
| | .99960297 1447 1447 | 1447 1447 | 1447 | | • | -43 | 6827 | 109 | .996 | 1116 | 1.30 |
| | | | | | • | -30 | | • | 68 | 127 | .378 |
| 3 . | 3 . | \$ | \$ ' | | • | -32 | 1484 | -62 | | | |
| | .99850554 1355 135 3 | 1355 1353 | 1353 | | • | -75 | 8311 | 47 | .998 | 1116 | 1.21 |
| - 80 | - 80 | • 80 | | | • | -28 | | | 80 | 115 | .390 |
| • • | - 46 | - 46 | - 46 | | • | -16 | 758 | -47 | | | |
| 5.72 - 3.98 .99760696 1310 1307 - | .99760696 1310 1307 | 1310 1307 | 1307 | | T | 16 | 9069 | 0 | | | |
| | | | | | •. | | 2765 | meters | 2.6% • | error compared | ared this fol |
| | | | | | | | | | | | |

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This relationship is also used in deriving the equation for p/V which is presented in paragraph 5.2.2.5.

4-4. EFFECT OF PROJECTILE MASS ON TRAJECTORY

Since C_{B_0} does not vary greatly with increasing length to diameter ratio, a long, and therefore heavy round will experience a lower drag deceleration than a lighter round of the same caliber and general shape. This is the reason for the use of subsaliber or "arrow" projectiles for antitank or antiaircraft fire, where a short time of flight to a given target is of great importance. The manmer in which the mass of the round after the velocity, time of flight, range, and terminal velocity is shown in the treatment which follows.

4-6.1 Horizontal Trajectory

In this case C_p is assumed to be a constant, and the gravity curvature of the trajectory is assumed to be negligible.

$$V = \frac{dz}{dt}$$

$$\frac{dV}{dz} = \frac{dV}{dt} \cdot \frac{dt}{dz} = -\frac{D}{m} \cdot \frac{1}{V} = -\frac{C_{ab}V^{a}S}{2mV}$$

$$\frac{dV}{V} = d\ln V = -\frac{C_{ab}S}{2m}dz$$

Integrating gives

$$\ln V = -\frac{C_{pe}S}{2m}s + C \qquad (4-1)$$

4-6.1.1 Velocity

If we substitute the initial conditions, $V = V_0$, when $X_0 = 0$, into Equation 4-1:

and i

$$V = V_{s} \exp\left[-\frac{C_{AB}S}{2m}x\right]$$
 (4-3)

which shows the importance of a small C_p and a large mass if a high velocity is to be maintained as X, the range, increases. Replacing the frontal area S by $(\pi/4)d^2$ and m by W/g, we have

$$V = V_{o} \exp\left[-\frac{\pi}{8} \frac{C_{D}\rho q}{W/d^{2}} z\right]$$
(4-3)

The ratio W/d^3 is called "sectional density", and in most of the older publications is written as m/d^2 , using m as a symbol for weight.

4-6.1.2 Time of Flight

The time of flight to a given range can be obtained by substituting dx/dt for V and rearranging Equation 4-3

$$dt = \frac{1}{V_o} \exp\left[\frac{C_{MN}S}{2m}z \, dz\right]$$

Integrating

$$t = \frac{2m}{V.C_{MAS}} \exp\left[\frac{C_{MAS}}{2m}z\right] + C$$

and substituting initial conditions, z = 0 at t = 0

gives
$$C = -\frac{2m}{V \mathcal{L}_{ab}S}$$

or $l = \frac{2m}{V \mathcal{L}_{ab}S} \left\{ \exp\left[\frac{C_{abb}S}{2m}z\right] - 1 \right\}$ (4.4)

If \mathcal{T} is the time of flight to a given range X, then

$$\frac{\partial T}{\partial m} = \frac{T}{m} - \frac{X}{mV_{\star}} \exp\left[\frac{C_{ap}S}{2m}X\right] = \frac{1}{m}\left(T - \frac{X}{V_{T}}\right)$$
(4-8)

where $V_T =$ terminal velocity, or velocity at s = I.

Since $T = I/V_{exc}$ and $V_{exc} > V_{p}$, the quantity in the parentheses of Equation 4.5 is negative and the time of flight to a given target decreases in proportion to the relative increase in the mass or weight of the projectile, $\Delta m/m$, previding that V_{o} is independent of projectile weight.

However, when designing a round to fit an existing gun, mumle velocity depends in a very direct manner on projectile weight. If it is desired to make the mass of the projectile greater than the

mass, \mathbf{w}_{odd} , of the standard projectile fired from that gun, then V_o will be less than the muzzle velocity, V_{odd} , of the standard projectile. This is due to the necessity of keeping the muzzle momentum, and therefore the load on the recoil system, at or below the capacity of the system. We can write

$$V_{o} = \frac{m_{old} V_{old}}{m} \text{ for } m \ge m_{old}$$

and substituting this in the Equation 4.4 for time of flight we get

$$i = \frac{2m^3}{m_{ad} V_{ad} C_{apS}} \left\{ \exp\left[\frac{C_{DaS}}{2m} z\right] - 1 \right\}$$

and $\frac{\partial T}{\partial m} = \frac{2T}{m} - \frac{X}{mV_T}$
 $= \frac{X}{m} \left(\frac{2}{V_{ad}} - \frac{1}{V_T}\right)$

Since the average velocity is usually not much different from the terminal velocity for the flat trajectories of interest to the designer (and indeed cannot be if the assumption of constant C_B is to be be valid), we can conclude that increasing the projectile weight in a momentum limited situation will usually increase the time of flight. If the projectile mass is less than m_{refs} , then V_s is limited by chamber pressure (a constant energy constraint, $mV^2_s = m_{refs}V^2_{refs}$) and $\partial T/\partial m = 1/m (3T/2 <math>X/V_T)$. Here there is more likelihood of decreased time of flight.

4-6.1.3 Terminal Velocity

Increased projectile weight can, however, improve the terminal velocity. If we substitute $V_{o} = m_{uel} V_{otb}$ in the velocity equation, 4-2,

we get

-

$$V = \frac{m_{idd} V_{idd}}{m} \exp\left[-\frac{C_{bd}S}{2m}z\right]$$

md -

$$\frac{\partial V_T}{\partial m} = \frac{m_{ed} V_{ed}}{m^2} \left(\frac{C_{ab}S}{2m} X - 1 \right) \exp \left[-\frac{C_{ab}S}{2m} X \right]$$

So Vinning decreases with increased projectile weight for ranges which are shorter than 2m/ (C_{DP}S), and increases for longer ranges. For a typical 20-mm projectile weighing 0.22 lb, Cpp8 might be $0.4 \times .002378 \times \pi/4 = (0.066)^2 = 4.1$ × 10 * and the range beyond which increased projectile weight will give increased terminal velocity will be about 1000 meters. At this range V/V_{s} will be s^{-1} , which makes the assumption of constant C_D questionable. The accuracy of the estimate of the cross-over range could be improved by performing the calculation in steps. Since projectile weight generally increases faster than frontal area with increasing diameter $(m = kd^2)$, approximately), the cross-over range generally increases with projectile caliber; for a 105-mm projectile weighing 32 lbs, $2m/(C_{DF}S)$ would be about 7000 meters on the assumption of a constant C_P of 0.40.

4-6.2 Curved Trajectory, Antiaircraft Fire

The analysis of antiaircraft fre is complicated by the changing air density and the inability to neglect gravity and trajectory curvature; it will not be attempted here.

4-7. EFFECT OF DRAG ON TRAJECTORY

4-7.1 General

The drag of a projectile has a direct effect on its range, time of flight, and wind sensitivity; and less directly affects both static and dynamic stability. In order to obtain long range, short time of flight, and minimum lateral deflection due to side winds; the drag of the projectile should be as small as possible. Sometimes stability considerations will lead to the acceptance of a high zero-yaw drag. A reduction in yaw, obtained by improving stability decreases the yaw drag and may improve accuracy by decreasing aerodynamic jump.

The material on drag which follows is confined to the drag of a projectile flying in line with the tangent to the trajectory of its e.g., i.e., at zero yaw. The drag coefficient at zero yaw, C_{B_0} , can in this situation be called the axial drag coefficient. The increase in drag with yaw, and its coefficient, C_{B_0} , will be discussed in paragraph 4-7.9. For a well behaved projectile the initial yaw damps rapidly to

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a small value, so that by far the greater component of C_D is C_{D_0} . The minimization of C_{D_0} is, therefore, of primary importance in nearly all cases.

The designer must seek a projectile shape which will have a small axial drag coefficient, C_{D_0} , and yet have sufficient internal volume to carry the required lethal charge. He must also avoid, as far as possible, surface irregularities such as alots, depressions or protrusions. The effect of general surface roughness varies with the velocity regime of the projectile; this will be discussed later.

4-7.2 Axial Drag

The axial drag at zero yaw may be divided into three components: wave drag, friction drag, and base drag. The relative importance of the various components depends strikingly on the Mach number regime. For example, wave drag is absent in subsonic flight. For this reason the designer will choose different shapes for rounds which fly predominantly in different regimes; however, many artillery projectiles fly in all three regimes and a trajectory celeulation of some sort must be made if the optimum drag shape is to be found.

Wind tunnel testing with pressure surveys will provide a division of C_{D_0} into its components; ballistic range testing gives only the overall value. The designer is urged to refer to Hoerner, *Fisid-Dynamic Drag* (Ref. 27) in all matters relating to drag.

4-7.3 Bloct of Mach Number

The simplest way to discuss drag is from the point of view of a person observing a projectile fixed in a wind tunnel, with air flowing around it. The auropred of the projectile is then clearly the velocity of the tunnel air far enough upstream of the model not to be significantly altered by the presence of the model. The speed of sound, V_{∞} in the tunnel air at the point at which the air velocity is measured then gives the Mach number, V/V_{∞} at which the test is being conducted. At points in the neighborhood of the model the air velocity is altered in magnitude and direction but the speed of sound is assumed to be unchanged, so that the local Mach number varies from point to parts over the surface of the model in a way which depends on its shape.

4-7.3.1 Subsenic Region, $0 < M < 0.8 \pm$

The aerodynamic coefficients of a conventional projectile are fairly constant when the projectile in flying (or being tested in a wind tunnel) at Mach numbers less than some critical number, which is usually in the vicinity of 0.8. This is the model or "free stream" Mach number at which the flow over some part of the model reaches M = 1.0.

4-7.3.2 Transenic Region, .08 \pm < M < 1.1 \pm

At a free stream Mach number slightly above the critical value, the coefficients such as $C_{M_{R}}$ or $C_{D_{0}}$ begin to increase rapidly and the projectile is said to have passed from the subsonic to the transonic regime.

4-7.3.3 Supersonic Region, $1 \pm < M < 5$

At some free stream Mach number greater than 1.0 the wave system characteristic of compressive flow in fully established, and the projectile is said to be in the supersonic regime.

4-7.3.4 Hypersonic Region, M > 5

Above M = 5 the flight is termed hypersonic. This regime will not be discussed as very for conventional artillery projectiles fly at such high speeds.

4-7.4 Effect of Roynolds Number on Drag Coefficient

Drag coefficients are also infinenced by Reynolds number; geometrically similar projectiles of different calibers will have slightly different C_{B_0} vs Mach number enross.

In the subsonie range $(0 < M < 0.8 \pm)$ we would like to have a rounded, but not necessarily pointed, none and as small a base diameter as eas be provided in view of the many considerations which after projectile shape, such as required internal volume, well strength, propulsive method,

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type of stabilization, fuzing, etc. The effect of projectile shape is discussed below.

4-7.5.1 Surface Roughness and Irregularities

Surface roughness corresponding to ordinary industrial practice will have little effect on the drag coefficient. Surface irregularities, such as alots, shallow holes, and protuberances may increase the drag very greatly, depending on their location and orientation. Fuzes are often poorly designed in this respect and consideration may be given to eovering them by a windshield.

4-7.5.2 Blunt Nese

Blunting the nose of a projectile will, in the subsonic regime, have little effect on overall drag. The important effect of blunting (short of a completely flat face) is to lower the critical Mach number. Small flat faces, such as appear at the nose in many point-detonating fuzes, have little effect on drag. The integral of the dynamic pressure forces over a properly shaped head will be close to zero, and the forebody drag will accordingly be close to zero. The base drag is thus the result of a pressure deficiency over the base of the projectile; the existence of this sub-static (less than atmospheric) pressure is evident in everyday life in the wake of trains and automobiles.

4-7.5.3 Beettailing

Reducing the diameter of the base below that of the cylindricel body, called "boattailing", is a very effective way of reducing base drag in the subsonic regime. Boattailing also reduces the lift coefficient and changes the position of the center of pressure of the normal force, moving it forward. This reduces the stability of the projectile, placing another limit on the amount of boattailing that can be tolerated.

The extent to which this can be done on a spinstabilised projectile is limited by the necessity of applying a rotating band, which must be supported by a relatively thick wall, and by the fact that the projectile walls aft of the rotating hand are ordinarily exposed to the full chamber pressure so that they must also be thick. These considerations limit the length of the boattail and may also limit the amount of reduction in base area. Use of a hollow

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boattail avoids these limitations, but sacrifices internal volume.

I'se of a large boattail angle (greater than about 16°), without a rounded transition from the cylindrical body, can cause the air flow to separate at the junction, cancelling all of the drag reduction.

4-7.5.4 Fin-Stabilized. Projectiles

The zero-yaw drag of fins is, of course, related to their shape and size, but these are dictated primarily by stability considerations. While it is true that some fin profiles have less drag than a simple flat plate, the extra cost of manufacturing the double wedge or streamline profile fins must be weighed.

4-7.6 Transonic Drag

4-7.6.1 Spin-Stabilized Projectile

The transition from the subsonic to the supersonic drag regimes is clearly illustrated, for a typical low-drag spin stabilized projectile, in E. D. Boyer, Aerodynamic Properties of the 90-mm HB M71 Shell (Ref. 79). The ogive of this projectile extends over about half its length, the boattail is half a caliber long and the boattail angle is 7°. Its subsonic C_{D_0} is 0.15, even though the rotating band area has four circumferential slots.

Shadowgraphs at M = 0.88, M = 0.97, and M = 1.05 show the initiation of the shock waves at the points of abrupt change in diameter and their growth to fully developed waves. Co, rises from 0.15 to 0.39 in this Mach number interval. as can be seen from the drag curve in Appendix VIII-E. No shock wave appears over the nose of the projectile before photograph at M = 1.05, when a separated how wave is present. So we can say that for this projectile the transonic regime covers the Mach number range from approximately 0.88 to 1.05. Note this is only one example; the numbers would be different for a different projectile. The development of the shock waves on the body and fins of an arrow projectile is shown by the shadowgraphs in BRL Report 934 (Ref. 89).

The greatest part of the increase in drag in the transo, is regime can be attributed to the presence of the shock waves and is called "wave drag". The base drag peaks at about M = 1.0; the friction



4.9

drag becomes relatively small as the total C_{B_0} inereases.

4-7.6.2 Fin-Stabilized Projectile

The drag of typical fin-stabilized projectiles in the transmic regime increases in about the same way as described above, as may be seen from the drag curves presented in Appendixes VIII-T through VIII-Z. The designer should obtain and study a number of shadowgraphs or schlieren photographs of projectiles of varying shapes in conjunction with their drag curves.

4-7.7 Supersonic Drag

4-7.7.1 Decrease of CD, with Mach Humber

After the shock wave system is fully developed, which usually occurs at a free stream Mach number between 1.1 and 1.2, we find that C_{D_p} decreases with increasing Mach number.

In fact, we can use $Q = \sqrt{c + C_{B_0}} M^2 = a + bM$ as an interpolation formula; a typical set of values of the constants might be a = 1.6, b = 0.2, c = 2.7.

4-7.7.2 Effect of Ness Shape on CD.

The size of C_{P_0} in the supersonic regime depends largely on the shape of the none. By the Taylor-Maccoll formula (Ref. 30) we have

$$C_{P_{P}} = \left(.0016 + \frac{.002}{M^2}\right) e^{1.7}$$

where $C_{P,p}$ is the forebody pressure drag (wave and drag) component of $C_{P,p}$, e is half of the conc. angle, in degrees, and M is Mach number.

While by this formula the lowest drag shape for the rose would be a cone, an ogival none having a large ogival radius will have slightly lower drag (and also afford a greater warhead volume). **B.** R. Dickinson (Ref. 24) found from ballistic range firings at M = 2.44 that the minimum drag head shape of a caliber .50 projectile (d = 0.0417ft) was a secant ogive having a radius twice that of the tangent ogive of the same length and maximum diameter (ratios between 1.7 and 2.5 were nearly as good).

The presence of a small flat (or rounded) surfuse at the front of the none, called the meplat, has only a small effect on C_{B_0} , and indeed, if not too large, may reduce C_{B_0} slightly below that for a pointed none of the same length.

4-7.7.3 Effect of Beattailing on CD.

Boattailing reduces the drag of supersumic projectiles as long as the airflow is able to follow the contour of the body. For each projectile shape there is a critical angle (generally about 8°) and a critical boattail length (about 1 caliber at the critical angle, longer for smaller angles) beyond which the flow will separate from the projectile forward of the base, reulting in a C_{D_0} which is greater than the minimum attainable, and which varies from round-to-round with consequent degredation of accuracy. See Bafs. 25 and 26.

4-7.8 Dual Flow

As a general rule, we assume that projectiles having the same shape and e.g. location will have the same set of aerodynamic coefficients when fired at the same Mach number (and Reynolds number), and that small differences in shape and surface finish will produce only small differences in the cuefficients. The few outstanding exceptions to these rules are discussed below.

4-7.8.1 Spike-Neaed Projectiles

It was found some time ago that replacing the ogival head of a projectile by a slender cylinder protruding from the flat forward face of the body would move the c.p. of the normal force rearward, reducing $G_{H_{\alpha}}$ and reducing the spin rate required to stabilize a spin-stabilized round, or reducing the length of the tail required on a fin-stabilized round. These spike-nosed projectiles had higher drag coefficients than the corresponding projectiles with ogival heads. Also, for some designs, projectiles from the same lot, fired under the same conditions, exhibited drag coefficients which fell in one or the other of two groups, with the averages of the two groups as much as 30% apart.

Examination of spark photographs showed that the low drag coefficients were associated with rounds on which the airflow separated from the spike at its tip, while on the high-drag rounds the flow separated at a point about half-way down the spike. This phenomenon was called "dual

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M=2.75

L=1.0 CALIBER

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M=3.80



L=1.0 CALIBER



L=1.5 CALIBERS



The pictures, taken in the DRL supersonic wind tunnel, show that the character of the flow over a spike nose depends on Mach number and nose length. The flow separation is delayed, with consequent increase in drag, on the three photographs at the lower right hand corner(*). Thicker spikes showed delayed separation at shorter lengths (Ref. 35b).

L=1.5 CALIBERS

Figure 4—2. Flow Patterns on Varying Length, Constant Caliber .33 Diameter Spike Nases at Supersonic Velocities



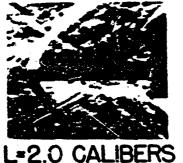
M=1.73













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How"; its existence was a function of the geometry of the spike. In order to avoid the occurrence of dual flow, with its serious effect on accuracy, modern spike-nosed rounds are furnished with a small ring near the tip of the nose which insures the early separation of the flow.

Figure 4-2 shows the effect of Mach number and nose length on the flow pattern produced by a spike-nosed projectile.

4-7.8.2 Undercut Projectiles

Another example of dual flow was found in ballistic range firings of projectiles having the central part of the body deeply undercut; drag and moment coefficients varied from round-to-round by as much as 50%. The flow pattern, whether high- or low-drag, was stable; i.e., once established, it persisted throughout the observed flight of the projectile. The possibility of dual flow may sometimes be detected by wind-tunnel tests when ballistic range firings do not reveal its existence.

4-7.8.3 Hemispherical or Sharply Conical Base Projectiles

The point of separation of the airflow from the base of a projectile having a hemispherical or sharply conical base will also vary from roundto-round, but in a continuously distributed manner, so that this behavior is not classified as 'dual flow'. The hemispherical shape allows the wall of the base to be thinner, so that more HE can be carried, but extra care must be taken to insure dynamic stability (see Appendix VIII-H).

4-7.9 Drag Variation with Yaw

The increase in drag when the attitude of the projectile changes from zero yaw to a yawed position is called by some writers "induced drag." This term is borrowed from airplane terminology, and is equivalent to "drag due to lift." For small yaws, the axial drag is very nearly unchanged from its zero-yaw value, and its component parallel to the trajectory is also very little changed, since $\cos \delta = 1$ when $\delta = 0$. The normal force is inclined rearward at an angle δ , so it has a component in the drag direction which is given by $C_{S_n} \delta^2 q \delta$ when $\delta = \sin \delta$. The expression for the drag coefficient then becomes

$$C_D \approx C_{D_0} + C_{H_0}$$

However, the observed coefficient of variation of drag with yaw squared, C_{Dg^*} , is usually about twice as large as $C_{N_{a^*}}$.

While the induced drag may be reduced somewhat by choosing a body shape having a small $C_{N_{\alpha}}$, dynamic stability may be impaired so that the set effect on drag may be unfavorable.

The above observations apply to fins as well as to bodies. It will be seen that over-stabilizing a finned projectile by means of a large fin lift may result in a C_0 penalty as well as increased muscle blast sensitivity.

4-7.10 Muzzie Blast

4-7.10.1 Yawing Velocity Due to Transverse Vibration of Muzzle

Nearly all projectiles emerge from a gun with essentially zero yaw. Even mortar projectiles, which have large bore clearance to facilitate drop firing, can lie in the tube no more than 0.3° out of line with the tube axia. The possibility exists that transverse vibrations of the muscle may movthe rear end of the projectile after the e.g. has passed the muscle; this action, as well as any overall motion of the gun tube, can impart yawing velocity, to the projectile[®], but no significant exit yaw.

Equations for aerodynamic jump, which is one of the two primary flight characteristics, will be presented later in this handbook. It is noted here that jump is primarily a function of initial yawing velocity, and not of initial yaw.

4-7.10.2 Transverse Pressure Gradients

Transverse pressure gradients in the massle blast can impart some yawing velocity to the projectile if the e.g. of the projectile does not coincide with the center of pressure of the transverse force. This effect is most prominent when firing with a worn gun tube. These transverse pressure gradients are probably related to the bore yaw of the projectile. Good obturation reduces the pressure differences in the blast and shortens the effective blast zone, thus reducing initial yawing velocity, aerodynamic jump, and dispersion at the target. An improvement in accuracy of hot rounds over cold

"For a theoretical and experimental study of the effects of gun motion, see Baf. 3.

rounds of the same projectiles arises chiefy from their better fit in the tube, partly because boreyaw is reduced and partly because obtaration is improved.

4---7.10.3 Fin-Stabilized Projectiles in Reversed Flow

Fin-stabilized projectiles are affected by the muzzle blast su yet another way. For a short time after emergence from the muzzle the blast gases are flowing forward over the fin surfaces, resulting in a large destabilizing moment which can impart a significant yawing velocity even though the time of action is abort. It is of great importance that the aerodynamic moment coefficient of the fins in reversed flow he kept as small as possible.

Many photographs of the mussle blast are available in firing test reports of the Development and Proof Services, Aberdeen Proving Ground, Maryland.

Since the camera usually takes thousands of pictures per second, the emergence of the projectile from the smoke cloud can be observed, and the time spent in reversed flow estimated. The data from the photographs can be correlated with the dispersion of hits on the target; these correlations clearly show the importance of obturation for fm-stabilized rounds.

4-7.18.4 Obtacation

Kateusion of the rotating hand material into the grooven of the riding is usually contidered to furnish adequate objuration for apin-stabilized rounds. However, some recent projectile designs have included special obturating rings or dises, similar to the devices constronly used on finstabilized rounds, these devices are described in paragraph 5-3.4.

4-7.11 Greateriad

4-7.11.1 Wind Sensitivity

While (as projectile draigner assaut do anything about the wind, he can do consthing about the smattivity of his projectile to the effect of wind. A stable projectile will near into the wind, i.e., the equilibrium position of the inngitudinal axis of the projectile, neglecting yow of response and trian, will be in line with the resultant of projectile velocity and wind velocity. The net drag force (drag minus rocket thrust) will then have a component at right angles to the projectile velocity. In the absence of rocket thrust, or if drag exceeds thrust, the projectile will acquire a downwind lateral velocity and displacement; if thrust exceeds drag, the projectile will more upwind.

4-7.11.2 Lateral Deflection

With no rocket thrust, a constant crosswind, and making the usual assumption that the projectile, aligns itself with the resultant air-stream as soon as it leaves the muzzle of the gun, we can write a very simple expression for the deflection of a fai trajectory by a crosswind (see II. P. Hitchcock, The Motion of z Very Stable Shell at Short Ranges, BkL Report 1047, April 1958, p. 19).

$$Y = V_{\bullet} \left(T - \frac{X}{V_{\bullet}} \right)$$

where.

X = lateral deflection at impact, ft
V_☉ = crosswind velocity, fps
T = time of flight, sec
X = range, ft
V_☉ = mussle velocity, fps

The only variable in the above expression is the time of flight. Substituting for 7 its equivalent, as given in paragraph 4-6.1.2, we have

$$Y = \frac{V_{\pi}}{V_{\pi}} \left\{ \exp\left[\frac{C_{bp}S}{2m}X\right] - 1 \right\} - X \right]$$

From this equation we can find that the lateral deflection in mile decreases with increased projectile weight or mussle velocity, and increases with inerrose in C_p.

These relations furnish the designer with additional reasons for neeking low drag and high sectional density (unless his projectile contains a recht motor, when the trade-off situation becomes more complex).

4-7.12 Values of CD, vo Mach Humber

Curves of Ca_p vs Mach number for typical projectiles are shown in Appandiare VIII-A through VIII-E. The configuration of the projectile is shown on each page in order to cashle the designer to interpolate between shapes.

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CHAPTER 5

CHOICE OF METHOD OF STABILIZATION

5-1. STABILITY

5-1.1 General

In order to have a small induced drag, a projectile must be stable, i.e., the yaw of the projectile must damp to a small equilibrium angle early in its flight. If not statically stable nor gyronospically stable, the projectile will commence to tumble as soon as it leaves the muzzle of the gun; if not dynamically stable, the yaw of the projectile will grow continuously with time, so that the projectile will tumble or go into a tat spin unle the expected time of flight is very short.

5-1.2 Static and Gyroacopic Stability

Static stability is related to the position of the center of gramme of the normal force with respect to the e.g. of the projectile. If the e.p. is aft of the e.g., the projectile is statically stable, i.e., any yaw of the projectile produces a moment about the e.g. which touch to return the axis of the projectile to the zero-yaw position. If the e.p. m ahead of the e.g., the normal force produces an overturning moment tending to increme the yaw. However, if the projectile is mining rapidly enough about its own axis, the yaw will not grow rapidly but mainly change direction; the projectile is said to be gyruscopically stable, even though othering moment.

ince the e.p. of a cylindrical body of revolution is usually alread of its centroid, a typical projectile shape is unstable unless:

a. Mass of the projectile is an concentrated at the forward and as to more the e.g. alread of the c.p. (this is rarely a practical solution). or

- b. Projectile in provided with a flaring rear end or with flat surfaces (fins) at the rear of the body which move the c.p. rearward of the c.g., or
- e. Projectile is made gyroscopically stable by spin.

5-1.3 Factors to be Considered in Choice of Fin-Stabilization

5-1.3.1 Against

Fixed fins take up length without adding to the payload volume of the projectile, except 1a the special case of an arrow, or subcaliber, projectile. Folding fins either add to the length or reduce the volume, depending on the design adopted, but in any case add to the complexity of the projectile. Since the unsfulnam of a projectile of a given maximum diameter and overall length in reduced when its payload volume in reduced, and, in general, spin-stabilised projectiles are cheaper than and an accurate as the corresponding fin-stabilised projectile having equal payload, properties are stabilard by spin unlanthere are overriding reasons to the contrary.

5-1.3.2 Ter

Some of the reason for chaosing fin-stabilization are :

a. A fin-stabilized projectile can be larger in perpection to its diameter (have a greater fineness paties) than one which is appo-

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stabilised. If the logistic limitations on length (storing, handling, loading into the gun) are not exceeded, the fin-stabilized projectile may be long enough to have an internal volume greater than that of the corresponding spin-stabilized round.

- b. The lethality or other terminal usefulness of the round may be impaired by spin. An example in this category is the shaped charge round.
- r. The mission of the projectile may require that it be fired at high quadrant elevations. Conventional spin-stabilized rounds suffer nevere degradation in neveracy when fired at quadrant elevations greater than about 65°; fin-stabilized rounds do not.
- d. The internal structure of the projectile may be such that the round becomes dynamically unstable when spun, or even such that it cannot be spun rapidly enough for gyroscopic stability by the guns available.
- The projectile may be designed to be fired from a smooth-bore gun.
- f. Pin-stabilized projectiles can be fired from a rifled gap without picking up enough spin to lose accuracy. This is done by the use of an obturator which engages the rifling but align on the projectile.

5-2. SPIN-STABILIZED PROJECTILES

The first requirement we place on a projectile in that it be atable. It must be stationally or gyrowopically stable; it must also be dynamically stable sulton its expected trajectory is very short. The stability of spon-stabilized projectiles is treated in the paragraphs which follow.

5-2.1 Gyrescopic Stability

5-2.1.1 Gyrescopic Stability Factor

The gyroscopic stability of a spin-stabilised projectile can be assessed by computing a_j, the gyroscopic stability factor.

.....

 $I_{\rm s} = xx_{\rm sl}$ moment of inertia, slug-ft²

 $I_p = \text{transverse moment of inertia,}$

- p = axial angular velocity, rad/are
- " = static moment factor, lb-ft/radian

On the assumption that the static moment varies linearly with yaw, the expression for the static moment per radian of yaw in

a = air density, slug/ft³

d == maximum body diameter, ft

V = airspeed, ft/me

 $C_{H_0} =$ static moment cuefficient, per radian

Close attention must be paid to the units used in these expressions, as some of them are not the units customarily employed in reporting measurements of the quantities.

5-2.1.2 Conditions on Value of s, for Stability

If $0 \le z_0 \le 1$ the projectile is unstable and will "tumble" within a few hundred feet of the gun.

If s_p is greater than one, the projectile is gyroscopically stable, and we then investigate its dynamic stability, as described later. Since s_p is inversely proportional to the density of the air, projectiles which are stable at standard atmospheric conditions may be unstable when fired under arctiv or other nonstandard conditions of temperature and pressure. Pumble environments must be taken into account is computing s_p ; this fart, roupled with the unvertainties in the other factors entering into s_p , has led some daugners to set 1.3 as a lower limit on s_p in the preliminary daugn stage, using standard air density in the computation.

Note that at the mussle we can write

=
$$C_1 \left(\frac{p}{V} \right)^*$$
 where $C_1 = \text{exastant}$

but $p/V = 2\pi/nd$, where n is the twint of the rifling at the mumle, in collibern per turn. Hence the initial stability of the projectile depends on the rifling twint and only indirectly on mumle velocity. If this were not in, morel fire, i.e., firing with re-

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duced propelling charge, would be impractical. The indirect influence of muzzle velocity arises from the dependence of $C_{H_{0}}$ on Mach number; this dependence can cause instability at reduced muzzle velocities.

Conventional projectiles lose airspeed much more rapidly than they lose spin. The value of s_{σ} thus nearly always increases as the projectile flies down range.

The stability factors of projectiles fired at high quadrant elevations can, unless projectile velocity is maintained by rocket thrust, reach quite large values at the summit of the trajectory, owing to decrements in both velocity and air density. These large values are not detrimental in themselves, but the conditions which produce them also bring about large increments in the equilibrium yaw of the projectile.

5-2.2 Yaw of Repose

5-2,2.1 General

The gravity enreature of the trajectory gives rise to an angle of yaw large enough to create a prevention rate which will permit the axis of the projectile to follow the tangent to the trajectory. This equilibrium requirement causes the projectile to point to the right of its flight path (right-hand yaw of repose) when the spin of the projectile is elockwise as viewed from the rear, which is the case with nearly all l'nited States artillery ammunition. The lift force associated with this angle causes a drift to the right, and an estimate of the magnitude of this drift is given in the firing tables for the projectile. The designer is interested in heeping this drift amail, and as miniferms, from round to rotsel, as pamible.

The yaw of repose in proportional to p/V^3 , If it becomes large, the projectile may become dynamically unstable with resulting loss in range and accuracy.

5-2.2.2 Formula for Angle of Repose

An approximate expression for the usual righthand yow of repose is

 $b = \frac{I_{g} pq \cos \Theta}{\frac{1}{2} pdd C_{H_{g}} V^{2}} \left(1 + i \frac{C_{H_{g}}}{C_{H_{g}}} \frac{pd}{V}\right)$

This equation shows that at the summit of a high angle trajectory, where $\cos \theta \approx 1$ and ρ is considerably less than its are level value, if 1' is small the yaw may be very large; it may even shift over to the left-hand equilibrium angle with disastrons results for the trajectory prediction. See Ref. 66, p. 392.

5-2.2.2 Trailing

An analysis of the first (and most significant) term of the expression for yaw of repose may shed

$$L = \frac{l_{*} p p \cos it}{\frac{1}{2} p^{N} d C_{N_{*}} V^{2}} + \dots$$

some light on the mechanism by which a spinning projectile "trails" as it moves along its trajectory. Rearranging the above equation gives

$$\frac{1}{2}\rho V^2 Sd C_{H_{\alpha}}L = I_{\alpha} \frac{\rho \cos \Theta}{V}$$

On the left side of the equation we have the static acrodynamic moment, on the right nide we have the axial angular momentum, I.p. multiplied by the rate of change of direction of the tangent to the trajectory, $g \cos \theta/V$ (see paragraph 4-5). The product is a rate of change of angular momentum, caused by the serodynamic moment; conversely, the aerodynamic moment arising from the yaw of repose is just sufficient to change the angular momentum of the projectile at the rate required for the axis of the projectile to remain tangent to the trajectory (in the vertical plane the yaw is in a plane normal to the trajectory plane and the stati- moment is at right angles to the rotation, or 'prevenies', of the projectile axis, which is the well knews gyroneopie behavior).

5-2.2.4 Projectile Asymmetries

Asymmetries of a projectile, arising from the manufacturing process, will add (vectorially) a small constant yaw to the yaw of ropose, increasing the pumibility of trouble at the summit. Asymmetry also introduces a forving function which can lead to resonance; the resulting yaw can be large for fin-stabilised projectiles, and the subject will be discussed further in paragraph 5-3.

5-2.2.5 Method of Computation of Projectile Spin

The gyroscopic stability factor is calculated at the muzzle and is often calculated at the summit of high angle trajectories as an index of summital behavior. It is recommended that the designer compute the yaw of repose at the aummit of such trajectories, and compute the stability factor at the muzzle and at impact. If his computer program does not include a running calculation of spin rate, he must estimate as well as he can what the apin rate of the projectile will be at summit and impact, using the expression (in the absence of recket thrust)

$$\frac{\frac{P}{V}}{\left(\frac{P}{V}\right)} \approx \frac{\cos \Theta}{\cos \Theta_{a}} \exp \left[\frac{\rho S}{2m} \left(k_{a}^{-1} C_{l_{p}} + C_{p}\right) (z-z_{a})\right]$$

where the subscript σ refers to conditions at the beginning of the interval over which the change in p/V is bring computed, x is distance measured along the trajectory, and $k_e^{-2} \equiv md^2/I_e$. This expression assumes that ρ , C_{i_p} and C_{σ} are constants, which is not likely. Average values of these parameters must be used, and it will be seen that the approximation for p/V may be poor. Designers of spin-stabilised projectiles have been willing to assume that the projectiles retained enough spin to be stable at impact and to accept whatever limitution on quadrant elevation was found to be pressure in test firings of the reand.

While C_{r_p} is negative, C_n is usually of sufficient magnitude that p/V increases as the projectile rises to the summit. On the descending limb the casine of the trajectory angle is decreasing, and p/V will decrease, since obviously V is increasing while p, in the absence of some spin-producing mechanism such as a canted fin, continues to decrease.

Shown in Table 5-1 and Table 5-2 are sample trajectories for a typical 5-inch projectile, with initial conditions differing only in quadrant elevation. The trajectory with $Q.E. = 3^{\circ}$ offers an opportunity for a simple check on the $(p/V)/(p/V)_{0}$ equation presented above. Using average values of p and C_{m} , we have, for p, V at import

$$\frac{\frac{p}{V}}{\frac{p}{V}} = \frac{r}{r_{e}} \approx \frac{\cos(-3.9^{\circ})}{\cos 3^{\circ}} \exp\left\{\frac{(.001186) (0.1355)}{1.435}\right\}$$

$$(6.89 (-.014) + 0.365) 9330 \left\{\frac{-.99777}{.99966} e^{-.384} = 1.325\right\}$$

The trajectory calculation gives $\nu/\nu_o = .295/.224 = 1.32$, so the approximate formula is very good for flat fire.

For the trajectory with Q.E. = 70°, the rough estimates of ρ and C_B obtained by taking simple means values would be 000000 for ρ and 2265 for C_B .

$$\frac{\cos((-77.8^{\circ}))}{\cos(70^{\circ})} \exp\left\{\frac{(.00088)(0.1355)}{1.435}\right\}$$

$$\left(6.89((-.014) + 0.285)(54100)\right\}$$

$$= \frac{.2113}{.3420^{\circ}} = 1.45$$

The trajectory calculation gives $\nu/\nu_{\nu} = .289/.224$ = 1.29, so the approximation is only fair. The use of values of C_{ν} weighted by the arc distance traversed, in calculating the means, would make the approximation for ν/ν_{ν} very good.

The high angle trajectory is presented principally to show the magnitude reached by the yaw of repose at the summit. The actual yaw might be nuch greater because dynamic instability, owing to nonlinearity of the acrodynamic coefficients, is likely to occur at yaws of this magnitude.

5-23 Zoning

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Conventional projectiles attain their maximum range when fired at a quadrant elevation of about 45°. For rocket-amisted projectiles the Q.E. for maximum range is greater than 45°, running up to 60° or 70° when using a long-burning rocket wit^b a high ratio of fuel weight to total projecti. weight. Eanges shorter than the maximum may be obtained by changing the Q.E., reducing the effective rocket thrust, or reducing the mustle velocity. Reduction of the mustle velocity in a sories of stops, by reducing the charge of gun propellant, is called "soning"; each level of mustle velocity is called a "some", and variations of range within cosh some are obtained by varying the quadrant elevation.

A projectile where range is controlled by muscle

velocity variation must be stable over a wide range of Mach numbers, which will almost certainly include transonie speeds at sea level air densities. Since CH, usually peaks in the transmie regime and the gyromopic stability factor is inversely proportional to $C_{H_{\alpha}}$, stability may be at a minimum in the transmie regime. If Cu, data are not available for the full range of speeds, estimates may be made by use of the shapes of the $C_{H_{\alpha}}$ vs Mach number curves of projectiles similar to the one in apestion. Use of an estimated $C_{H_{\alpha}}$ requires a greater margin of safety on the gyroscopic stability factor to insure that it does not become less than unity. However, if trajectory calculations show that the projectile will spend only a short time in the transpaie regime, it may be possible to accept a certain amount of instability for that short time.

The gyroscopic stability factor of a conventional spin-stabilized projectile usually has its smallest value at the muzzle. Rocket-assisted projectiles, on the other hand, are more likely to become gyroscopically unstable on the descending limb of the trajectory, near impact. This instability can be avoided by:

- a. Distributing the mass of the projectile sy that its e.g. is forward of the usual location in a projectile of the given aerodynamic shape.
- . b. Increasing the rifting twist of the gun.
- c. Canting the rechet nearles, or providing internal means of rotating the jet from a single nearle.

5-2.4 Dynamic Stability of Spin-Stabilized Projectiles

5-2.4.1 Magnitude of Modal Vectors

The yew of a symmetric projectile acted on by a linear force and moment system is given by

- K₁₀ = initial magnitude of notation verter
- K_{1,} = initial magnitude of preormion vostor
-), = solation damping exponent, per caliber

 λe = precession damping expotent, per caliber
 a .= travel of projectile, calibera

- $\phi_1 = \text{phase angles of the model}$
 - vectors (j = 1,2)

– equilibrium yaw

We are concerned here with the magnitudes and signs of λ_1 and λ_2 . It will be seen that the magnitude of a modal vector will increase if its associated λ is positive; the larger the value of λ the more rapid is the increase in the magnitude of the vector. The term $e^{i\phi}$ is, of course, simply a sinusoidal oscillation between +1 and -1, and between +iand -i. If neither of the two modal vectors, K_1 or K_2 grows in magnitude as the projectile files down range, the projectile is said to be dynamically stable. For dynamic stability, therefore, both λ_1 and λ_2 must be equal to, or less than zero.

From Ref. 12a we have

$$\lambda_{t} = -\frac{1}{2} \left[H - \frac{2T - H}{\sqrt{1 - 1/4_{p}}} \right]$$

and λ_0 differs only in having a + sign between the two terms inside the brackets.

$$H = \frac{aSd}{2m} \left[C_{L_0} - C_0 - k^{\frac{1}{2}} (C_{H_0} + C_{H_0}) \right]$$
$$T = \frac{aSd}{2m} \left[C_{L_0} + k_0^2 C_{H_0} \right]$$

So, since s_p is a function of C_{H_p} and (indirectly) of C_{ip} , we see that all of the major asrodynamic coefficients enter into the determination of the damping exponents.

5-2.4.2 Dynamic Stability Factor, sa

Murphy (Ref. 12a) recommends that instead of simply requiring that the λ_i be nonpositive, we should set an upper limit on the greater of the two which must not be exceeded if the projectile is to fulfill its mission. This limit, represented by an unsubscripted λ_i may be greater than zero because some growth of initial yaw may be tolerable, especially in short fights.

5-2.4.2.1 Stability for $\lambda_{aaa} \leq \lambda_{aaa}$

Marphy then introduces the

stability

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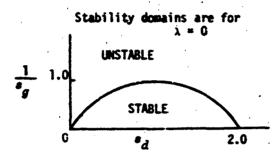
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$$=\frac{2T+2\lambda}{H+2\lambda}$$

and by use of the expression for λ_{max} with the restraints that $\lambda_{max} \le \lambda$ and $H + 2\lambda > 0$, arrives at the identity

$$\frac{1}{s_g} = s_d \left(2 - s_d\right)$$

Plotting this expression as a curve with $1/s_r$ and s_c as coordinates, we get





Conditions as to stability are a function of the location of the point determined by the intersection of $1/s_0$ with s_0 (Figure 5-2), namely:

- a. Intersection lies below curve: Projectile in gyroscopically stable and may be dynamically stable, with $\lambda_{max} < \lambda$.
- b. Intersection lies on the curve : $\lambda_{max} = \lambda$
- e. Intersection lies above curve: Projectile is dynamically unstable with $\lambda_{max} > \lambda$ and may be gyraneopically unstable.

5-2.4.2.2. Stability for $\lambda = 0$

In practice, λ is often set equal to zero. Then the expression for the dynamic stability factor is*

$$u_{g} = \frac{2T}{H} = \frac{2(C_{L_{g}} + k_{g}^{-1}C_{H_{gg}})}{C_{L_{g}} - C_{g} - k_{f}^{-1}(C_{H_{g}} + C_{H_{gg}})}$$

The curve in Figure 5-1 is now the locus of points where $\lambda = 0$. If the intersection of $1/s_p$ with z_p lies above the curve, we can aclculate λ_{max} by measuring Δs_p , the change in s_p required to reach "home authors add $C_p + k_p = C_{l_p}$ to the descentator; however, this sum is eductively zero compared with C_{k_p} . the curve, moving horizontally, and using the following relation:

$$\lambda_{\max} = \frac{H/2}{1 - \epsilon_{d_p} - \Delta \epsilon_d} \Delta \epsilon_d \text{ when } \frac{1}{\epsilon_p} < 1$$

(Remember that H contains the factor $p z_d/2m$.) Note that H > 0 is one of the constraints on z_{d_0} , so the λ_{max} computed by the above expression is pusitive, and one of the yaw vectors is undamped; we can estimate the growth of this vector from exp { λ_{max} } where s is travel in calibers. Similerly, when the intersection lies below the curve, use of the above expression for λ_{max} will result in a negative value with which the rate z_1^2 decrease of yaw can be computed.

Returning to the expression for s_{e_0} we note that $C_{L_{e_0}}$ is always positive and usually much greater than C_{B} . The denominator of s_{e_0} is nearly always positive. If it is not, we abould not compute s_{e_0} . The numerator contains the magnum moment coefficient, $C_{H_{B^0}}$, which is usually positive for spinstabilized projectiles at supersonic speeds, but often negative at transmic and subsonic speeds. s_{e_0} is usually positive, and indeed the values of the roefficients and radii of gyration (in calibers) are such that s_{e_0} is outside these limits, the projectile cannot be stabilized by spin.

In BRL Report 853 (Ref. 48), Murphy discurses the influence of mass distribution on the dynamic stability of statically unstable projectiles. He notes that at supersonic velocities many bodies of revolution cannot be stabilized by spin if the e.g. is more than two calibers aft of the centroid. The centroid is, of course, the point at which the e.g. would be located if the projectile were of uniform density; it is near the geometrical controid of the xilhouette of the projectile. In any case, there is an optimum e.g. location which minimises the spin rate required for stability, and this optimum location is usually near, and aft of, the erstroid.

The complete graph of 1/s, vn se, taken from Ref. 12a, appears as Figure 5-2.

Unfortunately $C_{H_{ph}}$ is sensitive 15 changes in yaw angle. We cannot preserve Hissarity in the magnus moment by restricting 3 to less than 10° as we have assumed that we could for some other iscredynamic coefficients. A large $C_{L_{ph}}$ and k_{p} will

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TABLE 5—1SAMPLE TRAJECTORY FOR SPIN-STABILIZED 5-INCE PROJECTILEAT Q.E. = 3°(SEE APPENDIX I)

| | | | A RGT | | FT | | |
|--------------------|---------------|----------------|-----------------|---------------|-------------------|--------------|--------------|
| 3.0 | .250 5. 0. | .540 .3 | 61 1.03 | | 4150 | | • |
| MT0 | VO | SPIS | SBT | DTH | TWIST | QE | |
| 46.08 WTB | 1925. ZO | TEMP. | .0 DTL | .400 DTE | 28.00 CDD2 | 3.000 CLP | |
| 46.08 | • | 59. | 4.0 | . 350 | 6.00 | 014 | |
| .001189 | 1116.0 | | | | - | • | |
| TIME | Ž | DIST THRUST | DRAG | CD YA!: | CHA DR Mach Sp | | |
| .00 | • . • | • | 1925.0 197.4 | .331 .000 | | 1.000 | 1.43 1.36 |
| .12 .99 .03 | 1694. 75. | 1695. | 1804.4 | . 342 | 4.01 | .997 .234 | 1.43 |
| .13 1.04 .03 | 1937. 34. | 1938. | 1787.5 | . 344 | 4.02 | •9 97 | 1.43 |
| .13 1.74 | 3156. | 3158. | 176.3 1704.1 | .000 | · | .236 .996 | 1.48 |
| .02 .14 2.94 | 118. 5125. | • 5197 | 163.7 1574.8 | .000 | | .244 | 1.57 |
| 00 | 137. | • | 144.6 | .001 | | .995 .259 | 1.43 1.72 |
| 4.09 02 .17 | 6867. 113. | 6870. • | 1465.8 129.8 | .377 .001 | | .996 .273 | 1.43 1.88 |
| 5.15 05 .18 | 8375. 55. | 8379. | 1375.5 117.9 | . 388 .001 | | •998 •286 | 1.43 1.99 |
| TINE,S | RANGE | V, FPS | THETA,D | SPIN | SG | | , |

5.85 2839. 1316. -3.9 .295 2.04



and the second secon

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TABLE 5---2SAMPLE TRAJECTORY FOR SPIN-STABILIZED 5-INCH PROJECTILEAT Q.E. = 70°(SEE APPENDIX I)

| FFD F 1.050 1. WTO | 250 5. | PE RG | 81 1.03 | 0.4 | 150 | 05 | |
|--------------------------|-----------------|--------|-----------------|--------------|---------------------|--------------|------------|
| 46.08 | 1925. | SPIS | .0 | | TWIST 28.00 | | |
| WTB | ZO | TEMP | DTL | DTE | CDD 2 | CLP | |
| 46.08 | • | 59. | 8.0 | .350 | 6.00 | 014 | |
| .001189 | 1116.0 | | • | | · | ·. | |
| TIME. | X | DIST | v | CD | CHA DR | MASS | |
| THETA | ź | THRUST | DRAG | YAVI | MACH SP | IN SG | • • |
| .00 | • • | • | 1525.0 197.4 | .331 .000 | 3.93 1.72 | 1.600 | 1.43 |
| .22 5.62 | 3140. | 8749. | 1260 0 | 207 | 4.53 | 770 | 1.43 |
| 1.17 | 8166. | • | 78.2 | .002 | 1.16 | .313 | 3.00 |
| .35 | 7140 | 40734 | 330 4 | •60 | F 60 | F D 4 | 1.43 |
| 15.86 | 7420. 16951. | 10731. | 739.1 8.6 | .100 | 4.6 9 .70 | | 9.64 |
| .68 | | | | - | | | • - |
| 31. 25 .27 | 13064. | 26588. | | | 4.21 | | 1.43 48.95 |
| .80 | 22407. | • | 2.0 | | | | |
| 34.45 | 14159. | 27696. | | • 375 | 4.18 | .485 | 1.43 |
| 02 | 22606. | • | 3.3 | . 186 | • 32 | 1.033 | 56.07 |
| 44.85 | 17496. | 31575. | 450.3 | .196 | 4.33 | .513 | 1.43 |
| 81 | 20841. | • | 3.2 | .069 | .43 | .757 | 27.51 |
| .80 60.85 | 22170. | 41728. | 819.9 | 168 | 4.79 | 682 | 1.43 |
| -1.23 | 11890. | | 12.4 | | .76 | | 4.95 |
| .80 | | | | - | | , | |
| 65.65 | 23443. | 45896. | 911.0 | . 220 | 4.97 | •775 | 1.43 |
| -1.28 | 7931. | •● | 22.8 | .004 | . 84 | . 340 | 3.19 |
| 70.45 | 24617. | 50416. | 966.5 | | 5.06 | .892 | 1.43 |
| -1.32 | 3566. | . • | 33.9 | | .87 | . 307 | |
| .00 | | | | | | | |

TIME.S RANGE, N V, FPS THETA D SPIN SG 74.20 7755. 988. -77.8 .289 1.82



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reduces the effect of changes in $C_{N_{po}}$, and a small and nearly constant yaw angle will reduce the size of the change in magnum moment. We see immediately the value of good obturation in keeping the initial yaw small, and the value of high projectile velocity in keeping the equilibrium yaw small.

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5-2.4.3 Further Discussion of Magnitude of Modal Voctors and Stability

The following paragraph is taken from Murphy (Ref. 12a):

The requirement that the exponential coefficients be negative throughout the flight is much stronger than necessary in a number of applications. This can be seen by the following example. Consider the case of a specific projectile whose exponential coefficients are strongly negative for $M \leq 2.0$ except for the Mach number interval (0.9, 1.1) where both exponents are positive. Baact numerical integration showed that an initial maximum angle of attack of four degrees for the launch Mach number of two will decay to a tenth of a degree before the Mash number decreases to 1.1. The dynamic instability associated with the transonic velocities then will cause the maximum angle to grow to approximately one degree and then decrease a second time when subsonie stability is established. Thus the "dynamically unstable" projectile has maintained a small angle of attack over the entire trajectory.

5....2.5 Aerodynamic Jump of Spin-Stabilized Projectiles

5-2.5.1 General

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The path taken by a projectile after leaving the muscle of the gan is determined principally by wind, gravity, drift. scrodynamic jump, and, of course, by the direction in which the gun is pointing when the projectile emerges from the muscle

The designer can reduce the sensitivity of the projectile to wind by reducing C_{p} , or balancing drag by rocket thrust; he can reduce the round-toround dispersion due to varying gravity drop by good obturation which reduces round-to-round variations in massie velocity. Drift absuld not vary much from round to round if the projectile yow is hopt small. In this discussion we will simply at wind, gravity, and drift equal to zero, assume that the transverse component of the velocity imparted to the projectile by the gun is negligible, and consider how the designer may reduce the remaining source of inaccuracy, aerodynamic jump.

5-2.5.2 Acrodynamic Jump Dofined

In the absence of wind, gravity, and drift, an average line drawn through the swerving path of the projectile, such that the projectile spends equal times on each side (or all sides) of the line, can be visualized as a straight line which intersects the muscle of the gun. At the muscle this mean trajectory line will make an angle with the line defining the direction of the borr of the gun; this angle is called the "aerodyanmic jump."

Note that the plane of the aerodynamic jump angle can lie in any orientation; jump can be up, down or sidewise. At a vertical target the effect of jump appears as a deviation from the theoretical point of impact, which is computed from the bore sight line, corrected for drift and gravity drop. (In flat firing wind corrections are seldom made; rounds are fired as rapidly as is practical, and the wind effect is assumed to be the same for all rounds).

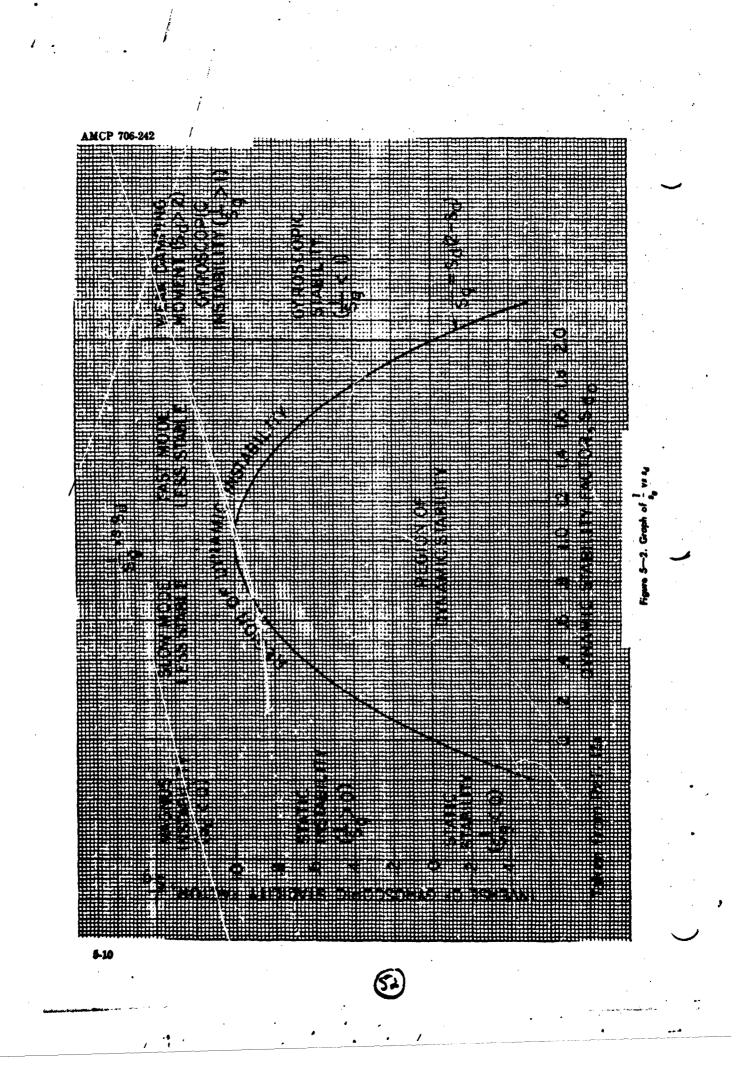
5-2.5.3 Magnitude of Aerodynamic Jump

The aerodynamic jump of a symmetric projectile, in radiana, is given (to a close approximation) by

$$\Theta_{F} = \frac{C_{L_{a}}\delta}{C_{H_{a}}V_{a}} \left(b_{1}^{a}\dot{b}_{a} - ib_{a}^{a}p_{a}b_{a}\right)$$

rhere V. = projectile

and the imaginary multiplier, i, shows that the contribution of initial yaw to jump is at right angles to the direction of the yaw. Asymmetry of the projectile adds another term to the expression for Θ_{A} a term which depends on the size and initial erientation of, the asymmetry; see Murphy, Commonie on Projectile Jump, Ref. 87. It is important



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that projectile asymmetries be kept as small as is economically feasible.

.2, is usually so small that the second term in the jump equation is about an order of magnitude smaller than the first. However, if the bore clearance is unusually large, or if there is a strong cross wind at the gun, the yaw may be large and the second term cannot be neglected.

d, varies from round to round. Good obturation will reduce its magnitude and the magnitude of the variation. For a low drag projectile, $C_{H_{a}}/C_{L_{a}}$ is approximately equal to the distance, in calibers, between the e.g. of the projectile and the e.p. of the normal force. Increasing this distance will reduce Θ_j for a given δ_s but the design changes which increase the c.p.-c.g. separation, such as an increase in the length of the projectile, often also increase k_{i}^{i} . Boatteiling will decrease $C_{L_{i}}$ and increase CH, , increasing the c.p.-c.g. separation without much change in k1. Since drag is also decreased, boattailing has a very beneficial effect on performance unless the stability of the design is impaired; this must be checked (see paragraph 5-2.4.). This discussion of aerodynamic jump applies only to dynamically stable projectiles.

5-2.5.4 Orientation of Aerodynamic Jump

The orientation of the aerodynamic jump angle also varies from round to round, because δ_0 is a vector. The direction of δ_0 depends on the pattern of the gas flow in the mumle blast, which in turn depends on the bore yaw of the projectile. Since projectiles loaded in the gan in the same manner probably ride the lands of the rifling in the same manner (see Ref. 56), the orientation of the blast pressure field, and therefore of δ_0 , is probably biased in one particular direction. Hence the distribution of jump orientation angles, when a group of rounds is fired, is probably sharply peaked in one quadrant.

5-2.5.5 Distribution of Aerodynamic Jump

The distribution of impact points on the target is really a circular (or elliptical) distribution about the theoretical point of impact of all the rounds, assuming no change in gan direction. The bias described in the preceding paragraph produces a hit pattern which appears to be a rectangular distribution about a mean point of impact which is the "center of gravity" of the pattern. Artillery targets are always analyzed as though this were the true situation, since the center of impact and the vertical and horizontal probable errors are very easy to compute from the coordinates of the hits. The location of the theoretical point of impact is very difficult in obtain from the coordinates of the hits and cannot be computed from the boresight line with any certainty, which makes the derivation of the true Θ_d distribution impractical.

The above discussion is presented because of its implications for design descisions based on the results of firing tests. Since the P.E.v and P.E.m method commonly used is theoretically inappropriate, design changes should not be based on small semples, i.e., groups of fewer than 15 rounds. Furthermore, since most design changes are aimed at reducing only the magnitude of Θ_j and not at reducing its directional dispersion, the statistically indefensible procedure of eliminating "maverick" rounds from the error calculations may be justified by the contention that their points of impact on the target were the result of unusual orientations of the jump angle, not large changes in its magnitude.

5—2.5.6 Relationship Botween Aerodynamic Jump and Q.Z.

5-2.5.6.1. Vertical Component

In firing for range, the importance of the vertical component of Θ_j depends on the quadrant elevation of the gun. Differentiating the expression for range in a vacuum gives an approximation of the effect of changes in angle of departure on range.

$$X = \frac{V_{+}^{2}}{\theta} \sin 2\theta$$
$$dX = \frac{2V_{+}^{2}}{\theta} \cos 2\theta, d\theta,$$
$$\frac{dX}{X} = \frac{2}{\tan 2\theta}, d\theta,$$

When $\Theta_0 = 45^\circ$, the change in range is negligible. At $\Theta_0 = 15^\circ$ the change in range, in mils, is about

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3.5 times as great as the change in departure angle (in milliradians) due to aerodynamic jump, so at low quadrant elevations jump is an important factor in range accuracy.

5-2.5.6.2 Herizental Component

The horizontal component of Θ_r produces a horizontal deviation at the point of fall of the projectile, which is proportional to the are length of the actual trajectory. Since the deflection dispersion of rounds fired for range is usually reported in mile based on the mean range, the effect of a given horizontal jump is multiplied by the ratio of the arc length of the trajectory to its horizontal projection. Again we can estimate this ratio from the vacuum condition, giving

$$\frac{Arc}{\overline{X}} = \frac{1}{2} \left[\frac{1}{\cos \Theta_{i}} + \frac{1}{\tan \Theta_{i}} \ln \left(\frac{\cos \Theta_{i}}{1 - \sin \Theta_{i}} \right) \right]$$

and at $\Theta_{0} = 45^{\circ}$, $\frac{Arc}{\overline{X}} = 1.15$, while at $\Theta_{0} = 15^{\circ}$,
 $\frac{Arc}{\overline{X}} = 1.01$. Hence, this factor can be significant
in estimating deflection P.E.'s from aerodynamic
income the $\Theta_{i} > 40^{\circ}$

5-3. FIN-STABILIZED PROJECTILES

5-3.1 General

The inconvenient fact that the center of pressure of the aerodynamic forces on a projectile body is almost invariably forward of the c.g. of the body can be counteracted by placing lifting surfaces (fms) rearward of the c.g. If, when the projectile is yawed, the moment produced by the lift forces on the fins is greater than that produced by the forces on the body, the net moment will oppose the yaw and the projectile will be statically stable. In symbolic notation, we have

$$C_{H_{\alpha}} = C_{H_{\alpha p}} + C_{H_{\alpha p}}$$

$$C_{H_{\alpha}} = C_{H_{\alpha p}} (X_{c.P.p} - X_{c.d.}) + C_{H_{\alpha p}} (X_{d.P.p} - X_{c.d.})$$

$$C.P. - U.G. = \frac{C_{H_{\alpha}}}{C_{H_{\alpha}}}$$

where the subscript B refers to the body and the subscript T refers to the tail. Unsubscripted quantities apply to the whole projectile. The X's are distances in calibera, measured from the base of the whole projectile, which is usually the base of the tail. The tail comprises all of the fins and the (usually) cylindrical boom on which they are mounted. Arrow or subcaliber projectiles have the fins mounted directly on the body, so the base of body, base of tail, and base of whole projectile may coincide. Folding fins may require an arbitrary definition of their base location, depending on the design.

5-3.2 C.P.-C.G. Separation

It will be noticed in the above equations that $X_{GP,\varphi} = X_{GG}$ is negative, and $C_{H_{e}}$ will be negative if the projectile is statically stable. C.P.-C.G. is then also negative, but this quantity is often referred to simply as "e.p.-e.g. separation," in calibers, and treated as though it were unsigned.

The optimum magnitude of the c.p.-c.g. separation is not well defined. For minimum sensitivity to murale blast the tail moment coefficient.

$$C_{\mathbf{Z}_{\mathbf{G}_{-}}}(\mathbf{Z}_{\mathbf{G},\mathbf{P}_{-}}-\mathbf{Z}_{\mathbf{G},\mathbf{G}_{-}})$$

should be small; to minimize the yaw angle due to projectile asymmetries, the total static moment coefficient, $C_{H_{\alpha}}$, should be large. The writer believes that the design value of the c.p.-c.g. separation should be far enough above 0.5 caliber that inaccuracies in estimation of $C_{H_{\alpha}}$ and $C_{H_{\alpha}}$, including the effects of manufacturing variability, will not reduce the c.p.-c.g. separation of any round below 0.5 caliber. On the other hand, c.p.-c.g. separations greater than one caliber have been found to be accompanied by increased dispersion at the target.

5-3.3 Fin Type

The choice of fin type is obviously a trade-off problem, involving the utilities of projectile volume, range, accuracy and cost. Retablishing trade-off curves for each design, determining optimum points for each design, and then comparing the optima would be a long process. It is doubtful that the choice will ever be made explicitly in this way, but the intuitive marrowing of choices must follow

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these lines. A brief discussion of the types of fins follows.

5-3.3.1 Fixed Fins

Fixed fins of one caliber span are easy to make, and easy to make uniformly; this promotes accuracy. However, space is required between the leading edge of the fins and the location of the full body diameter in order to reduce fin-body interference and allow the fins to develop their expected lift. This reduces the projectile volume-tolength ratio. If low drag is important, the long boattail required further reduces the useful projectile volume.

5-3.3.2 Felding Fins

Folding fins which are bunched behind the projectile when in the gun tube and fanned out to more than one caliber span by some mechanism after the projectile has left the muscle blast can produce large e.p.-c.g. separations without large muscle blast effects. They are expensive and conducive to large projectile asymmetry. They need not reduce the volume-to-length ratio of the projectile as much as do fixed fins.

Folding fins which are wrapped around the projectile near its base when in the gun tube and spring out after the projectile leaves the murile, can produce the required stability with reduced sensitivity to muscle blast and very little reduction in projectile volume. They are not cheap; the asymmetry they produce can be offset by a large $C_{\rm He}$.

5-3.4 Obturation

Good obturation is important for both spinand fin-stabilised projectiles, especially so for the fin-stabilised rounds. It has been achieved by the use of rubber or plastic rings on or near the cylindrical portion of the body, or by the use of a $^{-1}$ \pm of suitable material placed behind the projectile (pusher obturator). The obturator is sometimes given the added function of holding folding fins in the closed position; the obturator must then break up on emergence from the muscle, usually no problem with rubber or plastic obturators which can be notshed or, if necessary, segmented. Obturators ou mortar projectiles must break-up into small nonlethal fragments on emergence; this behavior may be required for other weapon systems. Obviously, rets'ning the obturator in flight increases the drag.

, s'in-stabilized projectiles are often fired from rifled guns. The obturator must be designed to fill the grooves of the rifling, but it must not impart a high spin to the projectile. Friction between obturator and projectile will impart a slow spin which is usually remarkably uniform from round to round, and which can to some extent be controlled by the designer by varying the material of the obturator and the area of its surface of contact with the projectile.

5-3.5 Arrow (Subcaliber) Projectiles

5-3.5.1 General

The large mumb energy obtainable with large caliber guns offers the possibility of launching a light projectile at very high velocity. If the light projectile is reduced in caliber, its weight per unit deceleration due to drag would be so great as to soon reduce its velocity below that of a heavy projectile fired from the same gun. But if the light projectile is reduced in caliber its weight per unit of frontal area (sectional density) can be increased up to the point at which it becomes a useful item for employment against armor, owing to its high striking velocity. Since these subcaliber projectiles are usually very long in proportion to their diameters, they must be fin-stabilized; they are referred to as "arrow" projectiles.

5-3.5.2 Sabot

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The space between the subcaliber projectile and the gun barrel is filled by an annular device called a "sabot." The fins, attached to the body near its base, have a span equal to the gun caliber so that they and the sabot, which is usually placed near the c.g. of the projectile, form two riding surfaces which keep the bore yaw of the projectile small.

If the projectile is propelled by a pusher obturator, the sabot has only a centering function and can be relatively light and lightly attached to the projectile. However, the abot must often provide the obturation and transmit most of the accelerating force to to the projectile since the sabot

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area is often greater than the base area of the projectile. The sabot is then heavy, and attached to the prejectile by means of grooves around the projectile body. These grooves naturally give rise to aboek waves which increase the drag. If fired from a rifled tube, provision must be made for rotational alippage between obturator and projectile. The sabot must leave the projectile by break-up or segmentation shortly after leaving the mussie because its drag would be intolerable. Fraements of the sabet may strike the fins, so the fin, must be strong. For this reason, and to improve the riding of the fins on the interior surface of the can tube, the fins are often end-plated. While the transverse plates on the taps of the fins success. the drag, they also increase the lift of the finit. permitting a reduction in fin area which largely effects the drag of the plates. Some interesting sphot designs are described by Alian in BRL Rept. 1005 Part I (Ref. 61).

MacAllister and Roschite (Ref. 63) compiled and analyzed the drug data obtained in several ballistic range firings of arrow projectiles. They found that the addition of four one-celiber square taildan to a tru-caliber some-cylinder body increased the drug to about 160% of the drug of the body alone, when the fin thickness was 5% of the fin cord. When the fin thickness was 5% of the fing merusared to about 220% of the body-alone value. When these fins were canted 2° the drug increased by an additional 30% of the body-alone tail value. These large ("a, values are made televable by the fact that they are based on the diameter of the dender body.

S-ISJ Accolations

Because of the high velocity of the arrow rounds, the arrow/ranger forces and measures to which they are subjected one because in large as to cause a long, stender projectie to deferm in Eight into a slight here. Some the forces change direction as the projectile yor's and rolls slowly, the howing deflection because an cardination wheels loads to the publiship of removed magnification. Hold bedom are not likely to give treation budy in loads to the asignificant perton of the budy in this walled, the astrue frequencies of the budy vibrating as a red destife to advised and compared with the particip frequency $\sqrt{-\mu/l_{p_i}}$ is radians per second. Large deformations increase the drag of the projectile even if they do not threaten its integrity.

5-3.6 Dynamic Stability of Fiz-Stabilized Projectiles

5-3.6.1 General

As documed (at greater length) in the subsection on spin-stabilised projectiles, a projectile is said to be dynamically stable if its treasient yaw does not increase during flight. Statically stable fin-stabilised projectiles having zero spin are always dynamically stable; the yaw, which is planar, decars according to the expression

when

$$\lambda = -\frac{\rho M}{4m} \left[C_{L_0} - C_{\rho} - k_i^{\sigma} \left(C_{M_0} + C_{M_0} \right) \right]$$

s in the travel is calibers, and &, in the constant yaw due to projectile asymmetry, or "trim angle." The additional yaw which arous from the curveture of the trajectory is nightable for normal trajectories.

S-3.6.2 Zero Spin

A condition of zero apin almost zeros exists unce manufacturing tolerances permit same alight twint of the fine resulting in a spin producing torque. In fact, zero spin is very undesirable, berouse then the lift produced by the trim angle, δ_{ii} will steer the projectile away from its predicted trajectory, this deflection due to asymmetry on be satalerably great if the roll rate of the projectile is zero are sero over much of the trajectory.

S-J.6.) Zquilibrum Roll Rate

5-3.6.3.1. Equilibrium Spin

Nearly all finatabilised projection are doserved to argume a vertain equilibrium upin, called a dow opin bi-1.......it is much emailer than the roll rotes used for upon 0.201-leasture. The spin targue is

generally produced by "canting" the fins, or, if the projectile is recket-assisted, may be produced by canting the recket presses.

5-3.6.3.2 Tergas

When the tarque is produced by twisting or cambering the fins, or by canting, i.e., bending up a portion of each fin, the spin tarque is produced by the lift of the fins, which acts in opposite directions on opposite sides of the projectile axis. The angle at which the air flow over the projectile strikes the fins depends on the spin rate; as the spin rate increases, the angle of attack of the canted partion of the fits decreases and the spin tarque decreases until it just balances the decelerating tarque produced by skin friction.

5-3.6.3.3. Computation of Equilibrium Roll Rate

This equilibrium roll rate is given by

$$p_{i} = -\frac{C_{ij}}{C_{ij}}\frac{V}{d}k_{i}$$

where 9,

p. = equilibrium roll rate, rad/see C_{I_0} = roll moment coefficient due to fin

cant (at zero spiz)

 C_{i_p} = roll damping moment coefficient A_{i_p} = fin cost angle, radians

 C_{i_0} is a function of the personnage of fin area which is canted; C_{i_0} is alwaye negative. This expression is useful when C_{i_0} has been determined in a wind tunnel test. However, C_{i_0}/C_{i_0} may be estimated from the approximation, valid only for fine with a tip radius at kast three times as great as the past radius,

$$\frac{C_{i_{1}}}{C_{i_{1}}} = \frac{2d}{b\left[12\frac{b^{2}C_{i_{1}}}{b^{2}\frac{b^{2}C_{i_{1}}}{b^{2}\frac{b^{2}}}{b^{2}\frac{b^{2}}{b^{2}\frac{b^{2}}{b^{2}\frac{b^{2}}{b^{2}\frac{b^{2}}{b^{2}\frac{b^{2}}{b^{2}\frac{b^{2}}{b^{2}\frac{b^{2}}{b^{2}\frac{b^{2}}{b^{2}\frac{b^{2}}{b^{2}\frac{b^{2}}{b^{2}\frac{b^{2}}{b^{2}\frac{b^{2}}{b^{2}\frac{b^{2}}{b^{2}\frac{b^{2}}}{b^{2}\frac{b^{2}}}{b^{2}\frac{b^{2}}}{b^{2}\frac{b^{2}}}{b^{2}\frac{b^{2}}}{b^{2}\frac{b^{2}}}{b^{2}\frac{b^{2}}}{b^{2}\frac{b^{2}}}{b^{2}\frac{b^{2}}}{b^{2}}\frac{b^{2}}}{b^{2}\frac{b^{2}}}{b^{2}\frac{b^{2}}}{b^{2}\frac{b^{2}}}{b^{2}}\frac{b^{2}}}{b^{2}\frac{b^{2}}}{b^{2}}\frac{b^{2}}}{b^{2}\frac{b^{2}}}{b^{2}\frac{b^{2}}}{b^{2}\frac{b^{2}}}{b^{2}}\frac{b^{2}}{b^{2}}\frac{b^{2}}}{b^{2}}\frac{b^{2}}}b^{2}}b^{2}b^{2}\frac{b^{2}}{b^{2}}\frac{b^{2}}}{b^{2}}\frac{$$

where C_{hap} is the fin lift coefficient slope based on fin area, C_{hap} is the roll damping moment coefficient of the body slows, F_{re} is the total fin area (not the writed area, which is twice as great) and S_{max} is the total control area. Hence the rolls S_{max}/S_{pa} is the properties of fin area which is control. S is freezed area, b is fin area and d is maximum discurse of the body. AMCP 706-942

5-3.6.3.4 Sample Calculation

Per example, a 6-meh projectile with enccaliber fins (b = d) might have the following characteristics:

$$C_{L_{a_j}} = 2.0 \text{ per radian}$$

$$C_{L_{a_j}} = -0.02$$

$$S = 0.196 \text{ ft}^2$$

$$S_{res} = 0.5 \text{ ft}^2$$

$$S_{rest} = 0.1 \text{ ft}^2$$

$$\delta_{res} = 4^2 \approx 0.073 \text{ radian}$$

$$V = 1600 \text{ fps}$$

$$\frac{C_{i_0}}{C_{i_0}} = \frac{3}{12\left[\left(\frac{0.196}{0.5}\right)\left(\frac{-0.02}{2.0}\right)\right] - 1} \left(\frac{0.1}{0.5}\right) = \frac{0.6}{-1.05}$$

= -0.57
and $p_* = 0.57 \left(\frac{1600}{0.5}\right) (0.073) = 122 \text{ rad/asc}$
= -21 ray/asc

This calculation is not very amaitive to $C_{L_{\alpha_j}}$, which can be estimated by the expression

$$C_{L_{n_{j}}} = C_{H_{n_{j}}} \frac{S}{bs}$$

where b = span of fins, and c = average fin chord.If the fins have more than 45° sweephask, the above expression for C_{ig} / C_{ig} may not give a unable value.

5-3.6.4 Computation of Dynamic Stability

5-J.4.1 General

It is important to have a good estimate of the equilibrium spin since the likelihood of dynamic instability increases with increasing spin rate. This is often expressed by saying "the spin rate must be hept low enough to avoid magnus effects." Murphy's dynamic stability factor, so, was discussed in paragraph \$-2.4. This method at displaying the dynamic stability of a projectile can be extended, without change", to stationally stable projectiles; the complete curve of 1/s, ve so is shown in Figure 5-2. Pay fin-stabilised properties,

"Brough to ask that for do-antilized projection the designing expression, by and by are approximately equal.



 s_r in negative since $C_{H_{co}}$ is negative. For small volues of spin, s_r approaches zero and $1/s_r$ becomes a large negative number. Hence, the possibility of dynamic instability is small when the spin is small.

5-3.6.4.7 Sample Calculation

Our 6-inch finner used as an example in the discussion of spin due to fin. cant in preceding paragraphs might also have the following characteristica:

$$I_s = 0.15 \text{ sing-ft}^3$$

$$I_y = 3.0 \text{ sing-ft}^3$$

$$C_{H_y} = -2.5 \text{ per radii}$$

Then we have .

$$\frac{1}{4_{p}} = \frac{4J_{p} \stackrel{f}{}_{1} V^{2} Sd C_{H_{p}}}{I_{2}p^{2}}$$

$$= \frac{(4) (2.0) (.00119) (1800)^{2} (0.196) (0.5) (-2.5)}{(0.15)^{2} (132)^{2}}$$

Using Murphy's criteriou

$$\frac{1}{4_0} = a_{4_0} (2 - a_{4_0}) \text{ for } \lambda_1 = \lambda_0 \leq 0$$

we find that the projectile of this example is dynamically stable if s_{a_0} lies between --2.8 and +5.8. It should not be different to design a fastabilized projectile with a value of s_{a_0} lying between three limits.

5-3.6A3 Megnes Boundt- Coelleints

Platen, Ref. 45, points out that blanksting of the lowward firm by the body, when a slowly rolling projectile is yowed, can create an unbalanced aids force which is identified as a magnum force. This force, and the memoral associated with it, can be as large as the memoral associated with it, can be as large as the memoral associated with it, can be as large as the memoral associated with it, can be as large as the memoral associated with it, can be as large as the memoral associated with it, can be as large as the memoral associated with it, can be as large as the memoral force and memoral as reptily spinning body of reveletion. If the fan are conted, the fin lift, at equilibrium spin, is in opposite directions on the inheard and outband sections of the fin, hading to a mealmar variation of "magnet" memoral with you. In any ense, the magnus moment coefficients of fin-stabilized projectiles are less predictable than those of spin-stabilized projectiles. For this reason it is wise to allow as great a margin of dynamic stability as can be secured without falling into ressoance instability, which is discussed in the next paragraph.

5-3.7 Researce Instability

While spin-stabilised projectiles can theoretically experience coincidence of spin and yaw froquencies, this phenomenon is as much more likely to occur with fin-stabilised projectiles that it is discussed here.

5-3.7.1 Variation of Magnitude of Yaw with Asymmetry

 $K_{*} = \frac{A}{P - P + M}$

Murphy (Ref. 12a), in his discussion of the angular motion of a alightly unsymmetric missile, shows that the magnitude of the yaw due to asymmetry is usually well approximated by

where

$$= \frac{2e^2}{V}$$
 spin in radians per
subher of travel
$$= \frac{I_e}{I_e} \frac{2e^2}{V}$$

$$f = \frac{e^{2e^2}}{2I_e} C_{H_e}$$

and A is a constant which depends on the kind and degree of asymmetry.

If the denominator is act equal to zero and solved for a, the result in

$$i = \frac{p}{2} \pm \sqrt{\frac{p_1}{4} - M}$$

but this is precisely the expression for the fraquencies of the two model vectors of yow (Ref. 12a). So if either the nutational frequency or the presentional frequency is nearly equal to the spin frequency, the magnitude of the yow due to agrometry can become very large. The similarity to a spring-mass system enhjorted to an external alternating force has led to the use of the term "rusenance instability" as a label for this mechanism for yow increase. The increase in yow, unlike the growth of the amplitude of an ordinary spring-mass muters, is bounded not as much by the damping in the spatent as by its nonlinearity; the resonant yew of projectiles may become large enough to ensue less of range and accuracy through large drag increases, but not so large as to came the projectile to tumble.

5-3.7.2 Basenance Nell Rate, p.

5-3.7.2.1 Computation

The spin is most likely to coincide with the antation frequency of, which is given by

$$\phi_1' = \frac{P}{2} + \sqrt{\frac{P^2}{4} - M} = \frac{P}{2} \left(1 + \sqrt{1 - \frac{1}{4}} \right)$$

Siace

for resonance, then $\frac{2l}{2}$ = 1 + $\sqrt{1-2}$

 $\frac{dI_1}{I_1} - \frac{dI_n}{I_n} + 1 = 1 - \frac{1}{4_0} = 1 - \frac{dI_n}{I_1^2} - \frac{\mu}{p_1^2}$ This reduces to

where $\mu = \phi I_{c}C_{H}$, is the static moment faster per radius, and μ , is the resonant roll rate in radius per second. When I_{μ} is greater than I_{μ} which it always is for conventional artillery projection, μ must be segnive for resonance, and only statically stable ($C_{H,\mu} < 0$) projections can exhibit resonance instability. We can estimate the resonant roll rate from

$$n = \sqrt{\frac{-p}{L_r - I_r}}$$

which is seen to be just alightly higher than the word approximation for the yawing frequency of a fin-stabilized projectile, $\sqrt{-\rho/L_p}$ in radians per second.

5-87.2.2. Sample Calesimire

For the Sinch famor and as an example in paragraph 5-5.5

$$P_r = \sqrt{\frac{750}{3.0 - 0.15}} = 16.2 \text{ rad/sec}$$
 fps at see
level

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The equilibrium roll rate p, for this finner was 133 rad/me, as p, is well above p. Since both p, and p, are directly propertional to airspeed, changes in V along the trajectory do not alter the p./p. ratio.

5-3.7.2.3 Ratio of Po /Pe to Avoid Resonance Instability

It will be seen from the expression for μ that decreases in air density with altitude decreases p_r ; if the equilibrium roll rate is greater than p_r , fring at high quadrant elevations will decrease the chance of renonance instability. Therefore, in firing from a rifled gun, the obturator should be designed to produce a roll rule at emergence from the mumile at least three timis as great as the calculated renonant roll rate, p_r , and the fine should be designed for an equilibrium spin $(n_r = p_r d/V$ about the same as the spin at emergence. The n_r of our 6-inch finner, 0.061, is unaccessarily high in view of its n_r of 0.005; either the fin east angle or the percentage of fin area cauld be out in half.

Conventional projectiles fired cross a smoothbere gen emerge from the muscle with constially zero spin. Since normal manufacturing asymmetry can produce equilibrium roll rates clear to resonance, the fine are usually canted to produce a p_i greater than p_i . The roll rate of the projectile must therefore pass through p_i on its way to p_{ij} if this parage is rapid enough, the temperary growth in yow due to resonance will be negligible. The greater the p_i/p_i ratio, the shorter the time spent in the visibily of p_{ij} unless the disastrous phenomenon call "roll leak-is" occurs.

5-18 Boll Lock-In

Mestaides and others have made an extensive theoretical and experimental study of the beherier of alightly asymmetric projectiles opinning in the asighborhood of remeasure. Some of their work is reported in Role 40 and 51. Resource to these reports checkl be made when designing projectiles which must pass through the resourcest soil subs. Neukassetties and messadory accelynamic

moments not considered in the discussions in this handbook can offset the fin torque, causing the spin to remain at the resonant frequency long enough for the yaw due to as; mmetry to grow catastrophically. Giving the projectile a spin at emergence and at equilibrium—greater than ν_r , is the method recommended in this handbook for avoiding roll lock-in.

All of the material on the aerodynamic jump of spin-stabilized projectiles (paragraph 5-2.5) applies without change to fin-stabilized ammunition, with the exception that the drift of a fin-stabilized projectile is kept small by rolling the projectile slowly. However, it requires very good design and manufacture to keep the aerodynamic jump (and therefore the dispersion) of fin-stabilized rounds to as low a level as that of standard spin-stabilized rounds fired from the same gun. This has been observed many times in test firings of fin-stabilized task rounds, where spin-stabilized rounds were mind as control rounds.

The aerodynamic jump angle Θ_r , is reduced by increasing the c.p.-e.g. separation, as is seen in the equation in paragraph 5-2.5.3. (c.p.-e.g. ~ C_{X_R} / C_{L_R} for small yaw). Unfortunately, if this ineronse is achieved by increasing the moment coefficient of the tail, as by groater fix area or a longer base, then the effectiveness of the fins in the reversed flow existing in the blast zone is increased, with roughting increase in initial yawing velocity. If this increase in δ_r is greater than the iscrease in r.p.-e.g. separation, and it may well be, then the aerodynamic jump is increased, not reduced, by the change in c.p.-e.g. separation.

The e.p. of the normal force on the body alone can be moved rearward by changing the shape of the body; this can increase the e.p. e.g. separation of the whole projectile with little or no change in the tail memoral. If this body change is made by substituting a spike for the opixe, the drag is inoremed.

Pin-stabilized remains are probably more smaitive to transverse pressure gradients in the blast gaps than are spin-stabilized reands. Calculations indicate that the effect of these pressure gradients on aerodynamic jump is minimized if the resultant of the transverse pressures on the projectile passes through the normal flight c.p. of the round. However, since little is known about the distribution of mussle blast pressure in either space or time, the best way to reduce mussle blast effect is to reduce the magnitude and duration of the blast pressures on the projectile by good obturation.

It will be noticed that aerodynamic jump has been discussed only for dynamically stable projectiles where initial yawing velocity and e.p.e.g. separation are the quantities of interest. Finsiabilized projectiles which are statically stable are also dynamically stable unless they have an unusually high roll rate.

5-3.10 Fin Effectivezes at Supersonic Syeeds (Ref. 12b)

With low aspect ratio* fine of the order of 1.0 or less, the span is the predominant factor for producing high normal force coefficients. However, when spans are limited to no greater than one full body diameter, the optimum chord length must be determined. For a fixed span there is a definite limit to the chord length that will give the best combination of normal force and most rearward C.P. The normal force based on body frontal area decreases with increasing Mach number for a constant span and constant chord, and it decreases more rapidly as the chord is shortened. This means that an aspect ratio increases, the effect of Mash number is greater on the fin normal foress. The must efficient chord length appears to be between ralibers .70 and 1.0, dependent on Mash Aughor. The larger shord should be used for the higher Mach numbers.

The effect of leading-edge sweepback is negligible so far as normal force is concerned if constant area and accort ratio is held. From the wing theory the lift within the tip Mash cones is approximately ½ of the two-dimensional value.⁴⁰ This is esued by a pressure leakage around the tips from

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^{*}Aspect ratio is defined harvin as the separat span squared, divided by the expand in area. The aspect in area is the total plan virw area (of a pair of fee) has the area asrepted by the bases. The separat span is the total span has the (arwage) been diameter. "Two-diversities) for theory states that, for emperants

for, the sermal fore theory states that, for dependence, the sermal fore coefficient, based on expected for area, is given approximately by $C_g = 6/\sqrt{2^2} - 1$.

surface is affected by the tip Mach cones, the lower the total normal force will be and the further forward the C.P. will move. If by some method we roukl prevent this premure leakage around the tips, we would be able to two-dimensionalize a three-dimensional surface. Knd plating the flas was attempted. By this method it was found that the fit normal force could be increased as much as 40% depending upon the amount of fin area affected by the end plates and the amount of end plate width. The end plated fin as against the plain tail on the T108 frings had restoring moments 31% greater and much better accuracy. The damping coefficients were also larger for the end-plated tails as against the plain tail, and this canned the more stable round to damp to 1/2 amplitude in fewer cyclan.

the lower to the upper surfaces. If more of the fin

A complete end plate width would be classified as a shrouded or ring tail. Experimental evidence at low Mach numbers showed that the shroud had a strong tendency to choke or block the air flow over the fin surfaces, thereby causing poor flow over these surfaces. This in turn caused poor lifting results. However, since the flight velocities have been raised to high Mach numbers, the tendency for the flow to choke between the fine and shroad is eliminated, and fin normal forces are increased and C.P.'s moved rearward.

The number of fine necessary for optimum normal force appears to be six. Theoretically six fan, acting independently of each other, should give 1½ times the force of four fan, however, experimentally they usually produce only 20% to 30% more, dependent upon Mach number. If more than six fine are employed, the fine interfere with one another so far as the flow fields are concerned, and the normal force suffers.

In order to obtain maximum teil effectiveness, one would want the tail to be in a uniform flow region, i.e., outside of any body wake infinences. This, however, is only passible when using folding fas whose oweep angles are relatively small. For fixed fin configurations (except in the case of arrow projectiles) the fine are operating mainly in the boundary layer flow from the body. Means of giving the fin the most effective hifting surface are to make the supporting body as small as practical, i.e., herep the open to suppert body diameter as large as possible so that a greater pertion of the fin in outside of the body boundary layer, and boattail the main body so that smech uniform flow is prosented to the surface.

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CHAPTER 6

ROCKET-ASSISTED PROJECTILES

6-1. GEWERAL

The kinetic energy which a gun can impart to a projectile is limited by the diameter of the bore, the length of travel of the projectile in the tube, and by the curve of chamber pressure vs travel. The mumle energy can be increased by using a bigger, longer or thicker gun tube, thus increasing the cost of the weapon and, more important, decreasing its mobility. But range is limited by the kinetic energy supplied to the projectile since each foot of trajectory subtracts from the kinetic energy an amount equal in magnitude to the drag force.

To increase range, or to increase the payload carried to the same range, or to increase the velocity at target impact, without decreasing the mobility of the gun, the first step is to reduce the drag coeffrient of the projectile to as low a value as is compatible with the projectile volume required by the projectile's mission. The next step is to add kinetic energy to the projectile in fight.

By increasing the length of the projectile. or by sacrificing some of the warbead volume. a rocket motor can be included in the projectile. The rocket thrust adds kinetic energy to the projectile in flight. The resulting projectile is called a "rocket-assisted projectile," or, equivalently, a "gun-boosted rocket." The burning of the rocket fuel can be controlled, or "programmed," to be less than the drag force, approximately equal to drag, or very much greater for a short period.

The addition of a reaket motor increases the cost of the projectile and increases the storage space required for a given destructive canability. An added limitation on mussle energy is introduced by the maximum set-back acceleration which the propellant can tolerate without crushing, but this limiting acceleration is surprisingly high.

6-2. MOMENTUM LIMITED SITUATION

6-2.1 Variation of Muzzle Energy, Chambes Pressure and Propellant with Weight of Prejectile

Because of the set-back acceleration limit, recket-aminted projectiles are usually made beavier than the conventional ammunition fired from the same gun. The muzzle velocity is then limited by the capacity of the recoil system, and decreases in proportion to the increase in projectile weight. If we use the subscript "std" to identify the -symbols relating to a projectile which is launched at the mussle momentum limit, then

> mV = may Var (constant momentum)

squaring, rearranging, and dividing both sides by two gives

$$\frac{1}{2}mV^2 = \left(\frac{m_{ed}}{m}\right) \frac{1}{2}m_{ed}V^2_{ed}$$
 (mumbe energy decreases).

Equating mumic energy to the interval of the work done on the projectile by gas pressure in the CUN CITO

$$A\int_{a}^{L}P_{a}dl = \left(\frac{m_{eed}}{m}\right)A\int_{a}^{L}P_{eed}dl$$

where

P. m chamber pressure A = bore area

L = bore travel

Assuming the pressure-travel curves have the same shape, $P_o = kP_{e_{abl}}$ and $P_c = (m_{abl}/m)P_{e_{abl}}$ then muzzle energy and chamber pressure, and consequently the weight of gun propellant, are inversely proportional to the weight of the projectile, in a momentum limited situation.

6-2.2 Variation of Setback Acceleration

The netback acceleration, s, is given by

$$a = \frac{P_{s}A}{m} = \frac{m_{sdd}}{m^2} P_{s}_{odd} A = \left(\frac{m_{odd}}{m}\right)^2 \frac{P_{s}_{odd}A}{m_{odd}}$$

so the setback acceleration is inversely proportional to the square of the mass ratio.

6-2.3 Effect of Rechet Additions on Projectile Design Parameters

The reduction in weight, and volume, of gun propellant allows some of the extra length occupied by the rocket motor to be inserted in the space previously occupied by gun propellant. Whether, and how, this is done depends on the characteristics of the gas tube and loading system involved.

Large increases in range require, if warhead volume is not to be severely reduced, an increase in projectile length. Experience has shown that spinstabilized projectiles longer than 6 calibers usually require a high spin rate for gyroscopic stability; in the absence of resket thrust these projectiles slow down so much on a high angle trajectory that their equilibrium yew becomes dangerously large. However, when the projectile velocity is maintained by a rocket which burns searly to the summit of the frajectory, spin stabilization may be used for projectiles as long as 8 calibers, or possibly longer⁶. At 10 calibers, fin-stabilization is almost certainly required.

6-2.4 Effect of Rocket Additions on Accuracy

Long-burning rockets, sometimes called "sustainer" rockets, with thrust approximately equal to drag, can have a proving ground accuracy (no wind) very little worse than a conventional round fired from the same gun. Thrust malalignment, which contributes heavily to the dispersion of fastburning rockets, is a minor factor in the low-thrust rocket. Variation in rocket fuel specific impulse contributes to rocket dispersion and accounts for the alightly inferior accuracy of long-burning rockets compared with conventional projectiles when both are fired in the absence of wind. However, a long-burning rocket is less affected by wind than a conventional projectile, so that combet accuracy of the rocket-assisted round might well be better than the conventional.

Accuracy analyses of rocket-emisted projectiles, both spin- and fin-stabilized, are presented in Bullock and Harrington, Summery Report on Study of the Gun-Boosted Rocket System, Bel. 69. These analyses, with supporting experimental date, are very useful for design; an extensive bibliography in also included. Initial yawing velocity, dynamic unbalance, and wind are identified as the major sources of dispersion of spin-stabilized rockets; thrust malalignment on be significant in cases of high throat and slow spin. Dynamic unbalance is not significant for fanors, but fa asymmetry and thrust malalignment can be if the roll rate is too low; wind is also a major source of dispersion here. The reasons for the rmall windsensitivity of sustainer rockets are also discussed.

* Special tailoring of the e.g. leastion may be required in order to reduce dynamic instal-lity at the mambe and near impact.

CHAPTER 7

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LIQUID-FILLED PROJECTILES

7-L GENERAL

1

Projectiles having an inner cavity which is partially or completely filled with liquid are a special case of the class of projectiles having a nonrigid internal structure. The yawing motion of a projectile has usually such a low energy content that small transfers of energy between the internal parts and the wall of the projectile can increase the yaw significantly. When the mass of the nonrigid part is large relative to the mass of the projectile, as it is in the case of some liquidfilled projectiles, the yaw may increase very rapidly.

The instability of liquid-filled projectiles has been studied, theoretically and experimentally, by Karpov, Scott, Milne, Stewartson and others. Some of this work is reported in Refs. 71 to 73. The investigation is not complete; the statements made in the following paragraphs represent current (1964) concepts and opinions.

7-2. EFFECT OF SLOSNING OF LIQUID FILLER

Differences in the thermal coefficients of expansion of projectile body and liquid make it impractical to completely fill a projectile cavity with liquid. Mechanical devices for allowing the savity volume to change with the change in liquid volume are possible, but not much used. Fills of 36% are common; some projectiles may be filed to 56%.

It has been found that the eloshing about of the fill in a fin-stabilized projectile does not inervase the yew. So a simple solution of the problem of liquid fill is to use fin-stabilization. This is not always femilie; limitations on projectile length may reduce the volume of a finner below acceptable limits, or spin-stabilisation may be desirable for terminal effects.

7-3 COMPUTATION OF DESIGN PARAMETERS

The discussion which follows applies only to spin-stabilized projectiles.

7-3.1 Gyroscopic Stability Pactor

The gyroscopic stability fastor of a liquid-filled projectile is given (approximately) by

$$\epsilon_{p} = \frac{l_{sg}^{1} p^{2}}{4 \left(l_{sg} + \epsilon \, l_{sg} \right) \mu}$$

where

Ing = axial moment of inortia

- of rigid parts, slug-ft² I_{va} = transverse moment of inertis of rigid parts, slug-ft²
 - = a constant related to the viscosity of the liquid; for water, s = 0.3
- le_L = transverse moment of inertia of liquid parts, slug-ft³

= statis moment factor, ib-ft/radian

The rigid parts include both motal parts and high explosive; the transverse measures of inertia are computed about the total e.g. of the projectile, with the liquid fill distributed as a hollow con-

centric cylinder occupying the full length of the cavity.

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7-3.2 Dynamic Stability Factor

The dynamic stability factor—computed in the usual way from aerodynamic coefficients, except that k_{a}^{a} is given by $I_{s_{B}}/(m_{B}d^{a})$ and k_{a}^{a} by $(I_{v_{B}} + cI_{v_{L}})/[(m_{B} + cm_{L})d^{a}]$ —must be such that the projectile would be dynamically stable over its trajectory if there were no interaction between the liquid fill and the projectile wall.

7-3.3 Spin Rate

In the transient period, during which the liquid fill is acquiring a spin rate equal to that of the projectile wall, the transfer of angular momentum from wall to liquid will reduce the spin rate of the wall. The reduction in spin rate may be very rapid if the liquid fill has a high viscosity, or if baffes tied to the projectile wall are placed in the liquid. On the theory of paragraph 7-3.1, above, that the angular momentum of the liquid does not contribute to a_n the projectile may become unstable. However, the transient period is then so short that baffes (or high viscosity) may actually improve the flight. Haffes can be designed simply on the basis of the teeque exertsd on the liquid in giving it angular velocity and on the shear, due to setback, at the roots of the baffies.

7-4. RIGID BODY THEORY

When all of the liquid is rotating with the same angular velosity as the projectile wall, the projectile is said to be rotating as a "rigid body." If the liquid were not all of the same density, the heaviest fraction would be closest to the projectile wall as a result of the centrifugal field, which resembles a gravitational field. The air space, then, is as far away from the projectile wall as possible, surrounding the axis of the projectile or any solid core, such as a burster tube, which may be positioned along the projectile axis.

Stewartoon's theory is concerned with the instability of liquid-filled projectiles rotating as a "rigid body." It was derived for cylindrical eavities completely or partially filled with liquid of uniform density and low viscosity; the behavior of test groups of rounds of varying geometry and percentage of cavity filled has been successfully predicted by the use of this theory. The projectile cavity need not be precisely cylindrical near its ends. The necessary formulas and tables for applying Stewartson's criterion of instability are contained in Karpov, Dynemics of Liquid-Filled Ndell, BRL Memerandum Report 1477 (Ref. 72).

CHAPTER 8

RANGE TESTING OF PROTOTYPE PROJECTILES

8-1. GENERAL.

Very few projectiles are completely satisfactory as first designed. Metal parts failure is rare, but the first test firings usually show that either range or accuracy is not as good as was desired or expected. In instances where the first group of ten or fifteen test rounds fired gave excellent results, a second group has often failed to confirm the good results of the first. Conclusions are drawn from the behavior of the test rounds; design changes are made on the basis of these conclusions; and new prototype rounds are made and fired. This test and change sequence may go on through many cycles before an acceptable design is reached.

The difficulty that a designer may encounter in translating a round from the drawing board into a useful weapon is described in the following excerpt from the report of E. R. Dickinson, The Effects of Annular Bings and Grooves, and of Body Undercuts on the Aerodynamic Properties of a Cone-Cylinder Projectile of M = 1.73 (Bef. 80):

Often, in a projectile's progress from the designer's drafting board to the assembly line, there are many changes made in the details of the projectile's contour. As a result, the actual aerodynamic performance of the projectile may differ from that of the designer's prediction.

Almost all of the basic design data on projectiles concerns itself with smooth contours and simple geometric shapes. When practical considerations enter the picture and fuses have to be atteched, reliefs have to be machined, rotating bands have to be added, a projectile which may have been, originally, an optimum one, often falls short of experiations.

The engineer, who translates the ballistician's

design data into a practical piece of ammunition, should be cognizant of the differential corrections that have to be made to the predicted behavior of the projectile. The purpose of this report (Ref. 80) is to show the effect, on drag, lift, and pitching moment, of depressions and protrusions on the surface of a body of revolution. Unfortunately, there were insufficient data to determine effects on the damping and magnus moments and forces.

Obviously important to the designer is the soundness of the conclusions on which the design changes are based. This soundness is directly related to the care taken in preparing for, firing, and analyzing the firing test.

8-2. PRE-FIRE DATA

It is important that the designer know exactly what was fired and how it was fired. He must know what equipment was used for measuring the test parameters, such as velocity, time-of-flight, and target impact, in order to assess the accuracy of the numbers presented to him. Each round fired must be precisely identified so that its performance can be tied to its physical characteristics as determined before firing.

For each round, the following physical characteristics must be determined and recorded before firing:

- a. Individual weights and dimensions of all of the significant components of the round.
- b. Weight and center of gravity location of the projectile, including its simulated lethal charge.
- c. Amount of eccentricity of specific components relative to a chosen reference axis,

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when assembled into the complete projectile.

- d. Axial and transverse moments of inertia. (Moment of inertia data may be omitted if the projectile is fin-stabilized and it is known from a previous test that dynamic stability is not a problem.)
- e. Surface is regularities which could cause disruption of proper boundary layer flow.
- Round number or other identification, which should be permanently marked on the projectile.

Some experiences in the manufacture of prototype projectiles indicates that there should be no difficulty in meeting the following tolerances:

- a. Projectile weight: ±0.6% design value
- b. Center of gravity location: \pm 0.05 inch
- e. Eccentricity: ±0.008 inch
- d. Moments of inertia: ±2.0% of design value

Practical methods of measurement of projectile characteristics are described in E. R. Dickinson, *Physical Measurements of Projectiles* (Ref. 74).

8-3. TESTING

The primary function of the projectile test faeility is to acquire reliable and unbiased test results. Engineering changes must not be based on emplusions that are statistically unsound; accordingly, the test must be plauned to provide sufficient data for a statistical ansitysic (Ref. 76). It is the responsibility of the testing officer to insure onepletion of the test, as plauned, or to record any condition which will make completion impractical. The two types of tests, static testing and flight testing, are described below.

8-3.1 Static Testing

Static testing is an intermediate design tool, which is particularly useful in determination of the following:

a. Shaped charge penetration

- (1) stand-off distance
- (2) liner design : thickness, cone angle, etc.
- (3) high explosive charge: type, volume, density, shape, etc.
- (6) effect of spin

8-3

- **b.** Fragmentation studies
- c. Smoke tests: chemical type, shape, volume, density, etc.
- d. Rocket motor performance
- e. Propellant and high explosive ignition systems

• Many of these static tests involve design factors which contribute to the mass and mass distribution, and directly or indirectly affect flight characteristics.

8-3.2 Flight Testing

The mission of the projectile determines the type of flight test conducted. The two most common tests are to determine vertical target accuracy and range (distance), each of which is discussed below.

8-3.2.1 Vertical Target Accuracy

8-3.2.1.1 Measurement of Accuracy

For vertical targets, the accuracy is expressed in terms of two probable errors, $P.E_{.H}$ and $P.E_{.V}$. These indicate the distribution, both horizontally and vertically, about a center of impact.

8-3.2.1.2 Temperature Range

Test requests generally specify temperature conditioning of the test projectiles, for a 54-hour period prior to firing. The three temperature ranges usually employed are:

- a. Hot : 125°F b. Standard : 70°F
- e. Celd: -40°F

5-3.2.1.3 Data Recorded

In vertical target accuracy tests the projectiles are fired on a fist trajectory and the following data are recorded:

- a. Projectile identification ; round identification
- b. Gun identification and condition
- e. Changes in gun elevation or azimuth (if any) between rounds
- d. Target distance from gun
- a. Mussie velocity

Not always

observed

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- f. Coordinates of points of impact
- g. Ground level meteorological conditions
- h. Terminal velocity
- i. Time of flight
- j. Chamber pressure
- k. Early yaw

8-3.2.2 Range (Distance) Accuracy

8-3,2.2.1 Measurement of Accuracy

When testing projectiles for distance, the aceuracy is measured in these two ways:

- a. Probable error of range; indicating the distribution forward and aft of a calculated mean range.
- b. Probable error of deflection: indicating distribution to the right and left of the center of impact. Deflection P.E. is generally expressed in mile, based on the mean range.

8-3.2.2.2 Data Recorded

Thuse projectiles are generally tested through a range of quadrant elevations and the following data are recorded:

- a. Gun and projectile identifications as in flat fire
- b. Quadrant elevation and azimuth of gun
- e. Mussle velocity
- d. Coordinates of points of impact or burst

- e. Meteorological data at ground level and aloft
- f. Time of flight
- g. Chamber pressure h. Early yaw
- Not always observed

8-3.2.2.3 Instrumentation

Subsequent field tests may be conducted under localized weather conditions, such as at the Arctic Test Branch, Big Delta, Alaska. Instrumentation available for recording flight data are:

- a. Photography: Pictures taken at muscle show growth of amoke cloud which is related to adequacy of obturation. Sequence photos record discarding sabots or record spin activity.
- b. Yaw Cards: The projectile is fired through a series of strategically located soft-cardboard panels to record the attitude of the projectile relative to its line of flight.
- c. Radiosondes: A small radio transmitter built into the projectile is actuated upon firing. An on-ground receiver, being sensitive to the roll orientation of the transmitter antenna, is able to record the spin history of the projectile.
- d. Radar: Eadar tracking can provide position and velocity data throughout the flight.

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CHAPTER 9

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MANUFACTURING TOLERANCES

9-1. DIMENSIONAL CHANGES

Cost factors necessitate that tolerances on parts being produced in large quantity be less stringent than prototype manufacturing tolerances. Dimensional changes, to facilitate production, may be made only when the flight results will not be significantly impaired by the change; this implies that standards for high production runs can be established only after statistical analysis of prototype firing test data. A brief example of the type of analysis considered is presented below. Reference should be made to the Engineering Design Handbooks, *Experimental Statistics*, AMCP 706-110 through AMCP 706-114, for a thorough treatment of this important phase of data analysis.

9-1.1 Problem

Fin misalignment relative to the longitudinal axis of the projectile is recorded during preflight inspection. The assemblies accepted ε , this time must meet the requirements of prototype manufacturing. After test firing the accepted projectiles, the impact dispersion at target is recorded.

9-1.2 Analysis

A simple regression analysis of fin misalignment versus distance of hit from center of impact will produce numbers indicating the effect of misalignment. If the analysis indicates insignificant correlation, the tolerances on the fin dimensions which control alignment may be relaxed.

9-2. PREDICTED PROBABLE RANGE ERROR

Table 9-1 presents estimates of the probable variability of those projectile characteristics which most significantly affect range. These estimates were gathered from ballisticians at Picatinny Arsenal, Aberdeen Proving Ground, and the Naval Ordnance Test Station. The last column in the table presents sensitivity factors for a particular rocketassisted projectile when fired for maximum range. These sensitivity factors, which represent the percent change in range caused by a one percent change in the associated round variable, were obtained by trajectory computations as described in paragraph 4-2.

The predicted probable error in mange, in percent, due to each variable is therefore the product of the probable error of the variable and its associated sensitivity factor. Under the usual assumption that the errors are independent of each other, the resulting range probable error of the projectile, in percent, is the square root of the sum of the squares of the individual products. Vector sums of this type can be significantly reduced only by reducing their large components. Obviously, a significant improvement in the range dispersion of rocket-assisted projectiles could be obtained by reducing the round-to-round variation in specific impulse. In the absence of rocket thrust, variations in drag coefficient become most significant; dispersion might be improved by closer control of the external contour of the projectile.

The foregoing paragraphs apply to high angle indirect fire. As the quadrant elevation is decreased, the relative importance of the various factors changes so that in direct fire the most important items are quadrant elevation and aerodynamic jump.

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| | ARIABILITY OF ROCKET-ASSISTI ERISTICS AND SENSITIVITY FAC AFFECT RANGE | · · · · · · · · · · · · · · · · · · · | | | |
|----------------------------------|--|---------------------------------------|--|--|--|
| Round Variable | Probable Error as % of Zoon of Variable | Sonsitivity Pactor at mas. ronge | | | |
| Projectile Wright | | | | | |
| Mussle Velocity | 25 | . | | | |
| Pasi Weight | .50 | .76 | | | |
| Puel Specific Impalse | · 1.00 | | | | |
| Past Burning Rate | 01. | .08 | | | |
| Drag Coefficient .51 .77 | | | | | |
| Ballistie Density of air .90 .77 | | | | | |
| Quadrant Elevation | | | | | |

TABLE 9-1

9-1. DYNAMIC STABILITY OF 175-MM PROJECTILE, M437

The trajectory calculations in Table 9-2 show that the M437 projectile first at 45° quadrant elevation and 2000 fpe meanle velocity, will fly at a Mach number close to 1.15 ever the entire doseeding limb of its trajectory. Referring to the accedynamic data in Table 9-3, we see that in this Mach number visualty the expected value of sa in close to 1.0, so that a round having values of the negres moment and damping moment coefficients our to the average values measured for the rounds tested in the free fight range will be dynamically stable over its whole trajectory.

How we, the experimental data from the rea firings showed considerable motter, probably because of the small size of the year level. As a se sequence of this seatter, RRL investigated the sensitivity of the stability of the projectile to variations in the magnes moment and dauping moment coefficients. These variations could arise from lot-to-lot variations in projectile shape or center of gravity beation.

The results of result (1964) siz-degree-of-freedom competer runs at BRL show that the Mi27 projectile behaved properly with variations of over four standard deviations from the curve fitted to the experimental values, but variations of five standard deviations produced instabilities. These remputations, Table 3-4, indicate that other than miner let-to-let variations in shape or e.g. location can lead to trouble even when the basis during of a projectile in quite stable.

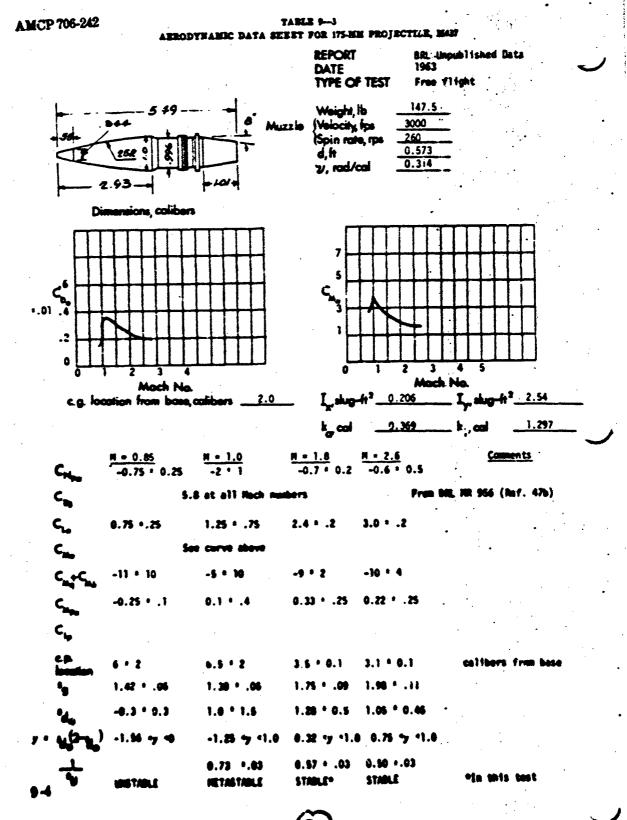
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TABLE 9--2 SAMPLE TRAJECTORY FOR 175-WM SPIN-STABILIZED PROJECTILE, MA37, AT Q.E. = 45*

| 1.000 1. WTO | | YPE RC .175 SPIS TEHP 59. | 569 1.29 SBT .0 DTL | 97 DTH .300 DTE | TWIST 20.00 | CLP | |
|-------------------|--------|---------------------------------------|------------------------------|--------------------------|-------------------|-------|--------|
| .001189 | 1116.0 | | | | | | |
| TINE THETA | X | DI ST THRUST | - | CD YAW | CMA DR Mach Sp | | |
| .00 .78 .06 | • | • | 3000.0 562.1 | . 203 . 000 | 3.62 2.68 | 1.000 | 4 1 |
| 3.46 | 6895. | 9621. | 2577.8 | . 222 | 3.73 | .806 | 4 |

| THE | X Z | DIST THRUST | V DRAG | CD YAW | CMA DR Mach Spi | | <u>.</u> |
|-------------------------------|--------------------|-----------------|-----------------|----------------|--------------------|----------------|---------------|
| .00 .78 .06 | • | • | 3000.0 562.1 | . 203 . 000 | | 1.000 | 4.58 1.95 |
| 3.46 .75 .07 | 6895. 6709. | 9621. · | 2577.8 366.5 | . 222 .C01 | | .806 .342 | 4.58 2.80 |
| 7.92 .71 .10 | 14749. 13815. | 20213. | 2198.8 229.5 | .249 .002 | | . 642 . 379 | 4.58 4.17 |
| 13.64 .64 .12 | 23745. 21066. | 31770. | 1858.3 140.3 | .260 .003 | | . 509 . 428 | 4.58 6.38 |
| 21.01 .52 .16 | 34145. 27972. | 44262. | 1552.6 84.4 | .279 .007 | | .408 .491 | |
| 30.84 .31 .23 | 4%693. 3371.3. | 58090. | 1282.1 50.1 | . 307 .015 | | .322 .572 | 4.58 15.85 |
| 43.01 00 .30 | 60831. 36054. | 72479. · | 1108.3 36.2 | . 332 .023 | | . 289 . 641 | |
| 58.01 43 .30 | 76566. 32435. | 88752. | 1092.1 | .335 | | . 342 , 627 | 4,58 16,30 |
| 73.01 -,78 .30 | 90373. 22521. | 105834. | 1193.4 69.4 | . 326 . 010 | | . 486 . 545 | 4.58 8.93 |
| 68 .01 -1.02 .30 | 101738. 7882. | 124410. | 1265.5 | . 325 | | · 777 · 473 | 4.58 4,21 |
| TIME. S 95.16 | RANCE .H 32333. | V. FPS 1247. | THETA . | .452 | | | |

03



(2

TABLE 9---4 DYNAMIC STABILITY ESTIMATE OF 175-MM PROJECTILE MAN

Projectile Type:

175-mm M437

1.14

Mach aumber: Air density:

 $\rho = 0.000688 \operatorname{slug}/ft^3$ at 36,060 ft above ma level

Average values of acrodynamic coefficients:

| CM. | = 5.0 |
|------------------|---------------|
| C4. | = 1.5 |
| C., | - 0.33 |
| C _{#20} | - 0.25 |
| | = -8.8 |

From Unpublished BRL data 1963

Spin. . = 0.64 rad/oal

Lummeter, d == 0.573 ft

Axial radius of gyration, $k_a = 0.300$ cal

Transverse radius of gyretion, k₁ = 1.297 cal

Projectile man, m == 4.56 slags

Cyressegie stability faster, sp:

 $a_{\mu} = \frac{2mk_{\mu}^{2}}{m^{2}} C_{H_{\mu}} = \frac{2(4.38)(0.300)^{4}(0.64)^{4}}{\pi (1.207)^{2}(4.28)(10^{-4})(0.573)^{2}(5.0)} = 20.8$

Dynamic stability factor, se,

 \therefore Dynamically Stable since $\frac{1}{a_0} < a_0$ (2 - a_0).

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GLOSSARY

- accuracy. The quality of correctness or freedom from error. C! precision.
- accuracy of fire. The correctness of fire as judged by the distance of the center of impact from the center of the target.
- acoustic velocity. The velocity of sound waves, or similar waves, in a given medium. For variation with altitude, in air, we: Standard Atmesphere.
- acrodynamic jump. The average deflection of the trajectory which arises from the alternating lift forem on a yawing projectile. Drift, which arises from a non-zero equilibrium angle, is not included in zerodynamic jump.
- airspeed. The speed of a projectile relative to the air is which it is insurance.

AMC (abbr). Army Materiei Command.

- angle of jump. The angle betw. v. 'to' line of elevation and the line of dynartur'
- angle of yew. The angle termines the direction of motion of a projectile and the direction of its axis. In computing acressing the "process is the presence of a lateral wind the very angle is based on the direction of the relative wind, rather than the direction of motion of the stat.
- atmospheric conditions. Ner: metavological data. azial drag. The component of the asredynamic force on a body in the direction of the longitudinal axis of sympotry.
- azis. Unless otherwise specified, the length dinal axis of symmetry.
- ballistic coefficient. A sumerical measure of thability of a projectile to overcome air resistance. It is dependent upon the mass, diameter and form factor, and was widely used in trajectory calculations before the advent of the electronic digital computer.

- tallistic range. A suitably instrumented area or enclosure in which projectile trajectories can be closely observed, as by park photography; analysis of the observations can yield good estimates of the aerodynamic coefficients of the projectile.
- blast zone. The zone of turbulent air and propellant gaves through which a projectile must fly as it leaves the mumile of the gan. The blast zone ends where, and when, the projectile enters undisturbed air.
- beattail. The base of a projectile when shaped like the frustum of a cone (a: like a reversed agive). (if: square base.
- boom. The central stalk or sloove to which the fins of a fin-stabilized projectile are attached.
- bore. The interior of a gun barrel or tube.
- boundary layer. A this layer of air (or other fluid) next to a body, distinguishable from the main flow by characteristics of its own, set up by friction. The layer within which the major effects of viscosity are concentrated.
- bearrelet. The cylindrical surface of a projectile on which the projectile bears while in the bore of the wespen. Conventionally the bourrelet is located just aft of the eqive and has a slightly larger diameter than the main body. In some cases the bourrelet antends the full length of the cylindrical body. In some designs a middle bourrelet is provided just forward of the rotating band. In some other designs a rear bourrelet is provided behind the rotating band, and in finstabilised designs a shread or end plates on the fine provide a rear bourrelet.
- Nonrrelat diameter. The maximum diameter of the projectile. The frontal area used in the computation of accodynamic coefficients is based on this diameter.

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GLOSSARY (cont'd)

- bow wave. A shock wave caused by the compression of air ahead of a projectile in flight. When this wave touches the tip of the nose of the projectile. it is called an "attached bow wave" or "attached shock."
- BRL (abbr). U.S. Army Ballistic Research Laboratories.
- turning rate. For solid propellant fuels, the rate of motion of the burning surface (normal to itself).
- burnout. The termination of combustion in a rocket motor owing to exhaustion of the propellant supply.
- calibar. The diameter of a projectile or the diameter of the hore of a gun. In rifici arms, the caliber is measured from the surface of one land to the surface of the land directly opposite. Often the caliber designation is based on a nominal diameter and represents a close approximation rather than an exact measurement.
 - Caliber may be used as a unit of length; for example, a 6-inch 50-caliber gun (6"/50) would have a hore diameter of 6 inches and s tube length of 50 calibers or 25 feet, measured from the breech face to the maxie.

calotte. See: miylat.

- unter of impact. Conter of the dispersion pattern. Calculated as though it were the conter of gravity of a system of discrete unit masses placed at the points of impact of the individual rounds of the group.
- easter of pressure. The point on the axis of a projectile (or on the chord of a fin) through which the resultant of a given set of seredynamic forces bases.
- chamber pressure. The pressure existent within the gun chamber at any time as a result of the burning of the propellant charge. This pressure normally varies from atmospheric pressure to a peak pressure which is attained when the projectile has traveled a short distance, then decreases steadily until the projectile emerges from the muzzle. In this hardbook *P*, is identified with the pressure existing at the base of the projectile, although the two pressures are not exactly equal, the base pressure being perhaps 5%

smaller than *P*, after the projectile has acquired a large fraction of its final velocity.

complete round. All of the components of ammunition necessary to fire a given gun once.

control rounds. See: reference rounds.

- damping exponent. A numerical measure of the rate of change of the amplitude of an uncillating motion.
- deflection probable error. The directional error, caused by dispersion, which will be exceeded as often as not, in a large number of rounds fired at a single gun setting. It is approximately oneeighth the greatest width of the dispersion pattern (for large samples).
- density of air. The max of a unit volume of air. It varies with altitude, generally decreasing as the altitude increases, since it varies with the current temperature and barometric pressure. When b is altitude in feet (b < 30,000) above we level, in $(\rho_{\mu}, \rho) \approx 3.2 \times 10^{-6}$ k. ρ_{μ} the standard density of dry air at 59°P and 14.7 psi, is 0.002378 slug/ft³ (NACA 1942).
- derivative. The rate change of one variable with respect to another. In projectile aerodynamics, the rate of change of an aerodynamic coefficient with respect to a change in the magnitude of the yaw angle, e.g., the slope of the C_H vs a curve gives the static moment derivative, $C_{H_{co}}$.

differential coefficient. See: manifivity factor.

- differential effects. The effects upon the elements of the trajectory due to variations from standard runditions.
- dispersion. The scattering of shots fired on a target by the same gan (or group of gams).
- dispersion error. Chance variation in a series of shots even though firing conditions are kept as constant as possible. For practical purposes the dispersion error of a particular shot is considered the distance from the point of impact or burst of that shot to the center of impact or burst.
- dispersion pattern. The distribution of the points of impact of a series of shots obtained under conditions as nearly identical as possible.
- distribution. Pattern of projectiles about a point. The art of values taken on by a random variable is successive trials.

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GLOSSARY (cont'd)

- diverging yaw. In the flight of a projectile, if the angle of yaw increases from the initial yaw, the yaw is said to be diverging.
- drag. Component of air resistance in the direction opposite to that of the motion of the center of gravity of a projectile.
- drag coefficient. A number relating drag force to the dynamic pressure of the air stream and to the frontal area of the projectile.
- drift. The lateral deviation of the trajectory of a spin-stabilized projectile, due to the equilibrium yaw.
- dynamic pressure. The pressure exerted by a fluid solely by virtue of its relative motion when it strikes an object. Proportional to density and the square of relative velocity $[q = (\frac{1}{2}) \rho V^2]$, it is obviously related to the kinetic energy posensed by, or imported to, the fluid. Sometimes called "velocity head."
- and plats. A narrow rectangular plate integral with the tip of a fin, forming a T when viewed in the chordwise direction. The other surface of the plate is curved to conform to the radius" of the gun bore, as the end plate supplies a riding surface for the fin in the barrel, as well as increasing the lift of the fin by preventing the flow of air around the fin tip from the lower to the upper surface.
- equilibrium yaw. The yaw angle to which the yaw of a dynamically stable projectile decays. Part of this angle is due to asymmetry of the projectile, part to the effect of gravity.
- error. 1. The difference between an observed or ealeulated value and the true value. 2. In gunmery, the divergence of a point of impact from the center of impact.
- **Encases** ratio. Ratio of length to diameter (l/d) of a projectile.
- fn-stabilized. Of a projectile, made statically stable by the aerodynamic moment arising from the primence of lifting surfaces aft of the c.g.
- fring table. Table or chart giving the data needed for firing a gun accurate'y on a target understandard conditions and also the corrections that must be made for special conditions, such as winds or variations of temperature.

fat base. Descriptive of a projectile with a cylin-

- drical have section, as opposed to a beattail, which see. Nometime called "square base."
- form factor. Factor introduced into the denominator of the hallintic coefficient (q.v.), based on the shape of the projectile.
- free stream. The flow of air or other fluid undinturbed by the presence of a (relatively) moving hody; specifically the relative flow of air ahead of a shock wave.
- fringing groove. A groove cut into a rotating band to collect metal from the band while it travels through the bore. Excess metal as collected is prevented from forming a fringe bohind the rotating band. Fringe formation has been a cause of excess dispersion and short range.
- frontal area. The area of the greatest circular cross-section of the body of a projectile $jS = (\pi/4)d^2$; used as the reference area in defining the serodynamic coefficients.
- gravity drop. In ballistics, the vertical drop due to gravity ; equal to one-half the acceleration due to gravity multiplied by the square of the time of flight.
- HEAT (abbr). High explosive antitank. A term used to designate high explosive ammunition containing a shaped charge.
- hit. An impact on a target by a projectile.
- hit probability. The expected ratio of number of hits to number of projectiles fired at the target.
- HVAP (obk.). Hypervelocity armor-piercing.
- hypersenic. Of or pertaining to the speed of objects moving at Mach 5 or greater.
- impact velocity. The velocity of a projectile at the instant of impact on the target or target area. Also called "striking velocity."
- impulse, total. In rocketry, the product of the average thrust (in pounds) developed by the motor, times the burning time (in seconds).
- increment. An amount of propellant added to, or taken away from, a propelling charge of semifixed or separate loading ammunition to allow for differences in range.
- indirect fire. Gunfire delivered at a target which cannot be seen from the gap position.
- inhibitor. A material applied to surfaces of propellant grains to prevent burning on the control surfaces.

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GLOSSARY (cont'd)

- initial mass. The mass of a rocket-mainted projectile at the start of burning of the rocket propellant.
- initial yaw. The yaw of a projectile as it leaves the muzzle blust zone.
- initial yawing velocity. The rate of change of the yaw of a projectile as it leaves the muzzle blast zone.
- jump. 1. Movement of a gun tube when the gun is fired. 2. Angle of jump (q.v.). See: aerodynamic jump.
- **hill probability.** Probability (P_x) that, given a hit, a single projectile will kill (i.e., destroy) the target against which it is fired. The overall kill probability of a single shot is the product $P_H P_x$, where P_H is the hit probability, summed to be independent of P_H .
- instant flow. A nonturbulent airflow.
- land. One of the raised ridges in the bore of a rifled gun barrel.
- Interal deviation. Horizontal distance (normal to the line of fire) between the point of impact of a single round and the center of impact of the group.
- lift. The component of the total aerodynamic force perpendicular to the relative wind, and acting in the plane of yaw.
- line of departure. The path of the projectile as it leaves the mumle; the direction of the projectile at the instant it clears the mumle of the gun, providing it has no swerving motion.
- the of elevation. The prelongation of the bare when the gan is set to fire.
- legarithm, natural. Defined by $x = e^{ix}$, where e = 2.71828...
- lot. Quantity of material, the units of which were manufactured under identical conditions.
- M (abbr). 1. Mach number. 2. In such unge as M29, designates a standardised item.
- Moth. (Named for Brast Mach. 1838-1916, Austrian physicist.) Prequestly used for Mach number, which see.
- Mach angle. The scute angle between a Mach line and the line of flight of a moving bady.

$$\theta_{W} = \tan^{-1} \frac{1}{\sqrt{M^{2}-1}}$$

Mach effect. An effect resulting from the fact that an object is moving at transonic or supersonic speed; a compressibility effect. Mach effect may be considered in terms of (a) The changes in the air brought on by a shock wave, i.e., changes in pressure, velocity, density and temperature and (b) Changes in aerodynamic coefficients, such as drag, lift, and moment coefficients.

- Mach line. A theoretical line representing the backsweep of a cone-shaped aboek wave made by an assumed infinitely small particle moving at the same speed and along the same flight path as an actual body or projectile. This line, as represented on any plane bisecting the shock-wave cone, forms an angle with the flight path usually somewhat more acute than the angle formed by the shock wave of the actual body, which depends among other things upon the shape of the body.
- Mach number. The ratio of the velocity of a body to that of nound in the medium being considered. Thus, at sea level in the U.S. Standard Atmosphere, a body moving at a Mach number of one (M = 1) would have a velocity of 1116.2 fps (the speed of sound in air under those conditions).
- Mach number, critical. The free stream Mach number at which the relative speed of air and projectile attains sonic velocity at some point on the projectile.
- Mach number, free stream. The Mash number computed on the basis of the velocity of the projectile relative to air which is undisturbed by the prosence of the projectile.
- magnus force. The lateral thrust on a rotating body when acted on by an airstream having a velocity component sormal to the body's axis of rotation.
- magnus moment. The moment about the body e.g. produced by the magnus force.
- men. The constant of propertionality between the force on a body and the resulting acceleration. m = W/g. Unfor cunately, in previous references, "man" in sometimes used as symenymous with "weight."
- notorial. In a rostricted asses, these things used in combat or legistic support operations, such as weapons, ammunition, motor vohision, etc.

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- man range. Average distance reached by a group of shots fired with the same firing data.
- méplat. The flat nose formed by truncation of the ogival portion of a projectile or point fuze. Nometimes the méplat is convex, and may be eailed a "ealotte."
- meteorological data. Facts pertaining to the atmosphere, especially wind, temperatures and air density, which are used in determining correctings to basic firing data. Often shortened to "metro data."
- modal vectors. A pair of rotating arms, called the precession vector and the nutation vector, which when added together give the magnitude and orientation of the variable part of the yaw of the projectile at any instant. Adding the equilibrium yaw to the variable part gives the total yaw. The precession vector is often visualized as originating on the tangent to the trajectory, and rotating slowly. The outer end of this precession vector is taken as the origin of the nutation vector, which rotates more rapidity, and the resulting epicyclic motion of the outer end of the nutation vector represents the motion of the none of the projectile (neglecting the equilibrium yaw).
- muzzle blast. Nudden gas premure exerted at the muzzle of a weapon by the rank of hot gases and air on firing. Muzzle blast precedes the emergence of the projectile, and forms a zone of turbulent air, gas, and whoke through which the projectile must fly. The length of the projectile's path in the blast zone varies from about 20 feet to 200 feet, depending on the size of the gun and the amount of gas leakage past the projectile while in the tore.
- muzzle energy. Kinetic energy of the projectile as it emerges from the muzzle (plus a small amount of energy picked up in the muzzle blast, where for a short distance the muzzle gases outrun the projectile). This is a measure of the power of the weapon.
- musics momentum. The momentum of the projectile (i.e., product of mass and velocity) as it leaves the musule. Limited by the capacity of the recoil system built into the gun mount.

musile velocity. The projectile velocity at the

moment that the projectile ceases to be x > 2dupon by propelling forces (other than the thrust of a rocket motor). It is obtained so measuring the velocity over a distance for the gan, and correcting back to t^2a sounds for the retardation in flight.

- **NBS** (abbr). National Sureau of Standarda.
- NOL (abbr). Naval Ordinance Laboratory.
- normal force. The component of the total acrodynamic force perpendicular to the longitudinal axis of the projectile, and acting in the plane of yaw.
- NOTS (abbr). Naval Ordnance Test Station.
- autstion. The oscillation of the axis of a rotating iody such as a spinning projectile. This oscillation is superimposed on the slower motion of the projectile axis which is known as processies, which see.
- obturation. The act of, or means for, preventing the escape of gases.
- obturator. 1. A device (usually a ring or pad) incorporated in a projectile to make the tube or a weapon gas-tight. 2. A device incorporated in a rocket motor to prevent unwanted gas leakage.
- ogive. The curved or tapered front of a projectile. The fuze may or may not be included as a part of the ogive
- ogive, secant. An ogive generated by an arc not tangent to, but intersecting at a small angle, the cylindrical surface of the body. A secant ogive may have any radius of curvature greater than that of a tangent ogive for the same projectile, up to an infinite radius of curvature (i.e., a straight, conical ogive); a radius twice that of the tangent ogive is common.
- egive, tangent. An ogive generated by an arc tangent to the generator of the cylindrical surface. Called "true ogive" by the British.
- erientation of yaw. The direction of the plane of yaw (q.v.) relative to some reference direction such as a vertical plane containing the tangent to the trajectory.
- everturning moment. An aerodynamic moment tending to increase the yaw of the projectile.
- particle trajectory. The trajectory determined by gravity and zero-lift drag which would be described by a projectile which maintained zero



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angle of yaw. A meful approximation to the trajectory of an actual projectile.

- piazemetric efficiency. The ratio of the work done on the projectile by the propellant gases to the work that could have been done if the maximum chamber pressure had acted on the projectile base for the full travel in the bore; i.e., the ratio of average pressure to peak pressure.
- plane of yaw. The plane containing both the longitudinal axis of the projectile and the tangent to the trajectory.
- precession. A circular motion of the axis of rotation of a spinning body which is brought about by the application of a constant torque about an axis perpendicular to the axis of rotation. A nonconstant torque produces a noncircular precession.
- precision. The property of having small dispersion about the mean. Cf : accuracy.
- pressure front. Sec : shock front.
- pressure-travel curve. Curve showing chamber pressure plotted against the travel of the projectile within the bore of the weapon.
- probable error. In general, a value that any given error will as likely fall under as exceed. In gunnery, a measure of the dispersion pattern around the center of impact; half of the observed impacts will he within a band two probable errors wide and centered on the center of impact.
- quadrant elevation. Vertical angle between a horizontal plane and axis of bore of gun, just prior to firing.
- radius of gyration. The distance from the axis of rotation at which the total mass of a body might be concentrated without changing its moment of inertia about that axis. In this handbook radii of gyration are usually expressed in calibers.
- range correction. Changes of firing data necessary to allow for deviations in range due to weather, material, or ammunition.
- range deviation. Distance by which a projectile strikes beyond, or short of, the target measured along a line parallel to the gun-target line.
- range error. Difference between the range to the point of impact of a particular projectile and the range to the senter of impact of the group of shots fired with the same data.

- range probable error. 1. Error in range that a gun or other weapon may be expected to exceed as often as not. Range probable error given in the firing tables for a gun may be taken as an index of the accuracy of the piece. 2. In describing the dispersion pattern of a group of shots, the probable error in the range direction.
- range wind. Horizontal component of true wind in the direction of the line of fire.
- reference rounds. Ammunition rounds of known performance which are fired during ballistic tests of ammunition for comparative purposes. Also called "control rounds."
- relative velocity. The velocity of relative motion, especially in respect to a projectile and the airstream.
- relative wind. The velocity of the air with reference to a body in it. Usually determined from measurements made at such a distance from the body that the disturbing effect of the body upon the air is negligible. Equal and opposite to the relative velocity of a projectile.
- restoring moment. A static moment (q.v.) which is negative when the angle of attack is positive, and vice versa.
- reversed flow. Flow of the airstream from the base toward the nose of the projectile, such as exists in the muscle blast where the blast gases are moving faster than the projectile.
- Reynolds number. (Named after Ouborne Reynolds, 1842-1912, a British physicist and engineer.) An index of similarity used in the analysis of the fluid flow about scale models in wind tunnel tests to determine the results to be expected of the flow about full-scale models. The Reynolds number is expressed in a fraction, the numerator consisting of the density of the fluid multiplied by its velocity and by a linear dimension of the body (as for example its diameter), the denominator consisting of the fluid $(RE = \rho V l/\mu)$.

RMS error. Sec: standard error.

rechet motor. A nonairbreathing reaction propulsion device that consists ementially of a fuel chamber(a) and exhaust nessle(a), and that carrice its own solid exidiner-feel combination from which hot games are generated by combination and

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GLOSSARY (cont'd)

- expanded through a nozzle(s). (If the fuel is liquid the device is called a "rocket engine.") rell. An angular displacement about the longitudinal axis of a projectile.
- rell rate. The time rate of projectile rotation about its longitudinal axis.
- rell rate, nondimensional. The product of roll rate and a reference length, us for example a diameter, divided by the airspeed (r = pd/V). Usually called "spin."
- rolling moment. An aerodynamic moment about the longitudinal axis of a projectile, tending to change the roll rate.

relling velocity. Angular velocity; roll rate.

- root mean square. The square root of the arithmetical mean of the squares of a set of numerical values.
- retating band. Soft metal band around a projectile near its base. The rotating band centers the projectile and makes it fit tightly in the bore, thus preventing the escape of gas, and by engaging the rifling gives the projectile its spin.
- round (of ammunition). 1. Short for complete round, which see. 2. A shot fired from a weapon. scale effect. An effect in fluid flow that results
- from changing the scale but not the shape of a body around which the flow parses. Reynolds number is useful in the assessment of scale effect. schlieren, 1. Gradients or variations in mas density.
- from the German word. 2. Au optical system which either cuts off or pames a large change in light intensity, owing to the slight refraction of the light passing through the gas. This phenomenon is often used to make turbulence and shock waves visible by photographic means: hence, "schlieren photographs."
- sectional density. The ratio of the weight of a projectile to the square of its diameter. A measure of the mass per unit of frontal area, and therefore of the deceleration due to drag.
- sensitivity factor. The percent change in range (or deflection) produced by a one percent change in a parameter affecting range (or deflection), such as mumber velocity or initial yawing velocity. Also called "differential coefficient." Sec: difformatial effects.

- separation. '. The phenomenon in which the boundary layer of the flow over a body placed in a moving stream of fluid (or moving through the fluid) separates from the surface of the body. 2. The point on the body at which the separation begins. Also called "separation point."
- setback acceleration. The peak acceleration experienced by the projectile during launching. I'sually expressed in terms of the acceleration due to gravity, e.g., "the setback acceleration was 40000 g's" or about 1,286,4CD ft/sec².
- shock front. The outer side of a shock wave, at which the pressure rises from zero up to its peak value. Also called a "pressure front."
- shock wave. 1. A boundary surface or line across which a flow of air or other fluid, relative to a body or projectile passing through the air or fluid, changes discontinuously in pressure, velocity, density, temperature and entropy within an infinitesimal period of time. 2. Such a boundary surface or line that comes into being when an object moves at transonie or supersonic speeds. 3. Such a surface or line produced by the expansion of gases away from an explosion (or through a nozzle).
- shroud. A tubular section encircling the tips of the fins, and usually integral with the fins. The shroud often forms a rear riding surface for the projectile in the bore of the gun.
- slug. The engineering unit of mass, chosen such that a force of one pound acting on a unit mass will produce an acceleration of one foot per second per second. Since the weight of a body is equal to the product of its mass and the acceleration of gravity, the weight of a body having a mass of one alug is 32.17 lbs (at sea level at 45° latitude).
- span. The maximum dimension of an airfoil (e.g., a coplanar pair of fins) from tip to tip.
- spark range. A firing range in which projectiles in free flight can be photographed by the light from an electric spark which is triggered by passage of the projectile. See: ballistic range.
- specific impulse. The total impulse produced by burning a pound of rocket fuel. At constant thrust and mass burning rate, the thrust pro-

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duced per unit of mass burning rate, i.e., pounds per lb/sec.

specific weight. Weight per unit volume.

spike. A subcaliber cylinder, often slightly tapered, which replaces the ogive of a projectile. increasing the drag but moving the center of pressure of the lift force nearer the base of the projectile.

spin. Nee: roll rate, sondimensional.

spin rate. Sec: roll rate.

- spin stabilization. Method of stabilizing a projectile during flight by causing it to rotate about its own longitudinal axis.
- spotting charge. A small charge such as black powder, in a projectile under test, to show the location of its point of functioning (usually its point of impact).
- square base. Descriptive of a projectile with a cylindrical base section, as opposed to a beattail, which see. Also called "flat base."
- stability. A characteristic of a projectile that causes it, if disturbed from its condition of equilibrium or stead; flight, to return to that condition.
- stability factor, dynamic. A number related to the yaw damping characteristics of a projectile.
- stability factor, gyroscopic. A number relating the angular momentum of a projectile to the alope of its accolynamic overturning moment. Long unrel as a nole criterion of projectile stability and called simply the "stability factor," s. A necessary, but not sufficient, condition for stability is that this factor be greater than unity, or negative.
- stability, static. Stability in the absence of spin. In general, a mochanism is statically stable if any displacement from a rest position creates a force or moment opposing the displacement.
- Standard Atmosphere. The standard atmosphere for the United States Armed Services in the U.S. Standard Atmosphere which is that of the International Civil Aviation Organisation (ICAO). This standard atmosphere assumes a ground pressure of 760 mm of mercury (14.60 pai) and a ground temperature of 15°C (50°F). The temperature throughout the troposphere ex-

tending up to 11 kilometers (approx. 36,000 ft) is given by:

 $T(^{\bullet}F) = 59 - 0.263256 \text{ k}$

where h is the height above san level measured in feet. In the stratony, here, extending from 11 kilometers to 25 kilometers (approx. 82,000 ft) the temperature is assumed to be a constant 216.66 K (-69.7°F). Above the stratosphere other laws are assumed. Temperature is significant locause the acoustic velocity in feet per second is given by

$V_{a} = 49.1 \sqrt{460 + T}$ T in *P

standard deviation. In the field of testing, a measure of the deviation of the individual values of a series from their mean value. The standard deviation of a sample is expressed algebraically by the formula.

$$x = \sqrt{\frac{\sum(x_i - \overline{x})^2}{N}}$$
 where Σ means

the sum of N individual squared differences, the x_i are the individual values, \bar{x} is the mean $(\bar{x} = \sum x_i/N)$, and N is the number of individuals in the sample. The best estimate of σ , the standard deviation of the lot from which the sample was drawn, is obtained by multiplying the sample value, x, by $\sqrt{N/(N-1)}$.

- standard error. The square root of the average of the squares of all the errors. When error is identified as the difference between an observed point and the means of the observations, standard error becomes identical with the sample standard deviation. It might also be called the "EMS error."
- standard muzzle velocity. Velocity at which a given projectile is supposed to leave the muzzle of a gun: The velocity is calculated on the basis of the particular gun, the propelling charge used, and the type of projectile. Firing tables are based on standard muzzle velocity.
- standard projectile. That projectile which a given gun was primarily designed to fire.
- static moment. An aerodynamic moment related only to angle of yaw.

static pressure. The pressure which is exerted by

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GLOSSARY (cont'd)

3.

a fluid at rest, or which would be indicated by a gage placed in the stream and moving with the same velocity as the stream. It is the pressure arising from the random motions of the mole cutes of the fluid, rather than their organized motion in the direction of the flow.

- steady state. The condition of a system which is essentially constant after damping out initial transients or fluctuations.
- sting. A rod or type of mounting attached to, and extending backward from, a model, for convenience of mounting when testing in a wind tunuel.
- subsonic. Pertaining to relative motion between a body and a surrounding fluid at a speed less than the speed of sound in the same fluid.
- summit of trajectory. If ights point that a proiectile reaches in its flight.
- swerving motion. In flight, the motion of the center of gravity of a projectile perpendicular to its particle, or zero-lift, trajectory.
- *;stem reliability. The probability that a system will perform its specified task under stated tacical and environmental conditions. This will include accuracy.
- T (Subscript). In aerodynamic data, relating to tail alone configuration.
- terminal velocity. 1. The constant velocity of a falling body attained when the resistance of air or other ambient fluid has become equal to the force of gravity acting on the body. Sometimes ealled "limiting velocity." 2. Velocity at end of trajectory, i.e., impact velocity.
- time of flight. Elapsed time in seconds from the instant a projectile leaves the gun until the instant it strikes or bursts.
- telerance. The permissible difference between the two extremes in dimension, weight, strength or other quality which will not cause rejection of an item.
- trajectory. The curve in space traced by the center of gravity of the projectile.
- transition flow. A flow of fluid, about a body, that is changing from laminar flow to turbusent flow.
- transscic range. The range of speeds between the speed at which one point on a body reaches supersonic speed (relative to the airflow in the

vicinity of that point) and the speed at which the shock wave system is fully developed.

- transenic speed. A speed within the transonic range.
- transverse axis. In a projectile, any axis normal to the longitudinal axis and passing through the center of gravity.
- trim. The equilibrium attitude of the longitudinal axis of the projectile relative to the tangent to the trajectory; equilibrium yaw.
- turbulent flow. An unsteady flow characterized by the super-position of repidly varying velocities on the main velocity of flow, in contrast to the smooth, steady laminar flow in which velocity varies with distance but only slowly with time.
- twist (of rifling). Inclination of the spiral grooves of the rifling to the axis of the bore of the weapon. It is expressed as the number of calibers of length in which the rifling (ard therefore the projectile) makes one complete turn. A right hand twist is such as to impart a right hand (clockwise) rotation to the projectile when viewed from the rear. Most U.S. guns have right hand twist.
- utility. A numerical scale for comparing preferences between alternatives. Usually defined on the interval 0, 1 because of its relation to probability.
- vacuum trajectory. The path of a projectile subject only to gravity. A first approximation to the trajectory of an actual projectile.
- vector. 1. An entity which has both magnitude and direction, such as a force or velocity. 2. In connection with the yawing oscillations of projectiles, the rotating arms which can be used to represent the components of the yaw are ter.aed modal vectors, which see.
- velocity. Speed, or rate of motion, in a given direction and in a given frame of reference. In many contexts no distinction in meaning is made between speed and velocity, the symbol V often being used in equations in which the magnitude of the velocity, i.e., the speed, is the only attribute of velocity which is being considered.

velocity head. See: dynamic pressure.

viscosity, coefficient of. The ratio of the absaring stress to the velocity gradient in a boundary



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layer. Dependent on the fluid and on its temperature.

 $\mu_{\rm out}$ at 59° F = 3.72 \times 10⁻¹ lb-sec/ft²

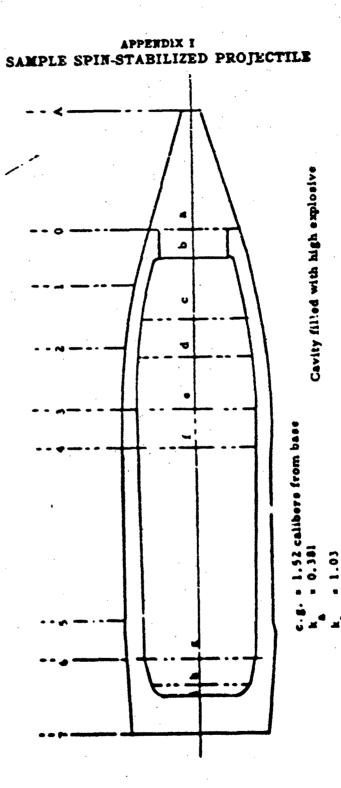
- wake. The zone of turbulent flow behind the bear of a projectile.
- wash. The surge of disturbed air or other fluid resulting from the passage of something through the fluid. Includes the waks and bow and side waves.
- wave, expansive. An oblique wave or zone set up. in supersonic flow when the change in direction of the airflow is such that the air tends to leave the new surface, such as flow around the juncture of a cylinder and a cone (e.g., at the forward end of a boattail). This condition is called "flow around a corner." The air after passing through an expansive wave or some has a lower density, static presure, and freestream temperature and has higher velocity and Mach number. Visible as a darkened zone in schlieren photographs, these waves are often called "expansion fame." wave length. 1. The distance traveled in one period or cycle by a periodic disturbance. 2. Of yaw of a projectile, the distance traveled by the projectile during one cycle of yaw.
- yaw. 1. The angle between the direction of motion of a projectile and the direction of the longitudinal axis of the projectile. 2. The oscillation of the direction of the longitudinal axis (as in "wavelength of yaw"). 3. To acquire an angle of yaw; to oscillate in yaw.
- yaw of repose. That part of the equilibrium yaw which is due to gravity.

yaw drag. Drag due to yaw.

- yawing moment due to yawing. Term sometimes used for the damping moment.
- yawing velocity. Time rate of change of yaw; the change may be a change in magnitude or direction, or both.
- zone charge. The number of increments of propellant in a propellant charge of semifixed rounds, corresponding to the intended sone of fire.
- zone of fire. The range interval which can be covered by a round containing a given number of increment: of propellant, i.e., the coverage obtainable by changing quadrant elevation at a constant muzzle velocity.
- zoned ammunition. Semifixed or separate loading ammunition in which provision is male for adding or removing propellant increments.

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APPENDIX II CALCULATION OF C. G. AND RADIUS OF GYRATION

Approximate formulas for high explosive projectiles are presented by Hitchcock in BRL Report 620 (Ref. 81). Method" (see Appendix VII) are:

$$\begin{aligned} X_{c+} &= 0.375 \frac{l}{d} \\ k^2_{o} &= 0.140 \\ k^2_{o} &= 0.070 + 0.0594 \end{aligned}$$

where X_{CL} , in the distance from the base of the projectile to its center of gravity, in solihors, and l/d in the figurum ratio of the projectile.

 $\left(\frac{i}{a}\right)^{1}$

a. Allernate Method:

For the sample projectile in Appendix I, the parameters calculated by use of the "Alternate $X_{c.c} = 1.5$ $k^2_{.c} = 0.145$ $k^2_{.i} = 1.07$

b. Hilchcock Method:

By Hitcheark's formulas, we would get

Xen .: 0.375 × 4.18 = 1.64

k*. == 0.140

 $k_{f}^{2} = 0.070 \pm 0.0694 \ (4.37)^{2} = 1.31$



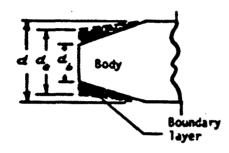
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APPENDIX III GYROSCOPIC STABILITY ESTIMATES

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A. SPIN-STABILIZED PROJECTILE WITE BOATTAIL

The following is a sample calculation for a spin-stabilised projectile with boattail, using the methods of Wood (Ref. 21) and Simmuns (Ref. 20) to estimate the normal force and static moment coefficients. The geometric and mass characteristics of the projectile are given in Appendix I.



Effective Base Diameter:

$$d_{*} = \sqrt{\frac{d^{*} + d_{1}^{*}}{2}}$$

where d = Rear body diam. = 4.98" (0.415 ft) d₀ = Base diam. = 4.22"

$$4_{*} = \sqrt{21.7314} = 4.66''$$

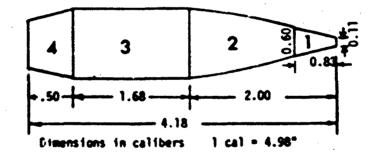
Effective Base Area: $S'_{4} = .7854 d_{4}^{2}$ $= .7854 (4.66)^{4} = 17.0654 in^{2}$

= .7854 (4.98)" = 19.4782 im²

 $\frac{\text{Base Ares Ratio:}}{\frac{S_{0}^{*}}{S} = \frac{17.0554}{19.4782} = 0.8756}$

Volume of Projectile (including boattail boundary layer):

V. - 203.5412 in* (see calculation below)



| Section | Calculations | Volume, ind |
|---------|---|-------------|
| 1 | $(3.60)^{2} + (3.00)^{2} + (3.00) (.55) + (.56)^{2}$ | 11.8276 |
| 3 | From Harvard Tables Caloulations ⁶ | 83.8740 |
| 3 | 7864 (8.382) (4.38) ⁸ == | 163.2060 |
| 4 | .2618 (2.50) {(4.98) ² + (4.96) (4.66) + (4.66) ²] | 45.6236 |
| | | |

Vo an Total Brendery Layer Volume an 208.5412

* Reference Appendia VII.

14

AMCP 705-362

APPENDIX III (cest'd)

Mean Finenez: Ratio: V_a 383,5412 3.1292 Nd (19.47)(2) (4.98)

Determination of f₁ and f₂: (See graph Appendix IV) At supersonic speed:

$$N = \sqrt{\frac{M^2 - 1}{V_0 \sqrt{Sd}}} = 0.45 \text{ for } M = 1.72$$

$$\frac{f_1 - 1}{V_0 \sqrt{Sd}} = 0.142 \text{ and}$$

$$\sqrt{M^2 - 1}$$

 $\frac{f_1 - 1}{\sqrt{M^2 - 1}} = 0.145$
 $\sqrt{M^2 - 1}$

$$C_{H_{0}} = \left(2\frac{S_{1}'}{S} + S\right)f_{1}$$

= $\left[2(.5756) + S\right](1.1987)$
= 2.70 mil⁻¹
Moment ('cofficient (about base):

$$\frac{C_{H_{a}}}{C_{H_{a}}} = \left(2\frac{V_{1}}{\mathcal{E}d}\right)f_{1} = \left[2(3.1202)\right](1.2300)$$
$$= 7.70 \text{ ms}^{-1}$$

Conter of Gravity (from Appendix 1): C. G. = 1.52 calibres from how C. P. = C. G. = 2.85 = 1.52 = 1.53 calibres

Static Moment Coefficient:

$$C_{H_{e}} = C_{H_{e}} (C. P. - C. G.)$$

= (2.70) (1.33) = 1.59

Gyroscópic Stability Factor, s.: Velocity: Val = 1925 (ps Twist: s = 28 calibers per turn Spin rate: p = 165 rps = 1040 rad per res Max body diam: d = 0.415 ft Air density: p = 0.002378 abg/ft²

$$I_{*}^{*}/I_{*} \approx 0.0010 \text{ dug-ft}^{*}$$

$$\mu = \tau_{\mu}\mu^{\mu} V^{\mu} C_{H_{\mu}}$$

$$\overline{S}$$

$$a_{\mu} = \frac{I_{*}^{2} y^{\mu}}{6 J_{\mu} a}$$

 $\frac{.6040 (1.0316 \times 10^{7})}{6 \left(\frac{\pi}{6}\right) (.0022057) (.6716) (1.706636 \times 10^{7}) (3.50)} = 1.40$

.



AME 17 706-542

APPENDIX III (cent'd) GYROSCOPIC STABILITY ESTIMATES

Downloaded from http://www.everyspec.com

B. SPIN-STABILIZED PROJECTILE WITHOUT BOATTAIL (FLAT BASE)

Assume only change from previous example is in volume and C. G. location. New volume : V = 306.5412 in.*

Mean Finences Ratio:

 $\frac{\overline{V_{\bullet}}}{\overline{Nd}} = \frac{306.5412}{(19.4782)(4.98)} = 3.160s$

Determination of f_1 and f_2 : (New graph Appendix IV)

$$N = \frac{\sqrt{M^2 - 1}}{V/Nd} = 0.44 \text{ for } M = 1.72$$

$$\frac{f_1 - 1}{\sqrt{M^2 - 1}} = 0.136 \text{ and } \frac{f_2 - 1}{\sqrt{M^2 - 1}} = 0.148$$

$$\therefore f_1 = 1.900 \text{ and } f_2 = 1.2237$$

Normal Force Coefficient:

$$C_{N_{\sigma}} = \left(2 \frac{S_{i}}{S} + .5\right) f$$
, where $S_{i} = 8$
 $= [2 (1.0) + .5] (1.500)$
 $= 3.00 \text{ rad}^{-1}$

Moment Coe . (about base):

$$C_{H_{0}} = \left(2\frac{V}{Sd}\right)f_{0} = 6.3216 (1.2337)$$

= 7.80 rad⁻¹

Center of Pressure: $C. P. = \frac{C_{W_{o}}}{C_{W_{o}}} = 2.60 \text{ calibers from base}$

Center of Gravity: C. G. is now located 1.50 caubers from base C. P. - C. G. = 2.60 - 1.50 = 1.10 calibers

Static Moment Coefficient:

 $C_{H_{\bullet}} = C_{H_{\bullet}} (C, P, -C, G)$ = (3.00) (1.10) = 3.20

Gyroscopic Stability Pactor, a,

Since the parameters—Vol. p. n. d. s. I_{i}^{2}/I_{y} —are the same as the example in part A:

$$r_{p} = 1.49 \left(\frac{C_{H_{p}} \text{ with boattail}}{C_{H_{p}} \text{ without boattail}} \right)$$
$$= 1.49 \left(\frac{3.59}{3.30} \right) = 1.62$$

Conclusion: Eliminating the boattail has incre the gyroscopic stability factor (but also inset the zero-yaw drag ecolicient).

AMAT 746-342

APPENDIX IV COMPARISON OF ESTIMATES OF BALLISTIC PARAMETERS BY VARIOUS METHODS

For comparison with the other estimates, ealculations by Hitchcock's method, BRL Report 630 (Ref. 21), for the same bostiniled projectile, Appendix I, are presented below:

| a (boattail angie) | = 7.5 degrees |
|--|-----------------|
| b (boattail length) | = 0.5 calibara |
| e (cylindrical body longth) | = 1.68 calibera |
| d (ogival head length) | = 2.00 calibera |
| (radius of agival are) | = 5.12 calibers |
| · · | 1.A/e = .1953 |

Normal Forve (arfficient: (using a, b, c, d, and *

- K. = .553 + .0223e .61396 .6023e + .2575d + .6678 (1.0/e)
- $K_{*} = .8^{5/3} + .1673 .0070 .0039 + .3270 + .1265$

.

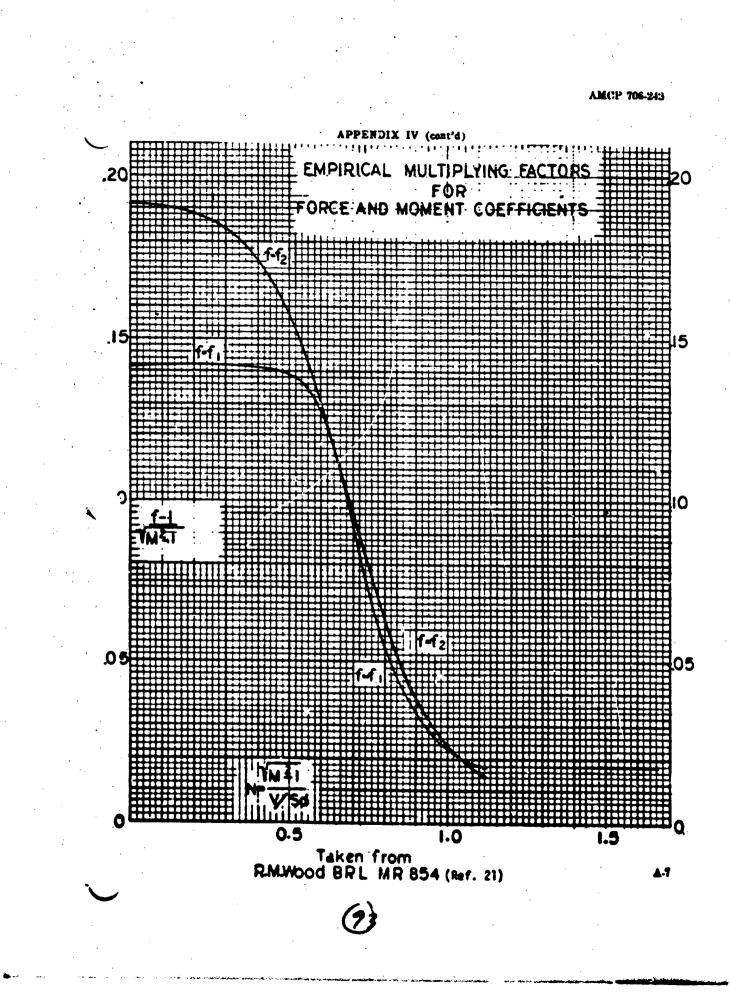
K. = 1.1629

$$(x_n = \frac{\pi}{2}, K_n = 2.96 \ (vo 2.70 \ by Wood's method)$$

('enter of Pressure:

- k = .0747 + .0443s + 1.0196 + .9032s + .2459d + .9082 (1.0/s)
- k = .0747 + .3323 + .5095 + 1.3494 + .4918 + .1579
- k == 2.51 calibers from the base (vs 2.85 by Word's method)

This agreement is considered to be better then average. While Hitchesch's actimates are very good for projectiles which lie within the range of his experimental data, the Wood-Simmons estimates will in general be more reliable.



AMCP 706-242

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APPENDIX V DYNAMIC STABILITY ESTIMATE

Problem: To determine s_{t_0} . The projectile will be stable if:

 $\frac{1}{s_0} < s_{0} (20 - s_{0}) \quad (\text{Ref. par. } 5 - 2 + 2.1)$

Permula:
$$k_{e} = \frac{k(C_{L} + k_{a}^{2}C_{M_{pe}})}{C_{L_{p}} - C_{p} + k_{i}^{2}(C_{M_{p}} + C_{M_{p}})}$$

 $\begin{array}{l} \hline \text{Data: For prototype projectile (Appendix I).} \\ \hline C_{L_{0}} = 2.70 \text{ rad}^{-1} \\ \hline \text{Mach} = 1.72 \\ \hline w = 46.08/32.2 \text{ shap} \\ d = 0.415 \text{ ft} \\ \hline I_{0} = 0.0359 \text{ shap} ft^{0} \\ \hline J_{1} = 0.0359 \text{ shap} ft^{0} \\ \hline J_{2} = 0.3640 \text{ shap} ft^{0} \\ \hline J_{1} = \frac{1}{L_{0}^{2}} = \frac{\text{mol}^{2}}{T_{0}} \\ = \left(\frac{46.08}{32.2}\right) \frac{(.415^{\circ})}{(.3540)} = 0.333 \end{array}$

Since our projectile has the same ballistic shape as projectile, 90-mm, HE, M71, the ballistic coefficients for the 90-mm projectile at Mach = 1.72 (ref. Appendix VIII-E) may be used, namely:

$$C_{H_{ph}} = 0.20$$

 $C_{H_{q}} + C_{H_{p}} = -9.0$
 $C_{p} = 0.32$

Nolution:

From Appendix III-A: $z_p = 1.40$ $\therefore \frac{1}{z_p} = \frac{1}{1.40} = 0.671$ $z_{i_p} = (2.0 - z_q) = 0.756 (2.0 - 0.756) = 0.96$

Conclusion : Projectile is stable since :

 $\frac{1}{4} < 4 u_0 (20 + 4 u_0)$, i.e.: 0.671 < 0.94

AMCP 706-342

APPENDIX VI STATIC STABILITY ESTIMATE OF A 5-INCH FIN-STABILIZED PROJECTILE

Problem: Determine normal force and center of pressure of the body alone, and normal force and center of pressure of the tail alone in order to solve for static stability:

 $C, P, -C, G_{1} > 0.5$ caliber

Solution:

1

(1) Body alone coefficients at subsonic muzzle velocities

Data: The effective base are:, S'_{i} , and total boundary layer volume are determined in a manner similar to that shown in Appendix III-A.

2.672" and a = 5" 4 Si $\frac{7854}{.7854} \frac{d_{\pi}^2}{(2.672)^2} = 5.6074 \text{ in}^2$ S .7854 # -.7854 (5)* = 19.635 19.635 d = 19.635 (5)Sil -96.175 Ľ. = 487.0151 im³ V. M 187.0151 · = 4,9000 98.175

Solving by Simmons' Equations Ref. 20:

$$\overline{C_{H_{B}}} = 2\left(\frac{S_{i}}{S}\right) + 0.5$$

$$= 2\left(\frac{5.6074}{19.635}\right) + 0.5 = 1.071$$

$$C_{H_{B}} = 2\left(\frac{V_{s}}{Sd}\right) = 2\left(\frac{478.0151}{98.175}\right)$$

$$= 9.9212$$

$$C. P. _{max} = \frac{C_{H_{B}}}{C_{H_{B}}} = \frac{9.9212}{1.071}$$

= 9.26 calibers from base of fins

(2) Tail alone coefficients at subsonic velocities: Data: effective tail length: $l = 3.0^{\circ}$ fa span: $S = 5.0^{\circ}$ effective base diameter: $d_s = 2.67^{\circ}$ $\frac{l}{S} = 0.6$ and $\frac{d_s}{S} = 0.53$ Solving by Simmons' Tables:

 $C_{L_T} = 2.20$ (for 6 rectaugular fins)

$$C_L = C_{L_T} (0.74) = 1.628$$
 (body interference
factor = 0.74)

 $C_{X_T} = C_L (1.80) = 2.9304$ (allowance for end plates and shroud = 1.80)

C. P. $_{inil} = 0.60$ caliber from base of fine

(3) Static Stability | C. P. - C. G. | > 0.5 caliber (Ref. par. 5-3.2):

Data: From parts (1) & (2):

$$C_{N_B} = 1.0710$$
 at s C. P. located 9.26 calibers
from base of fins

Cvp = 2.9304 at a C. P. located 0.60 caliber from base of fins

 $C_{N_{\mu}} = C_{H_{H}} + C_{H_{T}} = 4.0014 \text{ rad}^{-1}$

 $C_{\rm e}G_{\rm e}=3.68$ calibers from base of fins

 $(C, P_{r_B} - C, G_i) = 9.26 - 3.68 = 5.58$ cali zero $(C, P_{r_T} - C, G_i) = 0.60 - 3.68 = -3.08$ calibers

Solving (ref. psr. 5-3.1):

$$C_{M_{\pi}} = C_{M_{\pi}} (C. P_{.\pi} - C. G.) + C_{M_{\pi}} (C. P_{.\pi} - C. G.) + C_{M_{\pi}} (C. P_{.\pi} - C. G.)$$

 $C. P. - C. G. = \frac{C_{M_{\pi}}}{C_{M_{\pi}}} = \frac{(1.071) (5.58) + (2.9304) (-3.08)}{4.0014} = -\frac{3.0494}{4.0014} = -0.76$
 $1 C. P. - C. G. i = 0.76$ caliber

<u>Conclusion</u>: Static stability scenes adequate since | C. P. - C. G. | > 0.5, i.e.,0.76 > 0.5

A.

(95)

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AMCP 795-342

APPENDIX VII PROJECTILE GEOMETRY

The dasign parameters related only to the materials and geometry of the projectile are:

Weight

A.M

Center of gravity location

Axial and transverse moments of .nertia

Methods of Computation:

- 1. Mochanical Integrator (Ref. 95):
 - a. A scale drawing is made of the part or assembly.
 - (1) Dimensions in the *z* direction are not altered
 - (2) Dimensions in the y direction are altered by letting $y_1 = y^2/2$
 - b. The drawing is traversed by the mochanical integrator (a form of planimeter).
 - e. Dial indicators provide numbers, relative to the transformed plane areas.

- d. Equations convert dial readings to weight, conter of gravity, and moments of izertia of solids of rev. Aution.
- 2. Harvard Tables-Standard Method (Bel. 94):

a. Analyst works from dimensioned akstehes, or drawings, to evaluate weight, e.g., and mements of inwrita.

- b. Tables provide expedient method to supplement standard equations for solids of revolution.
- 8. Alternate Method: Analyst uses variations of formules for limited sumber of solid shapes, and simplifies summary of parts and assembly.
- 4. Computer (Ref. 98): The weight, location of center of gravity, volume, polar moment of inertia, transverse moment of inertia and total moment of inertia can be obtained through use of a digital electronic computer.

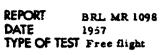
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9L

APPENDIX VIIL--A 30-MM HEI PROJECTILE, T306E10

Muzzle

AUTHOR(S) E. T. Roecker and E. D. Boyer REPORT



0.56

Variable

Variable 0.098 0.38

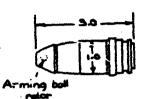
Weight, Ib

(Velocity, for

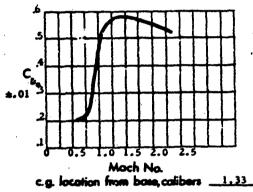
y, radical

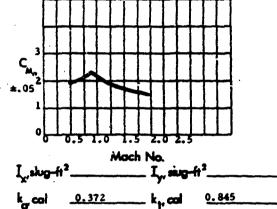
Spin rate, rps d, ft t











Subsonic Peak , 0.6 0.9

2.1+0.2

2.34.05

Supersonic 2.0

2.440.2

1.5±.05

-3.541.0

-0.13±C.10

<u>Comments</u>

M <u>,0.6</u> C_{by}: C_{La} <u>2.7</u>

С_{Ма} 1.9 С_{Ма}+С_{Ма}

C₁₀ = 0

C.P.

. . .

ation

2.3

2.35a.05 1.85a.05 5.6a0.1

. . 6

0.540...

Without arming ball rotor

{C_{Mpu}=C_{Mpu}|_{m=0} + b δ_a[±] M = 2.0 b = 90

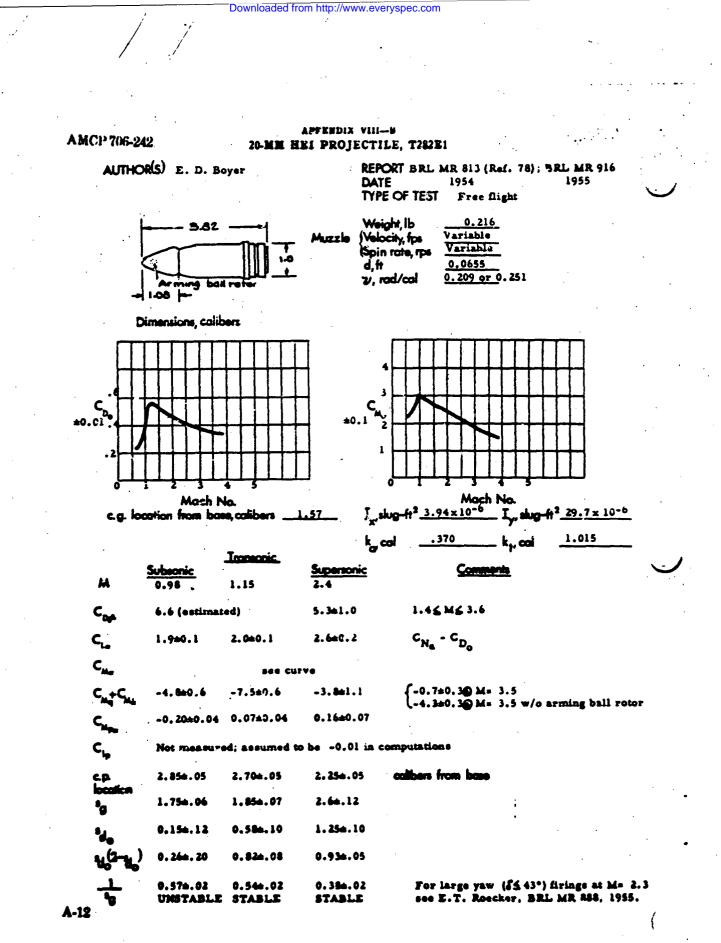
calibers from bass

Computed for standard 1:25 twiet (= 0.25)

Without arming ball rotor and at small yaw $(S_g < 2^{\circ})$

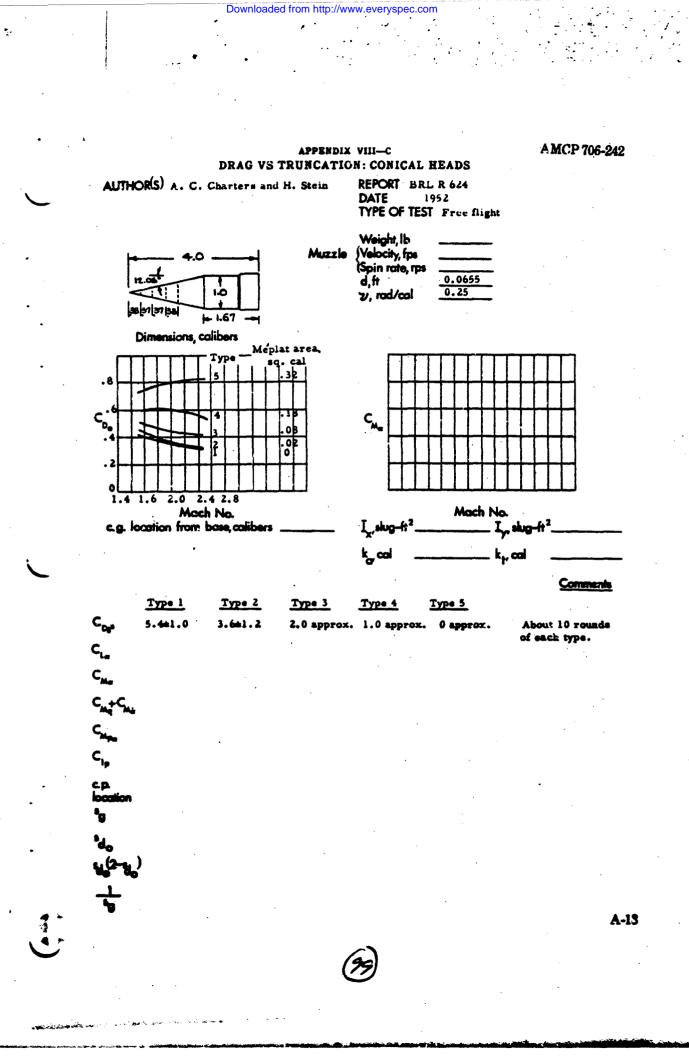
STABLE at small yaws w/e arming ball rotor. Usually UNSTABLE with arming ball rotor A-11

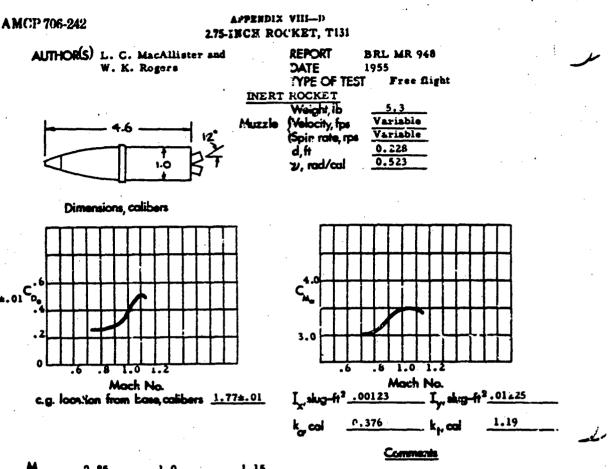
(9)



G

17





| - | V. 87 | 1.4 | 1.13 | | |
|---------------------|-------------|-------------|------------|--|--|
| Cor | 5.8 approx. | | | | |
| C _{Le} | 1.954.05 | 2.04.05 · · | 2.Q4.08 | | |
| CMa | 3.15*.05 | 3.45±.08 | 3.45±0.1 | | |
| $C_{M_q} + C_{M_k}$ | -4.5±0.5 | -7.5±1.0 | -1082 | | |
| ς. | -0.23±0.1 | -0.23±0.1 | -0.07±0.07 | | |

collibers from base

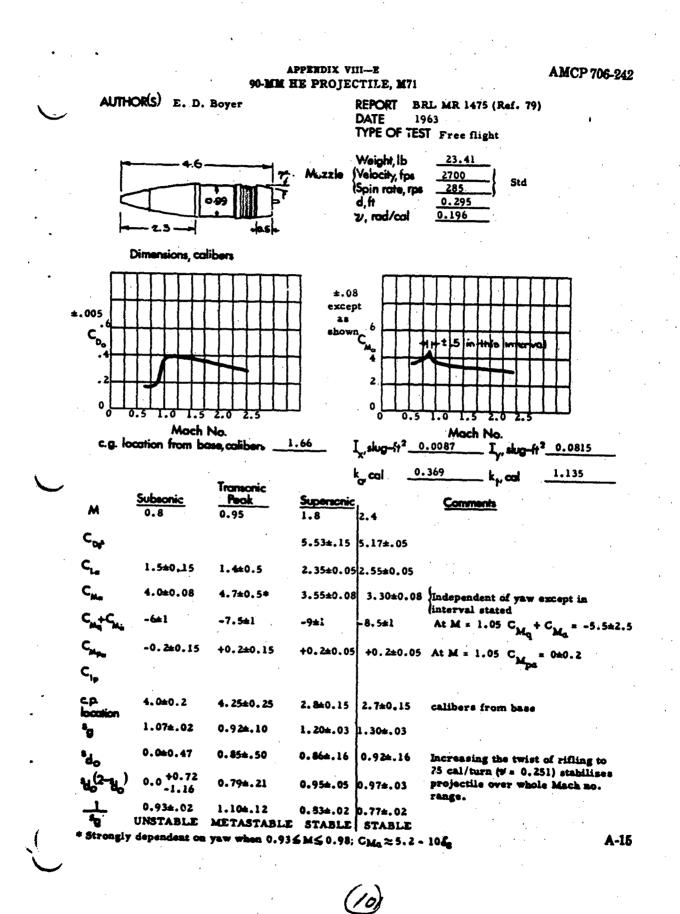
At all 3 Mach nos.

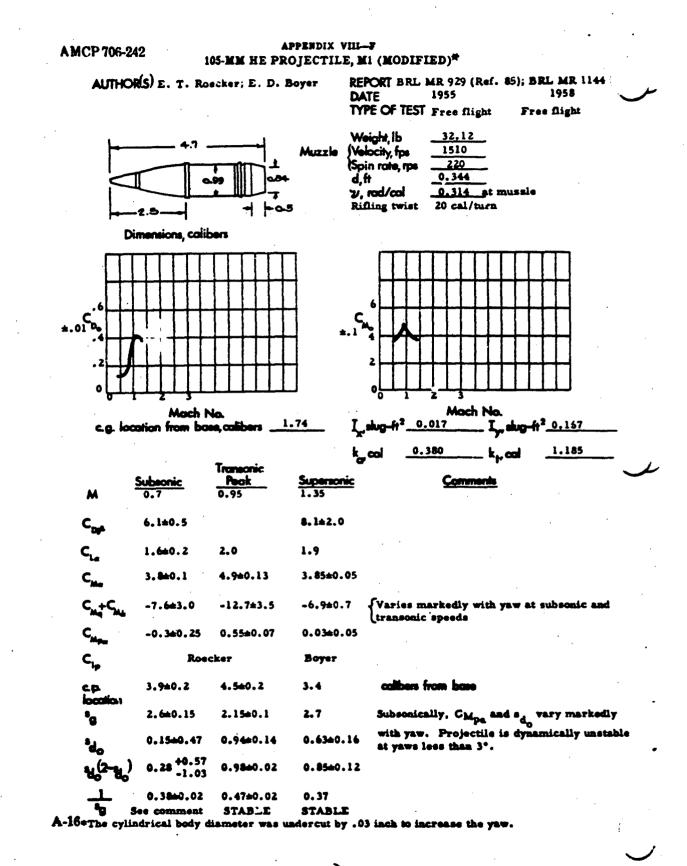


C_{Ip}

c.p. Location

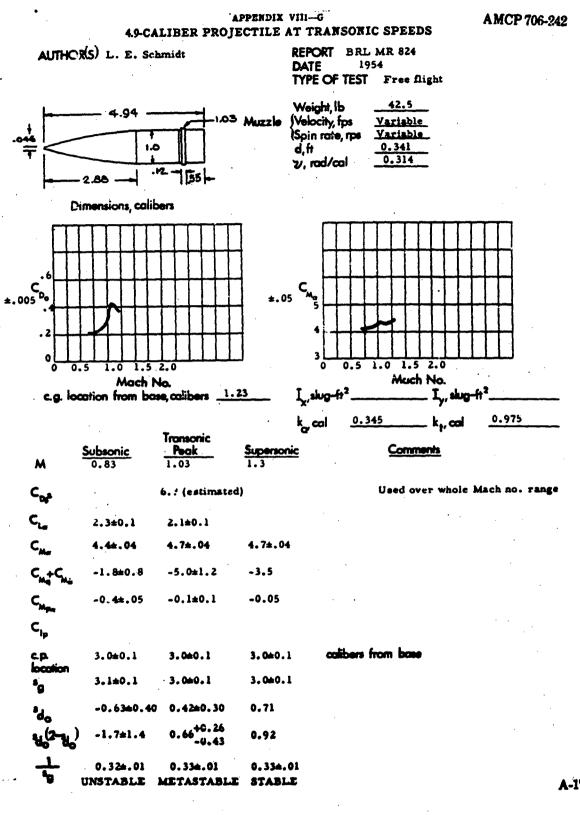
A-14



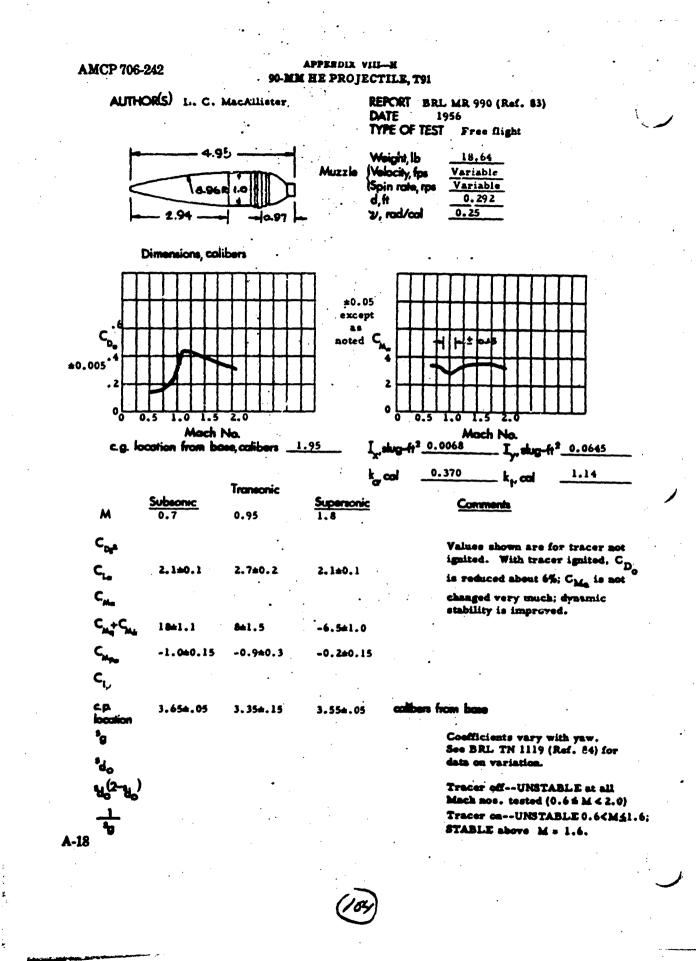


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A-17

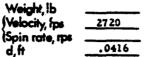


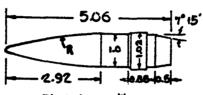
APPENDIX VIII-I EFFECTS OF HEAD SHAPE VARIATION

AMCP 706-242

AUTHOR(S) E. R. Dickinson

REPORT BRL MR 838 (Ref. 24) DATE 1954 TYPE OF TEST Free flight





Dimensions, colibers

c.g. location from base, colibers various

M = 2.44

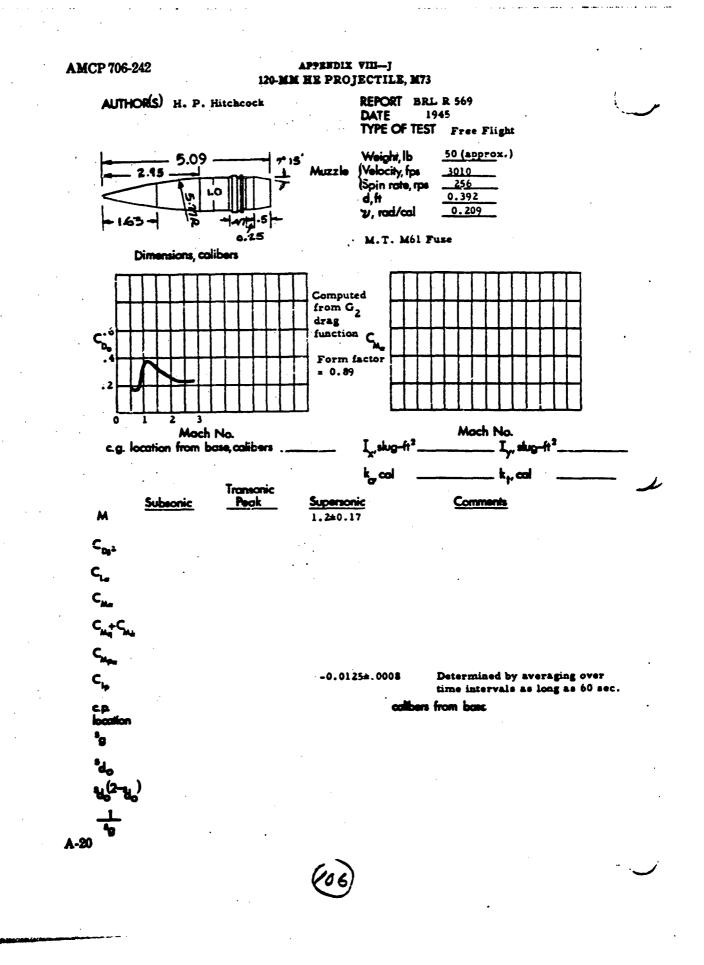
9.47 14.20 18.94 37.88 colibers R/R 1.0 1.5 z.0 4.0 cone) .235±.007 .210±.006 .210±.005 .217±.005 .205±.005 $C_{D_k^k} = 10.0$ for all types C_L 2.8±0.1 2.7±0.1 2.65±0.1 2.55±0.1 2.5±0.1 All values are at M = 2.44 c.p. location colibers from base 3.05±.05 2.93±.05 2.82±.03 2.71±.03 2.57±.05

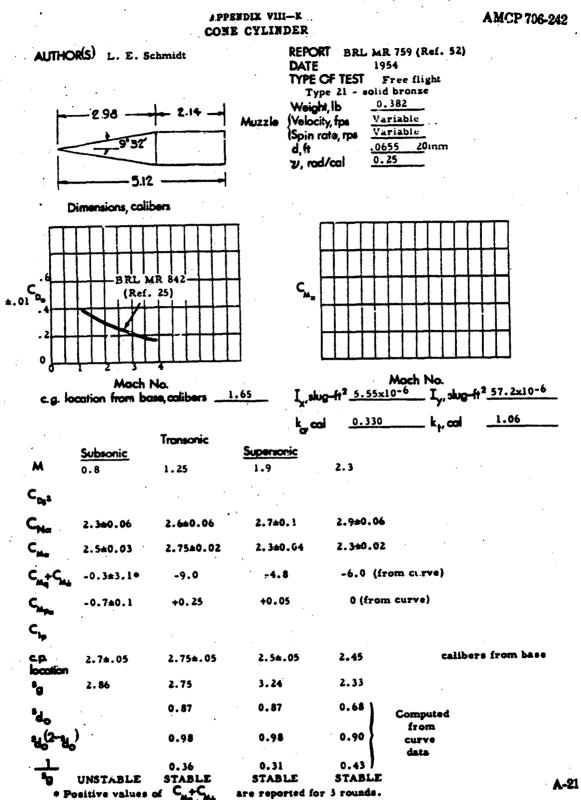
> $\boldsymbol{R}_{_{\mathbf{T}}}$ is the radius of a tangent ogive, in calibers. For this projectile $R_{m} = 9.47$ calibers.



A-19

Comment





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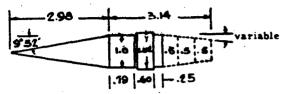
AMCP 706-242

APPENDIX VIII-L EFFECT OF BOATTAILING ON C.

AUTHOR(S) E. R. Dickinson

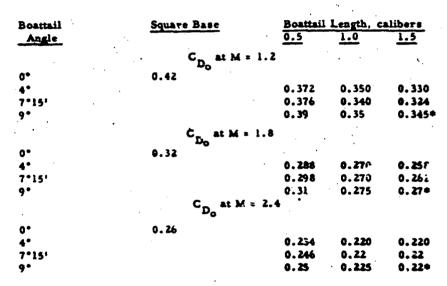
REPORT BRL: MR #42 (Ref. 25) DATE 1954 TYPE OF TEST Free flight

d = .0417 ft



PART I Effect of adding to length of projectile, and diminishing the area of the base, by adding boattail.

Dimensions, colibers



The C_{D_0} values shown were read from the curves in MR 842. The scatter of the observations averaged about ± 0.005 . Variation in surface finish, by

affecting the boundary layer transition, may account for much of the scatter.

*The 9°, 1.5 caliber boattail was a dynamically unstable configuration; these data are for a 9°, 1.25 caliber boattail.

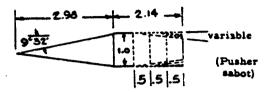
APPENDIX VIII-L EFFECT OF BOATTAILING ON C_s (cont'd)

AMCP 706-242

¹ A-23

AUTHOR(S) E. R. Dickinson

REPORT BRL MR 842 (Ref. 25) DATE 1954 TYPE OF TEST Free flight

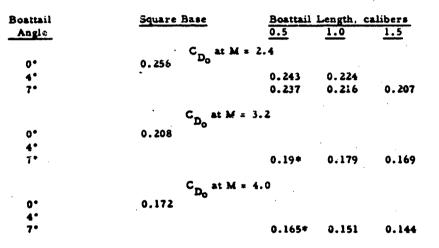


Dimensions, calibers

PART II

Effect of increasing the length of the boattail, and diminishing the area of the base, while keeping the overall length of the projectile constant.

d = .0655 ft = 20mm



The C values shown were read from the curves in MR 842. The scatter of the observations averaged about ± 0.003 .

Estimated effect of adding a driving band (rotating ring) is to add 0.01, or less, to the values shown assuming that the band does not extend to within less than 0.25 calibers of the boutsil.

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*These values were read from an interpolated curve.

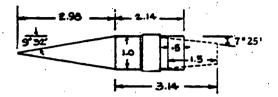
AMCP 706-242

A-24

APPENDIX VIII-M EFFECT OF BOATTAIL ON C_{p_1} AT M = 2.44

AUTHOR(S) T. Hailperin

REPORT BRL MR 347 (Ref. 26) DATE 1945 TYPE OF TEST Free flight

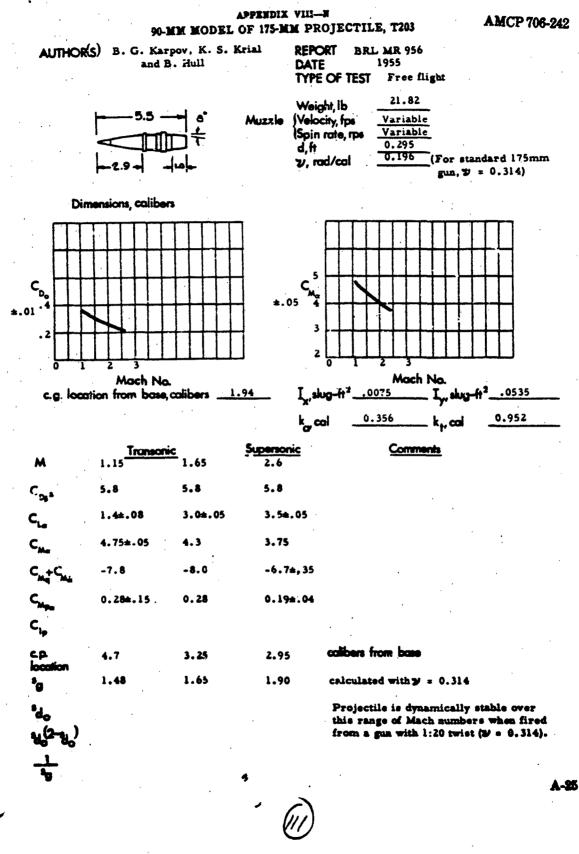


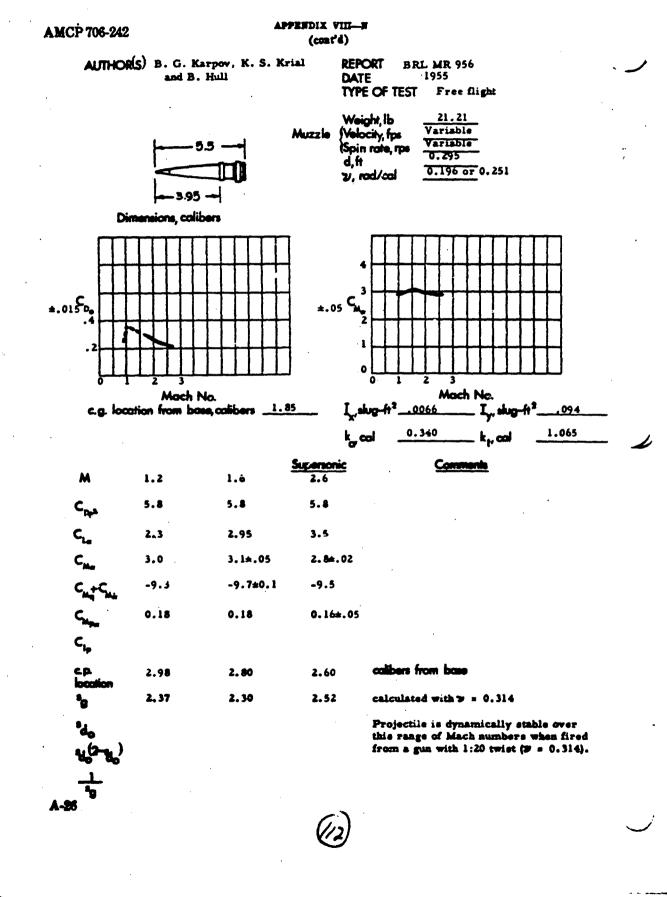
Dimensions, colibars

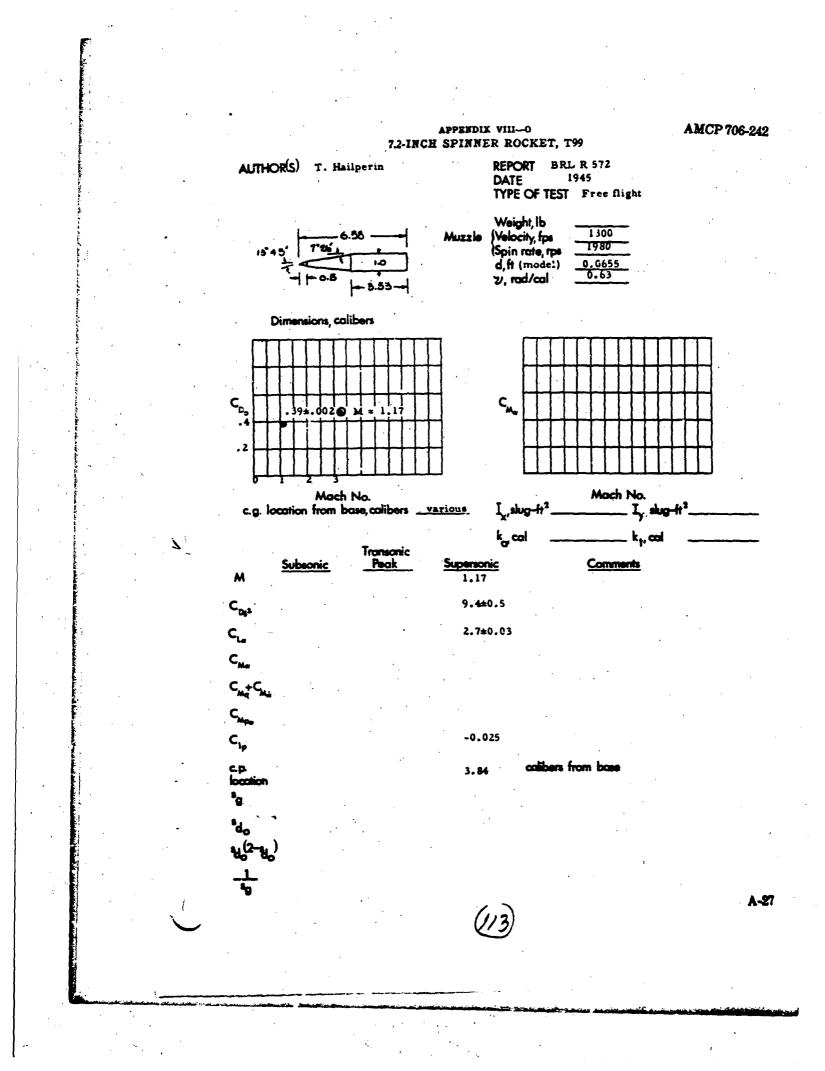
d = 0.0417 ftM = 2.44

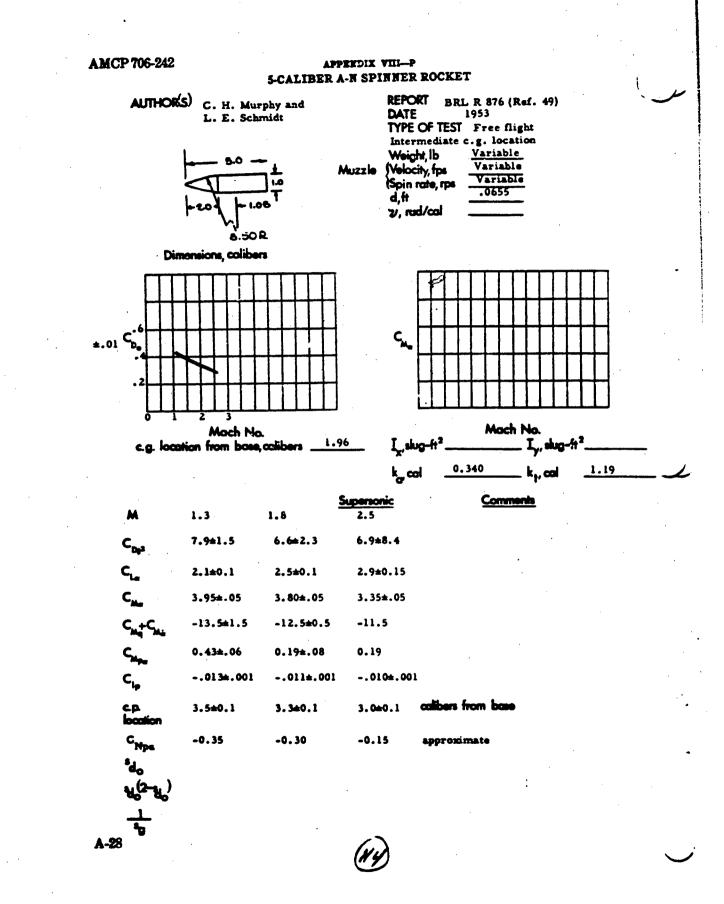
| • | , | Boattail Length, calibers | |
|-------------------|----------------|---------------------------|----------------|
| Base Area | Square Base | 0.5 | 1.5 |
| Frontal Area | 1.0 | 0.76 | 0.39 |
| C _{Do} . | 0.263 ±.027 | 0.248 ±.004 | 0.228 ±.005 |
| CDSI | 6.7 | 5.1 | 4.5 |

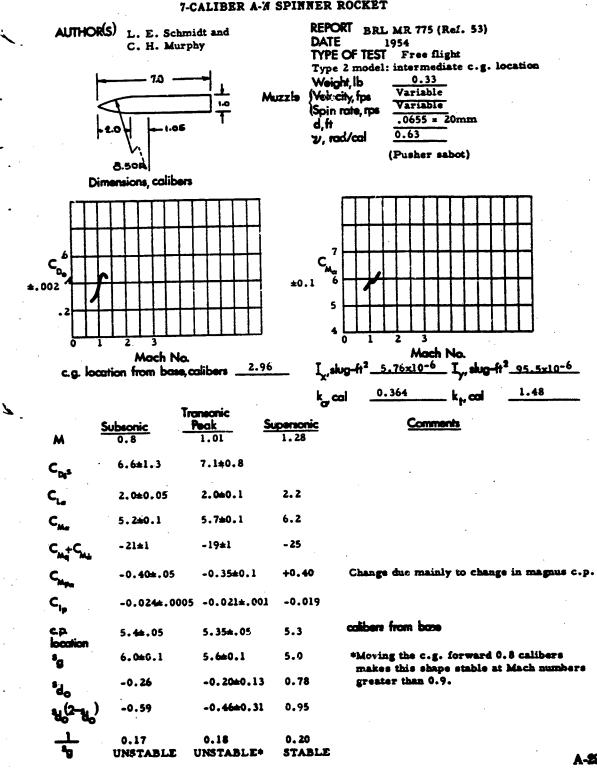








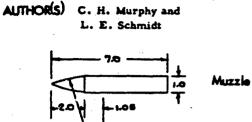




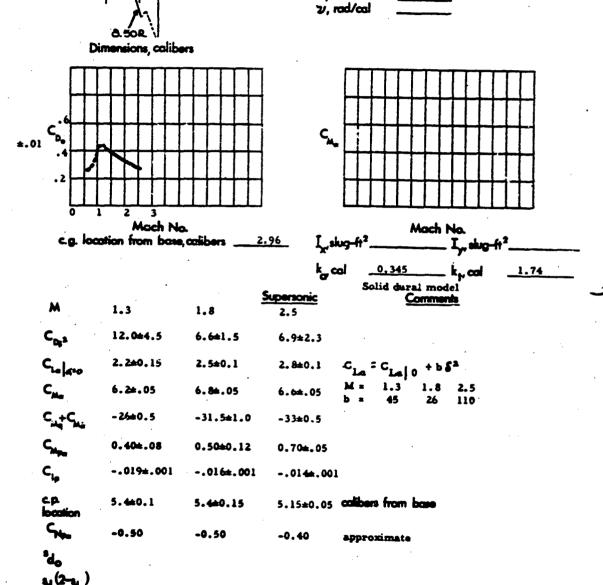
APPE IDIX VIII-Q 7-CALIBER A-X SPINNER ROCKET

A-29

APPENDIX VIII—12 7-CALIBER A-N SPINNER ROCKET



REPORT BRL R 876 (Ref. 49) DATE 1953 TYPE OF TEST Free flight Intermediate c.g. location Weight, lb Variable (Velocity, fps Variable Spin role, rps Variable d, ft 0.655

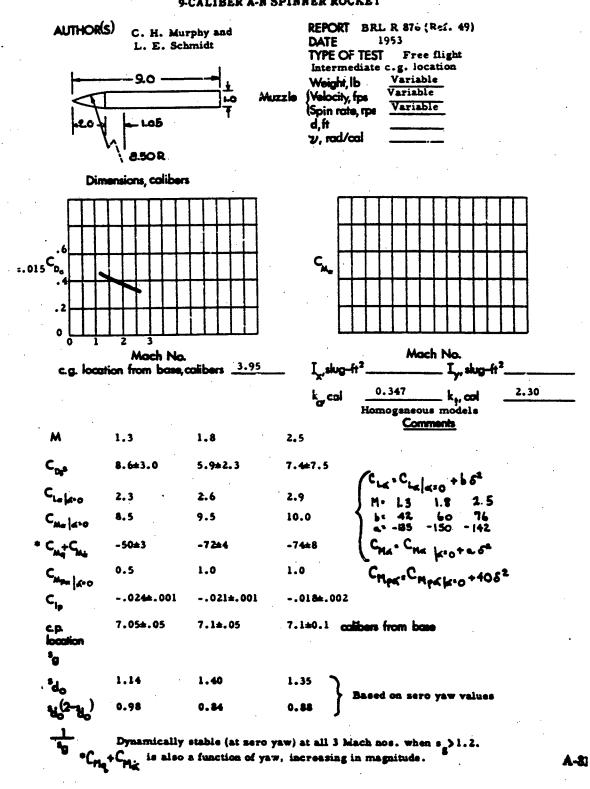


All test rounds were dynamically stable; s 21.5.

A-30

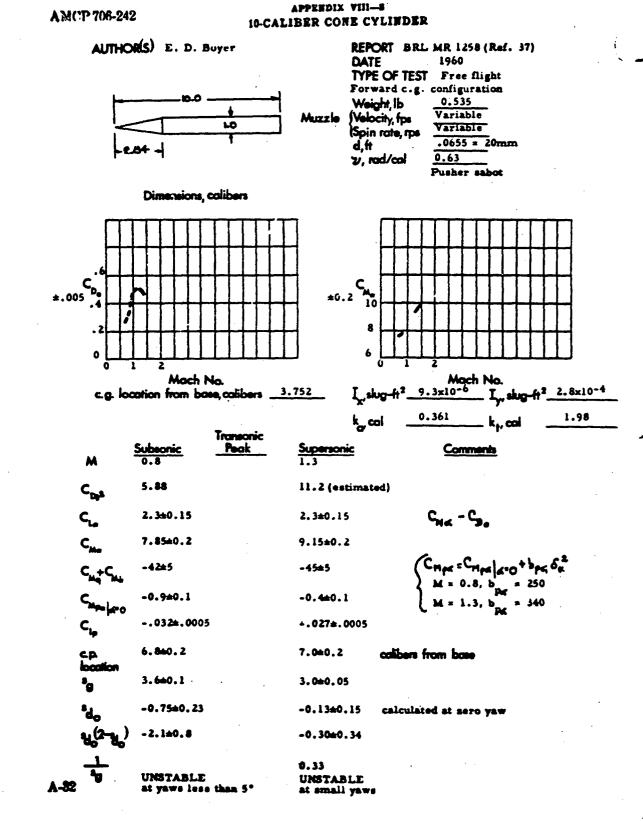
16

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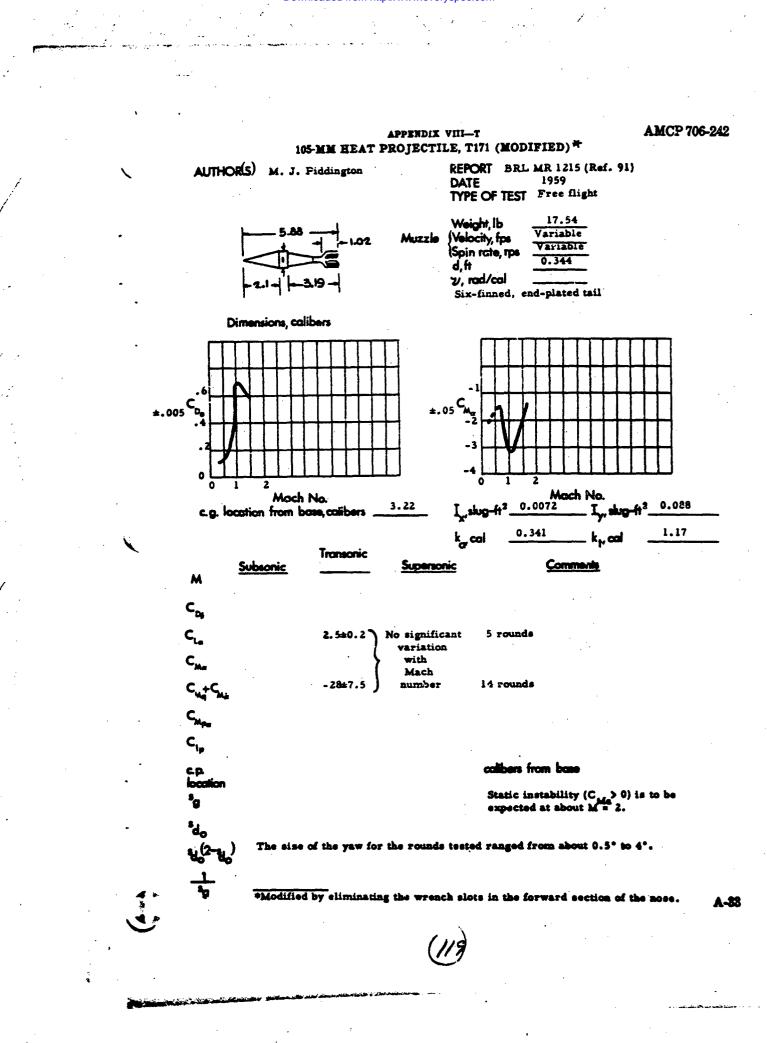


APPENDIX VIII --R 9-CALIBER A-N SPINNER ROCKET

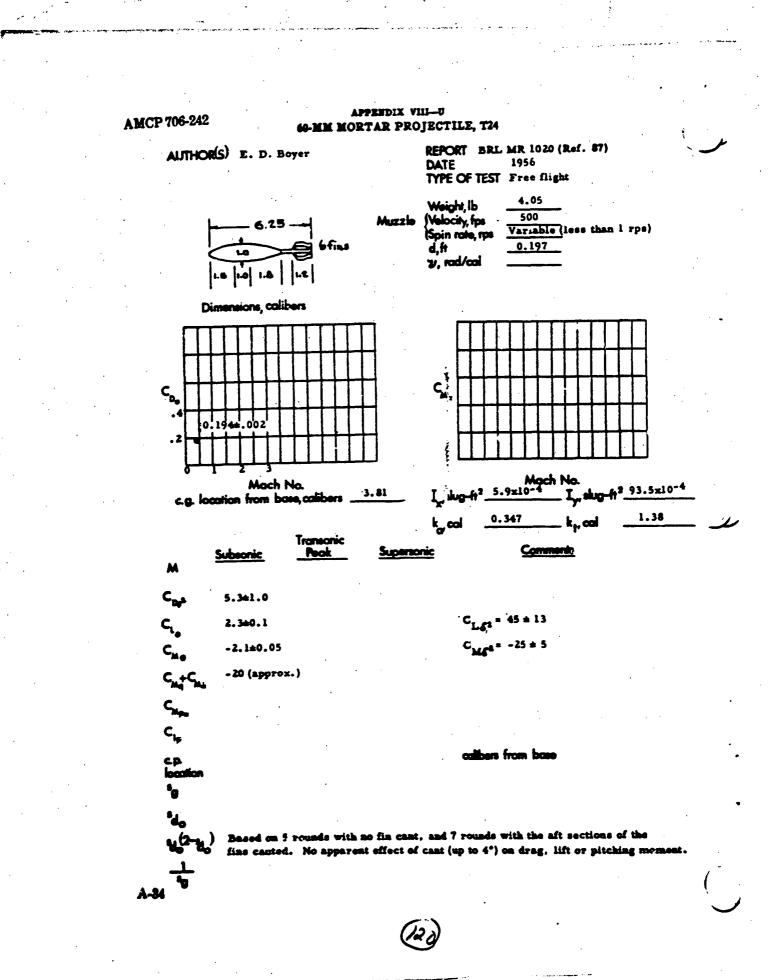
 $\overline{(1)}$

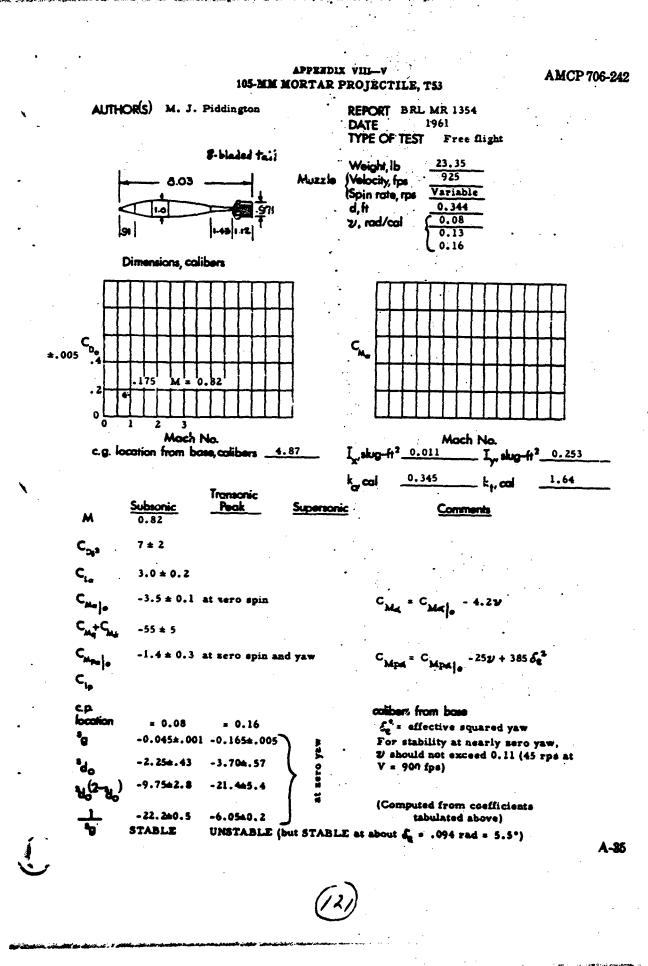


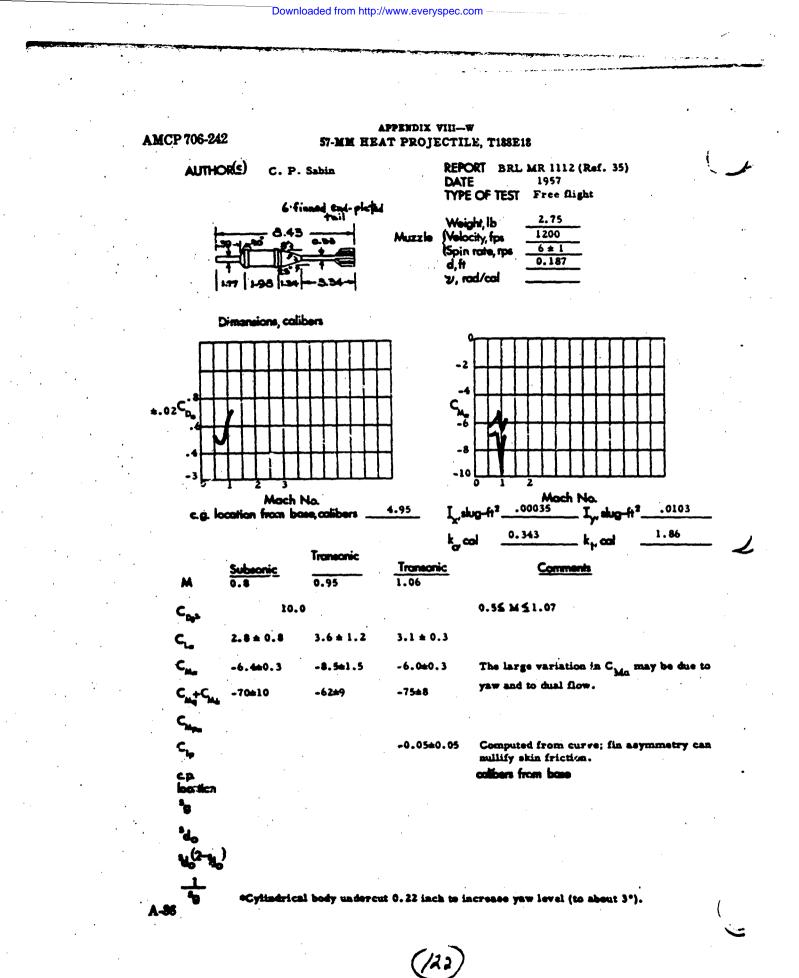
(18)

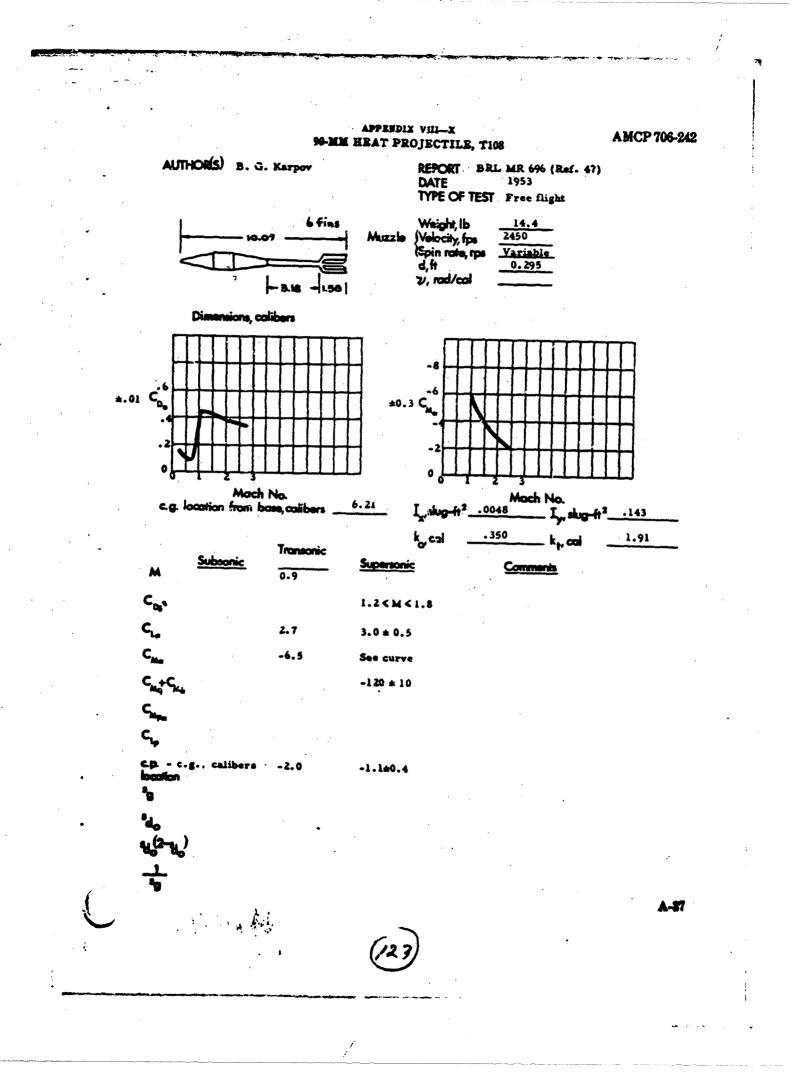


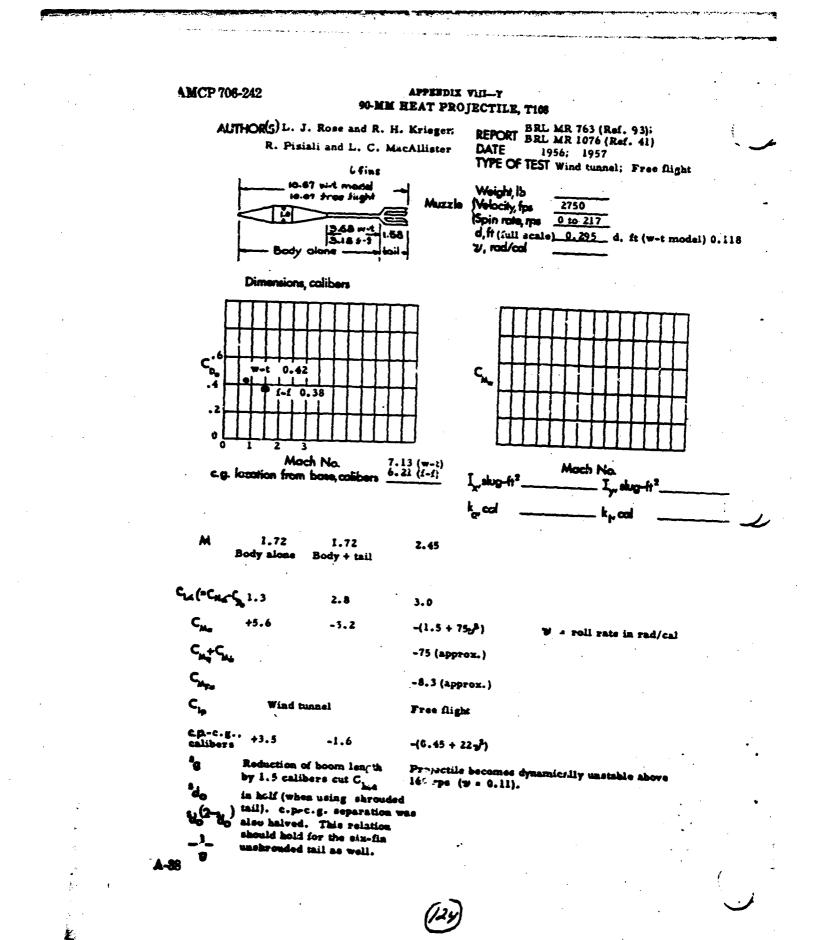
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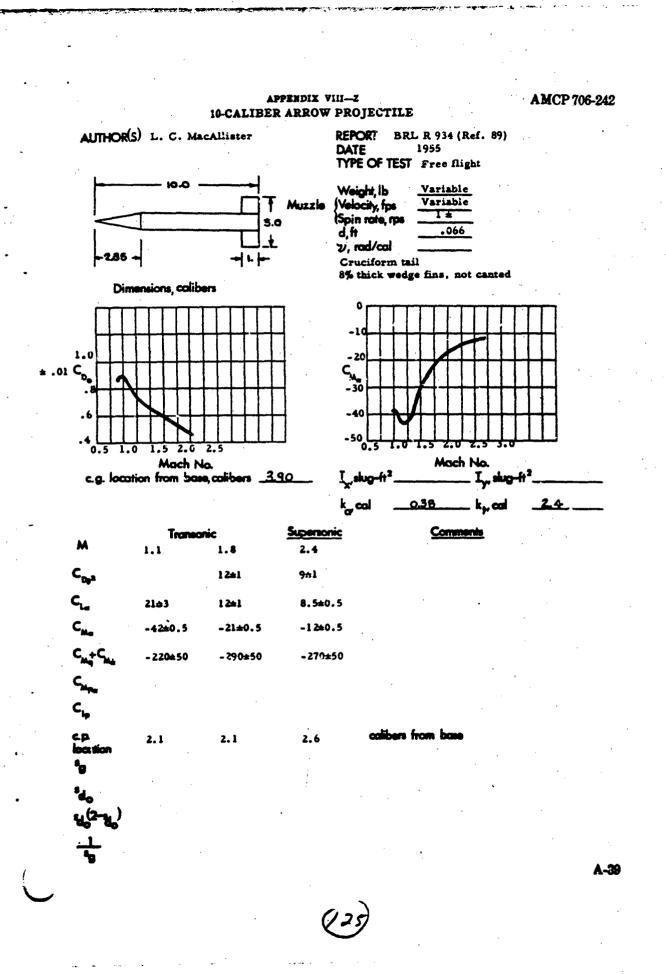












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| APPENDIX IX |
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| TRAJECTORY PROGRAM IN FORTRAN LANGUAGE |
| |
| DIHENSION CD8(9,2), CHA(9,2) |
| 1 FORMAT (49H HEAU)1953 |
| 6 FORMAT (F7.2,F8.0,F8.0,F7.1,F6.3,F6.2,F7.3,F6.2) 9 FORMAT (F6.3,F6.3,F6.3,F6.3,F6.3,F8.4) |
| 10 FORMAT (F8.6,F7.1) |
| 7 FORMAT (2H) |
| 100 READ 1 |
| READ 6, D, ZT, WTO, WTB, SPIS, SBT, OE, WO READ 6, FFD, FFH, CDD2, TWIST, CLP, PINT, RGA, RGT, DTE, DTL, DTH, ZO, TEMP |
| |
| 11 READ 9, CDO(1,1), CDO(1,2), X, CHA(1,1), CHA(1,2) |
| PRINT 1 PRINT 7 |
| READ 1 |
| PRINT 1 |
| PRINT 9, FFD, FFH, X, RGA, RGT, D |
| PAUSE 20 if (SENSE SWITCH 1) 21,22 |
| 21 ACCEPT 6. DE. SBT |
| 22 IF (SENSE SWITCH 2) 23,26 |
| 23 ACCEPT 6, FFD, VO,DTL,DTH 26 READ 1 |
| PRINT 1 |
| PRINT 6, WTO, VO, SPIS, SBT, DTH, TWIST, QE |
| PRINT 1 P |
| PRINT 6, WTB, ZO, TEMP, DTL, DTE, CD2, CLP |
| PRINT 7 |
| THST = 0.0 IF (WTO-WTB) 29, 29, 96 |
| 96 THST=(WTO-WTB) *SPIS /SBT |
| DWLSS=THST/(32,17=5P15) |
| 29 TEMPR = 518./(459.+TEMP) VAO = 1116./(TEMPR=40.5) |
| RH005 = .00118947EHPR |
| PRINT 10, RHODS, VAO |
| PRINT 7 PAUSE (DR stands for 'Density Ratio') |
| IF (SENSE SWITCH 4) 20,97 |
| 97 READ 1 Time X Dist V CD IMADR Mass PRINT 1 |
| READ 1 Theta Z Thrust Drag Yaw Mach Spin SG |
| FRIRI I |
| PRINT 7 PINTT = 0.0 |
| THE = 0.0 |
| X = 0.0 |
| DIST = 0.0 |
| |

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APPENDIX IX (cost'4) THT = QE Z = Z0 ZF = Z0 S = $\sqrt{20}$ Y = $\sqrt{20}$ Y = $\sqrt{20}$ Y = $\sqrt{20}$ S = $\sqrt{17453294}$ V = $\sqrt{20}$ IF (TWIST) 30, 31, 30 30 SGC = $R_{CA+44}/(4, 0+RH005+5)0+RGT+2)$ GNU = 6, 2832/TWIST YRC = 322.1748(CA+22/(RH005+5)) C = (RD GF INTIALIZATION 31 IF (Z-30000.) 32, 33, 33 32 RH0 = 2KPF(-3, 2Z-05+2)G0 T0 34 HO = 32289+2FF(-4, 6Z-05+(Z-30000.))33 RH0 = 32289+2FF(-4, 6Z-05+(Z-30000.))34 IF (Z-35500.) 35, 36, 36 35 VH = $\sqrt{170}$. 36 VH = $\sqrt{170}$. 37 IF (CD0(9, 1)-VH) 38, 38, 39 38 C0 = C00(9, 2) 39 I=Z 40 DIFF = VM-CD0(1, 1) IF (C1FF) 41, 41, 42 41 C0 = CC00(1, 2)+0IFF(CD0(1, 2)-CD0(1-1, 2))/(CD0(1, 1)-CD0(1-1, 1))) GD T0 43 42 I=1+1

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40 DIFF = VM-CDO(1,1) 1F (DIFF) 41,41,42 41 CD = CDO(1,2)+DIFF*(CDO(1,2)-CDO(1-1,2))/(CDO(1,1)-CDO(1-1,1)) GO TO 43 42 i=1+1 GO TO 40 43 CD = FFD*CD 1F (TWIST)44,95,44 44 IF (CMA(9,1)-VM) 45,45,46 45 CM = CMA(9,2) GO TO 50 46 1=2 47 DIFF = VM-CMA(1,1) 1F (DIFF) 48,48,49 48 CH = CMA(1,2)+DIFF*(CMA(1,2)-CMA(1-1,2))/(CMA(1,1)-CMA(1-1,1)) GO TO 50 49 1=1+1 SG = SGC*(GNU*2)*PMASS/(RHO*CH) 1F (SG-1.0) 51,51,53 51 PRINT 52, SG 52 FORMAT (F10.3,10H UNSTABLE) 53 YR = (YRC*PMASS*GNU/(RHO*CM*V**2)) * COSF (THETA) CD = CD + CD02*YR**2 95 GACC = -32.17*SINF(THETA) DRAG = RHOO5*RHO*(V**2)*5*CD ACC = GACC + (THST-DRAG)/PMASS

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APPENDIX IX (cont'd)

DT = DTL/(ACC*ACC) +*DTE IF (DT-OTH) 60,60,59 59 DT = DTH 60 IF (SENSE SMITCH 1) 57,55 55 PINTT = PINTT-1.0 IF (PINTT) 57,57,56 56 IF (THYT*HETA) 70,70,58 70 ZF = ZT 57 PRINT 6, THETA,2,DIST, V,CD,CM,RHO,PMASS PRINT 6, THETA,2,THST,DRAG,YR,VH,GNU,SG,DT PINTT = PINT IF (SENSE SMITCH 2)54,58 54 ACCEPT 6,DTL,DTM 58 IF (TINE-SET) 62,61,61 61 IF (THST)64,64,65 63 THST = 0.0 PMASS = VTB/32.17 G0 TO 57 62 IF (TINE-VDA,64,63 63 DT = DTM/A.0 64 DRAG = DRAG*(1.0+2.0*ACC*DT/V) ACCT = GACC + (THST-ORAG)/PHASS VBAR = V + (ACC+ACCT)*DT/4.0 DS = VBAR*DT V = 2.0*MPAR - V DIST = DIST + DS TIME = TINE + DT TH = TINETA - 16.09*COSF(THETA)*DT/VBAR X = X + DS*COSF(THBAR) Z = Z + DS*SINF(THBAR) Z = Z + DS*SINF(THBAR) THETA - THETA - 32.17*CCOSF(THBAR)*DT/VBAR GBU = GRU*(1.0 +((DRAG*CLP/(PHASS*CD*RGA**2))-ACCT)*DT/V) C i2ST FOR END OF TRAJECTORY IF (Z-ZF) 67, 67, 31 67 DS = (ZT-2)/SINF(THETA) THETA - THETA - 32.17*COSF(THBAR)*DT/VBAR GBU = GRU*(1.0 +((DRAG*CLP/(PHASS*CD*RGA**2))-ACCT)*DT/V) C i2ST FOR END OF TRAJECTORY IF (Z-ZF) 67, 67, 31 67 DS = (ZT-2)/SINF(THETA) THETA - THETA/.01745325 READ 1 PRINT 1 PRINT 6, TIME, X, V, THETA, GNU, SG PNUSE IF (SENSE SWITCH 4) 20,100 END

SW 1 ONFOR SYMBOL TABLE

FFD Ratio of drag coefficient curve to typical curve in memory FFM Ratio of static moment coefficient curve to typical curve in memory TYPE Identification of typical drag and moment curves in memory RGA Axial radius of gyration, calibers RGT Transverse radius of gyration, calibers D Maximum body diameter, ft

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APPENDIX IX (cont'd)

WTO Projectile weight at launch, 1b

Projectile velocity at launch, fps VO

SPIS Specific impulse of rocket fuel, sec SBT

SBT Rocket motor burning time, sec TWIST Twist of rifling, calibers per turn AE Quadrant elevation, deg

WTB.

Projectile weight at rocket burnout, 1b 7.0

ZT

Elevation of launcher, ft Elevation of target, ft Air temperature at launcher, O Yaw-drag coefficient, per rad? TEMP CDD 2

CLP

Roll damping moment coefficient Numerator of expression used to compute time intervals DTL

Exponent in expression used to compute time intervals Maximum length of time interval permitted DTE DTH

PINT Number of time intervals between automatic print-outs CDO(1,1) Element of mach no. column in drag coefficient table CDO(1,2) Element of drag coeff. column in drag coefficient table CMA(1,1) Element of mach no. column in moment coefficient table CMA(1,2) Element of static moment coeff. column in moment coeff. table THST Rocket thrust, 1b

THST Rocket thrust, 1D DMASS Rate of change of projectile mass, slugs/sec TEMPR Ratio of std. absolute temp.to absolute temp.of air at launcher VAO Sea level (Z=O) vel. of sound in air at temp.of air at launcher RHOO5 (ne-half air density at sea level at air temp.at launch, slugs/ft³ Horizontal distance from launcher in range direction, ft DIST Arc distance along trajectory, from launcher, ft THT Variable carrying sign of traj.angle at beginning of time interval S Frontal area of projectile, ft²

PMASS Projectile mass, slugs

Projectle mass, slugs THBAR Trajectory angle at middle of time interval, radians THETA Trajectory angle at end of time interval, radians V Projectile velocity, fps SGC Constant in computation of gyroscopic stability factor GNU Spin of projectile, rad/cal YRC Constant in computation of yaw of repose, ft²/ slug . sec² Z Altitude of projectile, measured from sea level, ft RHO Ratio of air density at altitude to density at sea level WH Mach number

VM Mach number

Drag coefficient CD.

DIFF Mach no.difference from tabular value, for interpolation in table Static moment coefficient, per radian Gyroscopic stability factor CM SG

YR Yaw of repose, radians

FINTT Counter for automatic print-out TIME Elapsed time since launch, sec

GACC

Projectile acceleration along trajectory, due to gravity, ft/sec² DRAG Drag, 1b ACC

Proj.acceleration along traj.at beginning of time interval, ft/sec² Proj.acceleration along traj.at end of interval, ft/sec² ACCT

30Blank

DT Length of time interval, sec

VBAR

Average velocity over time interval, fps Arc distance traveled during time interval, ft DS

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